

# t3\_lpspace1 (TMN- VChx3Wt219nWQ5U8YqnRtV5qtRoGR2V9)

October 27, 2020

Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v5\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v6\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v7\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v8\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $l1\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_lpspace1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $g1\_rlvect\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_7 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_lpspace1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k1\_realset1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_rlvect\_1 : \iota \Rightarrow \iota$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v8\_rlvect\_1 X0) \wedge (l1\_rlvect\_1 X0)))))))))) \Rightarrow \\
& (\forall X1.((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 X2 (u1\_struct\_0 X0) X1) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (k2\_zfmisc\_1 X1 X1) X1) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 X1 X1) X1)))) \Rightarrow (\forall X4.((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (k2\_zfmisc\_1 k1\_numbers X1) X1) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 k1\_numbers X1) X1)))))) \Rightarrow (((X2 = k4\_struct\_0 X0) \wedge ((X3 = k1\_realset1 (u1\_algstr\_0 X0) X1) \wedge (X4 = k2\_partfun1 (k2\_zfmisc\_1 k1\_numbers (u1\_struct\_0 X0)) (u1\_struct\_0 X0) (u1\_rlvect\_1 X0) (k2\_zfmisc\_1 k1\_numbers X1)))) \Rightarrow ((v2\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge ((v3\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge ((v4\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge ((v5\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge ((v6\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge ((v7\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4)) \wedge (v8\_rlvect\_1 (g1\_rlvect\_1 X1 X2 X3 X4))))))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 \\ X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.(l1\_rlvect\_1 X0) \Rightarrow (l2\_algstr\_0 X0) \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((\neg v2\_struct\_0 X0) \wedge (l1\_rlvect\_1 X0)) \wedge \\ ((\neg v1\_xboole\_0 X1) \wedge ((v1\_lpspace\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0)))))) \Rightarrow ((v1\_funct\_1 (k1\_lpspace\_1 X0 X1)) \wedge (v1\_funct\_2 \\ (k1\_lpspace\_1 X0 X1) (k2\_zfmisc\_1 k1\_numbers X1) X1) \wedge (m1\_subset\_1 \\ (k1\_lpspace\_1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 k1\_numbers \\ X1) X1)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((\neg v2\_struct\_0 X0) \wedge (l2\_algstr\_0 X0)) \wedge \\ ((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0)))))) \Rightarrow ((v1\_funct\_1 (k1\_ideal\_1 X0 X1)) \wedge (v1\_funct\_2 \\ (k1\_ideal\_1 X0 X1) (k2\_zfmisc\_1 X1 X1) X1) \wedge (m1\_subset\_1 (k1\_ideal\_1 \\ X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 X1 X1) X1)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge (l2\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ ((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0)))))) \Rightarrow (k1\_ideal\_1 X0 X1 = k1\_realset1 (u1\_algstr\_0 \\ X0) X1)) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_rlvect\_1 X0)) \Rightarrow (\forall X1. \\ ((\neg v1\_xboole\_0 X1) \wedge ((v1\_lpspace\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0)))))) \Rightarrow (k1\_lpspace\_1 X0 X1 = k2\_partfun1 (k2\_zfmisc\_1 \\ k1\_numbers (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_rlvect\_1 X0) \\ (k2\_zfmisc\_1 k1\_numbers X1))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1) \Rightarrow (k1\_funct\_7 X0 X1 = X0) \quad (9)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)) \Rightarrow (v1\_xboole\_0 X1)) \quad (10)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge ((v6\_rlvect\_1 X0) \wedge \\ & ((v7\_rlvect\_1 X0) \wedge ((v8\_rlvect\_1 X0) \wedge (l1\_rlvect\_1 X0)))))))))) \Rightarrow \\ & (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge ((v1\_lpspace1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))) \Rightarrow (( \\ & k4\_struct\_0 X0 \in X1) \Rightarrow ((v2\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ( \\ & (v3\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ((v4\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ((v5\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ((v6\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ((v7\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1))) \wedge ( \\ & v8\_rlvect\_1 (g1\_rlvect\_1 X1 (k1\_funct\_7 (k4\_struct\_0 X0) X1) (k1\_ideal\_1 X0 X1) (k1\_lpspace1 X0 X1)))))))))))))) \end{aligned}$$