

t3_stirl2_1

(TMQCGDhZbUmQ29kYyaMmDoz14LQmJLkMLSR)

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Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k5_numbers : \iota$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_nat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_nat_1 : \iota \Rightarrow \iota$ be given. Let $k4_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k6_seq_4 : \iota \Rightarrow \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $k2_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xxreal_0 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_numbers : \iota$ be given. Let $k3_xxreal_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $v3_membered : \iota \Rightarrow o$ be given. Let $v1_xreal_0 : \iota \Rightarrow o$ be given. Assume the following.

$$\forall X0.(v1_xboole_0 X0) \Rightarrow (X0 = k1_xboole_0) \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v1_xboole_0 X0) \wedge (m1_subset_1 X0 (k1_zfmisc_1 k5_numbers))) \Rightarrow \\ (\forall X1.((\neg v1_xboole_0 X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 \\ k5_numbers)))) \Rightarrow (k6_nat_1 (k6_seq_4 X0) (k6_seq_4 X1) = k6_seq_4 \\ (k4_subset_1 k5_numbers X0 X1))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.((\neg v1_xboole_0 X0) \wedge (m1_subset_1 X0 (k1_zfmisc_1 k5_numbers))) \Rightarrow \\ (k6_seq_4 X0 = k5_nat_1 X0) \tag{3}$$

Assume the following.

$$m1_subset_1 k1_xboole_0 k4_ordinal1 \tag{4}$$

Assume the following.

$$\forall X0.k2_xboole_0 X0 k1_xboole_0 = X0 \tag{5}$$

Assume the following.

$$\forall X0.\forall X1.((v1_xxreal_0 X0) \wedge (v1_xxreal_0 X1)) \Rightarrow (\\ r1_xxreal_0 X0 X0) \tag{6}$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X1 (k1_zfmisc_1 X0))))\Rightarrow(\forall X2.(m2_subset_1 X2 X0 X1)\Leftrightarrow(m1_subset_1 X2 X1)) \quad (7)$$

Assume the following.

$$k6_numbers = k1_xboole_0 \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.((m1_subset_1 X0 k5_numbers)\wedge(m1_subset_1 X1 k5_numbers))\Rightarrow(k6_nat_1 X0 X1 = k3_xxreal_0 X0 X1) \quad (9)$$

Assume the following.

$$k5_numbers = k4_ordinal1 \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1_subset_1 X1 (k1_zfmisc_1 X0))\wedge(m1_subset_1 X2 (k1_zfmisc_1 X0)))\Rightarrow(k4_subset_1 X0 X1 X2 = k2_xboole_0 X1 X2) \quad (11)$$

Assume the following.

$$(\neg v1_xboole_0 k4_ordinal1)\wedge(v3_ordinal1 k4_ordinal1) \quad (12)$$

Assume the following.

$$\forall X0.\forall X1.(\neg v1_xboole_0 X0)\Rightarrow(\neg v1_xboole_0 (k2_xboole_0 X1 X0)) \quad (13)$$

Assume the following.

$$m2_subset_1 k6_numbers k1_numbers k5_numbers \quad (14)$$

Assume the following.

$$m1_subset_1 k5_numbers (k1_zfmisc_1 k1_numbers) \quad (15)$$

Assume the following.

$$\forall X0.m2_subset_1 (k5_nat_1 X0) k1_numbers k5_numbers \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1_subset_1 X1 (k1_zfmisc_1 X0))\wedge(m1_subset_1 X2 (k1_zfmisc_1 X0)))\Rightarrow(m1_subset_1 (k4_subset_1 X0 X1 X2) (k1_zfmisc_1 X0)) \quad (17)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1_xxreal_0 X0) \Rightarrow (\forall X1.(v1_xxreal_0 X1) \Rightarrow ((\\ (r1_xxreal_0 X0 X1) \Rightarrow (k3_xxreal_0 X0 X1 = X0)) \wedge ((\neg r1_xxreal_0 X0 \\ X1) \Rightarrow (k3_xxreal_0 X0 X1 = X1)))) \end{aligned} \quad (18)$$

Assume the following.

$$k1_xboole_0 = \text{the } (\lambda X0 : \iota.v1_xboole_0 X0) \quad (19)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(m2_subset_1 X1 k1_numbers k5_numbers) \Rightarrow \\ (((\neg v1_xboole_0 X0) \wedge (m1_subset_1 X0 (k1_zfmisc_1 k5_numbers))) \Rightarrow \\ ((X1 = k5_nat_1 X0) \Leftrightarrow ((X1 \in X0) \wedge (\forall X2.(v7_ordinal1 X2) \Rightarrow ((\\ X2 \in X0) \Rightarrow (r1_xxreal_0 X1 X2)))))) \wedge ((\neg(\neg v1_xboole_0 X0) \wedge (m1_subset_1 \\ X0 (k1_zfmisc_1 k5_numbers))) \Rightarrow ((X1 = k5_nat_1 X0) \Leftrightarrow (X1 = k6_numbers)))) \end{aligned} \quad (20)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1_xxreal_0 X0) \wedge (v1_xxreal_0 X1)) \Rightarrow (\\ (r1_xxreal_0 X0 X1) \vee (r1_xxreal_0 X1 X0)) \end{aligned} \quad (21)$$

Assume the following.

$$\forall X0.\forall X1.k2_xboole_0 X0 X1 = k2_xboole_0 X1 X0 \quad (22)$$

Assume the following.

$$\forall X0.(m1_subset_1 X0 (k1_zfmisc_1 k1_numbers)) \Rightarrow (v3_membered \\ X0) \quad (23)$$

Assume the following.

$$\forall X0.(v1_xreal_0 X0) \Rightarrow (v1_xxreal_0 X0) \quad (24)$$

Assume the following.

$$\forall X0.(v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 \\ X0)) \Rightarrow (v1_xboole_0 X1)) \quad (25)$$

Assume the following.

$$\forall X0.(v3_membered X0) \Rightarrow (\forall X1.(m1_subset_1 X1 X0) \Rightarrow \\ (v1_xreal_0 X1)) \quad (26)$$

Theorem 1

$$\begin{aligned} \forall X0.(m1_subset_1 X0 (k1_zfmisc_1 k5_numbers)) \Rightarrow (\forall X1. \\ (m1_subset_1 X1 (k1_zfmisc_1 k5_numbers)) \Rightarrow (r1_xxreal_0 (k6_nat_1 \\ (k5_nat_1 X0) (k5_nat_1 X1)) (k5_nat_1 (k4_subset_1 k5_numbers \\ X0 X1)))) \end{aligned}$$