

t3_domain_1
(TMX3yHvZV2LHB5irvd1CYQMkubwzt66toV6)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k3_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_xtuple_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. \forall X5. \\ (k3_xtuple_0 X0 X1 X2 \in k3_zfmisc_1 X3 X4 X5) & \Leftrightarrow ((X0 \in X3) \wedge ((X1 \in X4) \wedge \\ & (X2 \in X5))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \neg(X0 \in k3_zfmisc_1 \\ X1 X2 X3) & \wedge (\forall X4. \forall X5. \forall X6. \neg(X4 \in X1) \wedge ((X5 \in X2) \wedge \\ & ((X6 \in X3) \wedge (X0 = k3_xtuple_0 X4 X5 X6)))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. (m1_subset_1 X0 X1) \Rightarrow ((v1_xboole_0 X1) \vee (X0 \in X1)) \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1_subset_1 X0 X1) \tag{4}$$

Theorem 1

$$\begin{aligned} & \forall X0. \forall X1. (\neg v1_xboole_0 X1) \Rightarrow (\forall X2. (\neg v1_xboole_0 \\ X2) & \Rightarrow (\forall X3. (\neg v1_xboole_0 X3) \Rightarrow ((X0 \in k3_zfmisc_1 X1 X2 X3) \Leftrightarrow \\ & (\exists X4. (m1_subset_1 X4 X1) \wedge (\exists X5. (m1_subset_1 X5 X2) \wedge \\ & (\exists X6. (m1_subset_1 X6 X3) \wedge (X0 = k3_xtuple_0 X4 X5 X6))))))) \end{aligned}$$