

## t3\_group\_9

(TMWnM3mMvpoWgDTvBjy1e4U1PgD9nvksxpM)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_group\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v3\_group\_9 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_group\_9 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_group\_9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k6\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l3\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_group\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_group\_9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_group\_1 X0) \wedge (l3\_algstr\_0 X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_group\_2 X3 X0) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X3)) \Rightarrow (\forall X5. \\ & (m1\_subset\_1 X5 (u1\_struct\_0 X3)) \Rightarrow (((X4 = X1) \wedge (X5 = X2)) \Rightarrow (k6\_algstr\_0 X3 X4 X5 = k6\_algstr\_0 X0 X1 X2)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v2\_group\_1 X1) \wedge (v3\_group\_1 X1) \wedge ((v3\_group\_9 X1 X0) \wedge (l1\_group\_9 X1 X0)))) \Rightarrow ( \\ & \forall X2.(m1\_group\_9 X2 X0 X1) \Rightarrow ((\neg v2\_struct\_0 X2) \wedge ((v2\_group\_1 X2) \wedge (v3\_group\_1 X2) \wedge ((v3\_group\_9 X2 X0) \wedge (l1\_group\_9 X2 X0)))) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.(l1\_group\_9 X1 X0) \Rightarrow (l3\_algstr\_0 X1) \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1) \wedge ((v2\_group\_1 X1) \wedge (v3\_group\_1 X1) \wedge ((v3\_group\_9 X1 X0) \wedge (l1\_group\_9 X1 X0)))) \Rightarrow ( \\ & \forall X2.((\neg v2\_struct\_0 X2) \wedge ((v2\_group\_1 X2) \wedge (v3\_group\_1 X2) \wedge ((v3\_group\_9 X2 X0) \wedge (l1\_group\_9 X2 X0)))) \Rightarrow ((m1\_group\_9 X2 X0 X1) \Leftrightarrow ((m1\_group\_2 X2 X1) \wedge (\forall X3.(m1\_subset\_1 X3 X0) \Rightarrow (k3\_group\_9 X0 X2 X3 = k2\_partfun1 (u1\_struct\_0 X1) (u1\_struct\_0 X1) (k3\_group\_9 X0 X1 X3) (u1\_struct\_0 X2)))) \end{aligned} \quad (4)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2\_struct\_0 X1) \wedge ((v2\_group\_1 X1) \wedge \\ & (v3\_group\_1 X1) \wedge ((v3\_group\_9 X1 X0) \wedge (l1\_group\_9 X1 X0)))) \Rightarrow ( \\ & \quad \forall X2. (m1\_group\_9 X2 X0 X1) \Rightarrow (\forall X3. (m1\_subset\_1 X3 ( \\ & \quad u1\_struct\_0 X1) \Rightarrow (\forall X4. (m1\_subset\_1 X4 (u1\_struct\_0 X1) \Rightarrow \\ & \quad (\forall X5. (m1\_subset\_1 X5 (u1\_struct\_0 X2) \Rightarrow (\forall X6. (m1\_subset\_1 \\ & X6 (u1\_struct\_0 X2) \Rightarrow (((X5 = X3) \wedge (X6 = X4) \Rightarrow (k6\_algstr\_0 X2 X5 X6 = \\ & \quad k6\_algstr\_0 X1 X3 X4)))))))))) \end{aligned}$$