

t41_hilbert1

(TMHK5XJeeNHRr7atn4bS8ZDZ7u5EmGj5LWK)

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Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_hilbert1 : \iota$ be given. Let $k3_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_hilbert1 : \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k1_hilbert1) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k1_hilbert1) \Rightarrow (\forall X2.(m1_subset_1 X2 k1_hilbert1) \Rightarrow (k3_hilbert1 \\ & (k3_hilbert1 (k4_hilbert1 X0 X1) X2) (k3_hilbert1 (k4_hilbert1 \\ & X0 X1) (k4_hilbert1 X2 X1)) \in k6_hilbert1))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k1_hilbert1) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k1_hilbert1) \Rightarrow (\forall X2.(m1_subset_1 X2 k1_hilbert1) \Rightarrow (k3_hilbert1 \\ & (k3_hilbert1 X0 X1) (k3_hilbert1 (k4_hilbert1 X0 X2) X1) \in k6_hilbert1))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k1_hilbert1) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k1_hilbert1) \Rightarrow (\forall X2.(m1_subset_1 X2 k1_hilbert1) \Rightarrow ((\\ & (k3_hilbert1 X0 X1 \in k6_hilbert1) \wedge (k3_hilbert1 X1 X2 \in k6_hilbert1)) \Rightarrow \\ & (k3_hilbert1 X0 X2 \in k6_hilbert1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1_subset_1 X0 k1_hilbert1) \wedge (m1_subset_1 \\ & X1 k1_hilbert1)) \Rightarrow (m1_subset_1 (k4_hilbert1 X0 X1) k1_hilbert1) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1_subset_1 X0 k1_hilbert1) \wedge (m1_subset_1 \\ & X1 k1_hilbert1)) \Rightarrow (m1_subset_1 (k3_hilbert1 X0 X1) k1_hilbert1) \end{aligned} \quad (5)$$

Theorem 1

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k1_hilbert1) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k1_hilbert1) \Rightarrow (\forall X2.(m1_subset_1 X2 k1_hilbert1) \Rightarrow (k3_hilbert1 \\ & (k3_hilbert1 X0 X1) (k3_hilbert1 (k4_hilbert1 X0 X2) (k4_hilbert1 \\ & X1 X2)) \in k6_hilbert1))) \end{aligned}$$