

t3\_gate\_2  
(TMcLFzD7Nk1v7a1uh23srERqSGHrDQp4xT2)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k2\_gate\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_gate\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_gate\_1 : \iota \Rightarrow \iota$  be given. Let  $k8\_gate\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. (\neg(\neg v1\_xboole\_0 (k3\_gate\_1 X0 X1)) \wedge ((v1\_xboole\_0 X0) \wedge (v1\_xboole\_0 X1))) \wedge (\neg(\neg(v1\_xboole\_0 X0) \wedge (v1\_xboole\_0 X1)) \wedge (v1\_xboole\_0 (k3\_gate\_1 X0 X1))) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (\neg v1\_xboole\_0 (k2\_gate\_1 X0 X1)) \Leftrightarrow ((\neg v1\_xboole\_0 X0) \wedge (\neg v1\_xboole\_0 X1)) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. (\neg v1\_xboole\_0 (k8\_gate\_1 X0 X1 X2)) \Leftrightarrow ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge (\neg v1\_xboole\_0 X2))) \quad (3)$$

Assume the following.

$$\forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (v1\_xboole\_0 (k1\_gate\_1 X0)) \quad (4)$$

Assume the following.

$$\forall X0. (v1\_xboole\_0 X0) \Rightarrow (\neg v1\_xboole\_0 (k1\_gate\_1 X0)) \quad (5)$$

Assume the following.

$$\forall X0. \forall X1. k3\_gate\_1 X0 X1 = k3\_gate\_1 X1 X0 \quad (6)$$

Assume the following.

$$\forall X0. \forall X1. k2\_gate\_1 X0 X1 = k2\_gate\_1 X1 X0 \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(\neg(v1\_xboole\_0 ( \\ & k2\_gate\_1 X0 X1))\wedge(v1\_xboole\_0 (k3\_gate\_1 (k1\_gate\_1 X0) (k1\_gate\_1 \\ & X1))))\wedge(((\neg v1\_xboole\_0 (k3\_gate\_1 (k1\_gate\_1 X0) (k1\_gate\_1 \\ & X1)))\Rightarrow(v1\_xboole\_0 (k2\_gate\_1 X0 X1)))\wedge(\neg(\neg v1\_xboole\_0 (k3\_gate\_1 \\ & X0 X1))\wedge(\neg v1\_xboole\_0 (k3\_gate\_1 X2 X1))\wedge(v1\_xboole\_0 (k3\_gate\_1 \\ & (k2\_gate\_1 X0 X2) X1))))\wedge(((\neg v1\_xboole\_0 (k3\_gate\_1 (k2\_gate\_1 \\ & X0 X2) X1))\Rightarrow((\neg v1\_xboole\_0 (k3\_gate\_1 X0 X1))\wedge(\neg v1\_xboole\_0 ( \\ & k3\_gate\_1 X2 X1))))\wedge(\neg(\neg v1\_xboole\_0 (k3\_gate\_1 X0 X1))\wedge(\neg v1\_xboole\_0 \\ & (k3\_gate\_1 X2 X1))\wedge(\neg v1\_xboole\_0 (k3\_gate\_1 X3 X1))\wedge(v1\_xboole\_0 \\ & (k3\_gate\_1 (k8\_gate\_1 X0 X2 X3) X1))))\wedge(((\neg v1\_xboole\_0 (k3\_gate\_1 \\ & (k8\_gate\_1 X0 X2 X3) X1))\Rightarrow((\neg v1\_xboole\_0 (k3\_gate\_1 X0 X1))\wedge(( \\ & \neg v1\_xboole\_0 (k3\_gate\_1 X2 X1))\wedge(\neg v1\_xboole\_0 (k3\_gate\_1 X3 X1))))))\wedge \\ & (\neg(\neg v1\_xboole\_0 (k3\_gate\_1 X0 X1))\wedge(\neg(\neg v1\_xboole\_0 X0)\wedge(v1\_xboole\_0 \\ & X2))\wedge(\neg(\neg v1\_xboole\_0 X2)\wedge(v1\_xboole\_0 X0))\wedge(v1\_xboole\_0 ( \\ & k3\_gate\_1 X2 X1))))))))) \end{aligned}$$