

t3\_scm\_inst  
(TMQfFLNXB81fUHiBLzqsptjzKgQbmj1cq7U)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k2\_scm\_inst : \iota$  be given. Let  $k7\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_7 : \iota$  be given. Let  $np\_8 : \iota$  be given. Let  $k3\_xtuple\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_scm\_inst : \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $np\_9 : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k6\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k1\_scm\_inst : \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_6 : \iota$  be given. Let  $k2\_finseq\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $np\_3 : \iota$  be given. Let  $np\_4 : \iota$  be given. Let  $np\_5 : \iota$  be given. Assume the following.

$$\forall X0.(v7\_ordinal1 X0) \Rightarrow (\forall X1.(v7\_ordinal1 X1) \Rightarrow ((X0 \in X1) \Leftrightarrow (\neg r1\_xxreal\_0 X1 X0))) \quad (1)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (2)$$

Assume the following.

$$((v2\_xxreal\_0 np\_9) \wedge (m2\_subset\_1 np\_9 k1\_numbers k5\_numbers)) \wedge ((m1\_subset\_1 np\_9 k5\_numbers) \wedge (m1\_subset\_1 np\_9 k1\_numbers)) \quad (3)$$

Assume the following.

$$((v2\_xxreal\_0 np\_8) \wedge (m2\_subset\_1 np\_8 k1\_numbers k5\_numbers)) \wedge ((m1\_subset\_1 np\_8 k5\_numbers) \wedge (m1\_subset\_1 np\_8 k1\_numbers)) \quad (4)$$

Assume the following.

$$((v2\_xxreal\_0 np\_7) \wedge (m2\_subset\_1 np\_7 k1\_numbers k5\_numbers)) \wedge ((m1\_subset\_1 np\_7 k5\_numbers) \wedge (m1\_subset\_1 np\_7 k1\_numbers)) \quad (5)$$

Assume the following.

$$\neg r1\_xreal\_0 \text{ np\_9 np\_8} \quad (6)$$

Assume the following.

$$\neg r1\_xreal\_0 \text{ np\_9 np\_7} \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge((m1\_subset\_1 X1 X0)\wedge(m1\_subset\_1 X2 X0)))\Rightarrow(k7\_domain\_1 X0 X1 X2 = k2\_tarski X1 X2) \quad (8)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0)\Rightarrow(k7\_card\_1 X0 = k6\_card\_1 X0) \quad (9)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (10)$$

Assume the following.

$$k1\_scm\_inst = k1\_xboole\_0 \quad (11)$$

Assume the following.

$$(\neg v1\_xboole\_0 k4\_ordinal1)\wedge(v3\_ordinal1 k4\_ordinal1) \quad (12)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0)\Rightarrow(k6\_card\_1 X0 = X0) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.k4\_tarski X0 X1 = k2\_tarski (k2\_tarski X0 X1) (k1\_tarski X0) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.k3\_xtuple\_0 X0 X1 X2 = k4\_tarski (k4\_tarski X0 X1) X2 \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(X2 = k2\_xboole\_0 X0 X1)\Leftrightarrow(\forall X3.(X3 \in X2)\Leftrightarrow((X3 \in X0)\vee(X3 \in X1))) \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(X2 = k2\_tarski X0 X1)\Leftrightarrow(\forall X3.(X3 \in X2)\Leftrightarrow((X3 = X0)\vee(X3 = X1))) \quad (17)$$

Assume the following.

$$\begin{aligned}
& k3\_scm\_inst = k2\_xboole\_0 (k2\_xboole\_0 (k2\_xboole\_0 (k1\_tarski \\
& (k3\_xtuple\_0 k1\_scm\_inst k1\_xboole\_0 k1\_xboole\_0)) (ReplSep2 \\
& (toset (\lambda X0 : \iota.m1\_subset\_1 X0 (k7\_card\_1 np\_9))) (\lambda X0 : \\
& \iota.toset (\lambda X1 : \iota.m1\_subset\_1 X1 k5\_numbers)) (\lambda X0 : \iota. \\
& \lambda X1 : \iota.X0 = np\_6) (\lambda X0 : \iota.\lambda X1 : \iota.k3\_xtuple\_0 X0 \\
& (k12\_finseq\_1 k5\_numbers X1) k1\_xboole\_0))) (ReplSep3 (toset \\
& (\lambda X0 : \iota.m1\_subset\_1 X0 (k7\_card\_1 np\_9))) (\lambda X0 : \iota. \\
& toset (\lambda X1 : \iota.m1\_subset\_1 X1 k5\_numbers)) (\lambda X0 : \iota.\lambda X1 : \\
& \iota.toset (\lambda X2 : \iota.m1\_subset\_1 X2 k2\_scm\_inst)) (\lambda X0 : \\
& \iota.\lambda X1 : \iota.\lambda X2 : \iota.X0 \in k7\_domain\_1 k5\_numbers np\_7 \\
& np\_8) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \iota.k3\_xtuple\_0 X0 (k12\_finseq\_1 \\
& k5\_numbers X1) (k12\_finseq\_1 k2\_scm\_inst X2)))) (ReplSep3 (toset \\
& (\lambda X0 : \iota.m1\_subset\_1 X0 (k7\_card\_1 np\_9))) (\lambda X0 : \iota. \\
& toset (\lambda X1 : \iota.m1\_subset\_1 X1 k2\_scm\_inst)) (\lambda X0 : \iota. \\
& \lambda X1 : \iota.toset (\lambda X2 : \iota.m1\_subset\_1 X2 k2\_scm\_inst)) ( \\
& \lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \iota.X0 \in k10\_domain\_1 k5\_numbers \\
& np\_1 np\_2 np\_3 np\_4 np\_5) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \\
& \iota.k3\_xtuple\_0 X0 k1\_xboole\_0 (k2\_finseq\_4 k2\_scm\_inst X1 X2)))
\end{aligned} \tag{18}$$

Assume the following.

$$\forall X0.\forall X1.k2\_xboole\_0 X0 X1 = k2\_xboole\_0 X1 X0 \tag{19}$$

Assume the following.

$$\forall X0.\forall X1.k2\_tarski X0 X1 = k2\_tarski X1 X0 \tag{20}$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k4\_ordinal1) \Rightarrow (v7\_ordinal1 X0) \tag{21}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.\forall X1.(m1\_subset\_1 X1 k5\_numbers) \Rightarrow (\forall X2. \\
& (m1\_subset\_1 X2 k2\_scm\_inst) \Rightarrow ((X0 \in k7\_domain\_1 k5\_numbers np\_7 \\
& np\_8) \Rightarrow (k3\_xtuple\_0 X0 (k12\_finseq\_1 k5\_numbers X1) (k12\_finseq\_1 \\
& k2\_scm\_inst X2) \in k3\_scm\_inst)))
\end{aligned}$$