

## t41\_borsuk\_6

(TMF88vKU8i8NKqE1VnW77JG9NTF5eSgMEuH)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $m1\_borsuk\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_topmetr : \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k2\_borsuk\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_borsuk\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\
 & \quad X0))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
 & \quad (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\neg (\exists X3. ((v1\_funct\_1 \\
 & \quad X3) \wedge ((v1\_funct\_2 X3 (u1\_struct\_0 k5\_topmetr) (u1\_struct\_0 X0)) \wedge \\
 & \quad (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 k5\_topmetr) \\
 & \quad (u1\_struct\_0 X0)))))) \wedge ((v5\_pre\_topc X3 k5\_topmetr X0) \wedge ((k1\_funct\_1 \\
 & \quad X3 k6\_numbers = X1) \wedge (k1\_funct\_1 X3 np\_1 = X2)))))) \wedge (\forall X3. ( \\
 & \quad (v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (u1\_struct\_0 k5\_topmetr) (u1\_struct\_0 \\
 & \quad X0)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 \\
 & \quad k5\_topmetr) (u1\_struct\_0 X0)))))) \Rightarrow (\neg (v5\_pre\_topc X3 k5\_topmetr \\
 & \quad X0) \wedge ((k1\_funct\_1 X3 k6\_numbers = X2) \wedge (k1\_funct\_1 X3 np\_1 = X1))))))
 \end{aligned}
 \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. \forall X2. ((l1\_pre\_topc X0) \wedge ((m1\_subset\_1 \\
 & \quad X1 (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X2 (u1\_struct\_0 X0)))) \Rightarrow (\forall X3. \\
 & \quad (m1\_borsuk\_2 X3 X0 X1 X2) \Rightarrow ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (u1\_struct\_0 \\
 & \quad k5\_topmetr) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 ( \\
 & \quad k2\_zfmisc\_1 (u1\_struct\_0 k5\_topmetr) (u1\_struct\_0 X0))))))
 \end{aligned}
 \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((\neg v2\_struct\_0 \\ & X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc X0))) \wedge ((m1\_subset\_1 X1 ( \\ & u1\_struct\_0 X0)) \wedge ((m1\_subset\_1 X2 (u1\_struct\_0 X0)) \wedge (m1\_borsuk\_2 \\ & X3 X0 X1 X2)))) \Rightarrow (m1\_borsuk\_2 (k2\_borsuk\_2 X0 X1 X2 X3) X0 X2 X1) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. (l1\_pre\_topc X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow ((r1\_borsuk\_2 \\ & X0 X1 X2) \Rightarrow (\forall X3. ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (u1\_struct\_0 \\ & k5\_topmetr) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 (u1\_struct\_0 k5\_topmetr) (u1\_struct\_0 X0)))))) \Rightarrow \\ & ((m1\_borsuk\_2 X3 X0 X1 X2) \Leftrightarrow ((v5\_pre\_topc X3 k5\_topmetr X0) \wedge ((k1\_funct\_1 \\ & X3 k6\_numbers = X1) \wedge (k1\_funct\_1 X3 np\_1 = X2)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. (l1\_pre\_topc X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow ((r1\_borsuk\_2 \\ & X0 X1 X2) \Leftrightarrow (\exists X3. ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 (u1\_struct\_0 \\ & k5\_topmetr) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 (u1\_struct\_0 k5\_topmetr) (u1\_struct\_0 X0)))))) \wedge \\ & ((v5\_pre\_topc X3 k5\_topmetr X0) \wedge ((k1\_funct\_1 X3 k6\_numbers = X1) \wedge \\ & (k1\_funct\_1 X3 np\_1 = X2)))))) \end{aligned} \quad (5)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. (((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. (m1\_borsuk\_2 X3 \\ & X0 X1 X2) \Rightarrow (((v5\_pre\_topc X3 k5\_topmetr X0) \wedge ((k1\_funct\_1 X3 k6\_numbers = \\ & X1) \wedge (k1\_funct\_1 X3 np\_1 = X2))) \Rightarrow ((v5\_pre\_topc (k2\_borsuk\_2 X0 \\ & X1 X2 X3) k5\_topmetr X0) \wedge ((k1\_funct\_1 (k2\_borsuk\_2 X0 X1 X2 X3) k6\_numbers = \\ & X2) \wedge (k1\_funct\_1 (k2\_borsuk\_2 X0 X1 X2 X3) np\_1 = X1)))))) \end{aligned}$$