

t42_cqc_the3 (TMHg- mEz42DaMbkKnviMMxWTyRy6HBbmZi87)

October 27, 2020

Let $m1_qc_lang1 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k9_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k3_cqc_lang : \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $r6_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r3_cqc_the1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8_cqc_lang : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v6_qc_lang1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r5_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r4_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r2_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k2_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_numbers : \iota$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $np_1 : \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_finseq_1 : \iota \Rightarrow o$ be given. Let $k3_finseq_1 : \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k3_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k2_nat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_cqc_lang : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0.(m1_qc_lang1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 \\
 & \quad (k3_cqc_lang X0))) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\
 & \quad X0) (k3_cqc_lang X0)) \Rightarrow (\forall X3.(m2_subset_1 X3 (k9_qc_lang1 \\
 & \quad X0) (k3_cqc_lang X0)) \Rightarrow (((v6_qc_lang1 X2 X0) \wedge (r3_cqc_the1 X0 (\\
 & \quad k4_subset_1 (k3_cqc_lang X0) X1 (k6_domain_1 (k3_cqc_lang X0) \\
 & \quad X2)) X3)) \Rightarrow (r3_cqc_the1 X0 X1 (k8_cqc_lang X0 X2 X3))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0.(m1_qc_lang1 X0) \Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 \\
 & \quad X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\
 & \quad X0) (k3_cqc_lang X0)) \Rightarrow (\forall X3.(m1_subset_1 X3 (k1_zfmisc_1 \\
 & \quad (k3_cqc_lang X0))) \Rightarrow ((r3_cqc_the1 X0 X3 (k8_cqc_lang X0 X1 X2)) \Rightarrow \\
 & \quad (r3_cqc_the1 X0 (k4_subset_1 (k3_cqc_lang X0) X3 (k6_domain_1 \\
 & \quad (k3_cqc_lang X0) X1)) X2))))))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m2_subset_1\ X1\ (k9_qc_lang1 \\ X0)\ (k3_cqc_lang\ X0)) \Rightarrow (\forall X2.(m2_subset_1\ X2\ (k9_qc_lang1 \\ X0)\ (k3_cqc_lang\ X0)) \Rightarrow ((r6_cqc_the3\ X0\ X1\ X2) \Rightarrow (r5_cqc_the3\ X0 \\ X1\ X2)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m2_subset_1\ X1\ (k9_qc_lang1 \\ X0)\ (k3_cqc_lang\ X0)) \Rightarrow (\forall X2.(m2_subset_1\ X2\ (k9_qc_lang1 \\ X0)\ (k3_cqc_lang\ X0)) \Rightarrow ((r5_cqc_the3\ X0\ X1\ X2) \Leftrightarrow (r4_cqc_the3\ X0 \\ (k6_domain_1\ (k3_cqc_lang\ X0)\ X1)\ (k6_domain_1\ (k3_cqc_lang\ X0) \\ X2)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m1_subset_1\ X1\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0))) \Rightarrow (\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0))) \Rightarrow (\forall X3.(m1_subset_1\ X3\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0))) \Rightarrow (\forall X4.(m1_subset_1\ X4\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0))) \Rightarrow (((r4_cqc_the3\ X0\ X1\ X2) \wedge (r2_cqc_the3\ X0\ (\\ k4_subset_1\ (k3_cqc_lang\ X0)\ X1\ X3)\ X4)) \Rightarrow (r2_cqc_the3\ X0\ (k4_subset_1 \\ (k3_cqc_lang\ X0)\ X2\ X3)\ X4)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1\ X0) \Rightarrow (\forall X1.(m2_subset_1\ X1\ (k9_qc_lang1 \\ X0)\ (k3_cqc_lang\ X0)) \Rightarrow (\forall X2.(m1_subset_1\ X2\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0))) \Rightarrow ((r2_cqc_the3\ X0\ X2\ (k6_domain_1\ (k3_cqc_lang \\ X0)\ X1)) \Leftrightarrow (r3_cqc_the1\ X0\ X2\ X1)))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.((m1_qc_lang1\ X0) \wedge ((m1_subset_1 \\ X1\ (k1_zfmisc_1\ (k3_cqc_lang\ X0))) \wedge (m1_subset_1\ X2\ (k1_zfmisc_1 \\ (k3_cqc_lang\ X0)))))) \Rightarrow ((r4_cqc_the3\ X0\ X1\ X2) \Rightarrow (r4_cqc_the3\ X0 \\ X2\ X1)) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v1_xboole_0\ X0) \wedge ((\neg v1_xboole_0\ X1) \wedge \\ (m1_subset_1\ X1\ (k1_zfmisc_1\ X0)))) \Rightarrow (\forall X2.(m2_subset_1 \\ X2\ X0\ X1) \Leftrightarrow (m1_subset_1\ X2\ X1)) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.((m1_subset_1\ X1\ (k1_zfmisc_1 \\ X0)) \wedge (m1_subset_1\ X2\ (k1_zfmisc_1\ X0))) \Rightarrow (k4_subset_1\ X0\ X1\ X2 = \\ k2_xboole_0\ X1\ X2) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(m1_qc_lang1 X0) \Rightarrow (\neg v1_xboole_0 (k3_cqc_lang X0)) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0) \wedge (m1_subset_1 X1 X0)) \Rightarrow (m1_subset_1 (k6_domain_1 X0 X1) (k1_zfmisc_1 X0)) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((m1_subset_1 X1 (k1_zfmisc_1 X0)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 X0))) \Rightarrow (m1_subset_1 (k4_subset_1 X0 X1 X2) (k1_zfmisc_1 X0)) \quad (12)$$

Assume the following.

$$\forall X0.(m1_qc_lang1 X0) \Rightarrow (m1_subset_1 (k3_cqc_lang X0) (k1_zfmisc_1 (k9_qc_lang1 X0))) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) \Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow ((r6_cqc_the3 X0 X1 X2) \Leftrightarrow ((v6_qc_lang1 X1 X0) \wedge (\exists X3.(m1_subset_1 X3 k5_numbers) \wedge ((r1_xxreal_0 np_1 X3) \wedge (\exists X4.((v1_relat_1 X4) \wedge ((v1_funct_1 X4) \wedge (v1_finseq_1 X4)))) \wedge ((k3_finseq_1 X4 = X3) \wedge ((k1_funct_1 X4 np_1 = X2) \wedge ((k1_funct_1 X4 X3 = X1) \wedge (\forall X5.(m1_subset_1 X5 k5_numbers) \Rightarrow (\neg (r1_xxreal_0 np_1 X5) \wedge (\neg r1_xxreal_0 X3 X5) \wedge (\forall X6.(m2_subset_1 X6 (k2_qc_lang1 X0) (k3_qc_lang1 X0)) \Rightarrow (\forall X7.(m2_subset_1 X7 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow (\neg (X7 = k1_funct_1 X4 X5) \wedge (k1_funct_1 X4 (k2_nat_1 X5 np_1) = k11_cqc_lang X0 X6 X7))))))))))))))))) \end{aligned} \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.k2_xboole_0 X0 X1 = k2_xboole_0 X1 X0 \quad (15)$$

Assume the following.

$$\forall X0.(v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 X0)) \Rightarrow (v1_xboole_0 X1)) \quad (16)$$

Theorem 1

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) \Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow (\forall X3.(m2_subset_1 X3 (k9_qc_lang1 X0) (k3_cqc_lang X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (k1_zfmisc_1 (k3_cqc_lang X0)) \Rightarrow ((r6_cqc_the3 X0 X1 X2) \Rightarrow ((r3_cqc_the1 X0 (k4_subset_1 (k3_cqc_lang X0) X4 (k6_domain_1 (k3_cqc_lang X0) X2)) X3) \Leftrightarrow (r3_cqc_the1 X0 X4 (k8_cqc_lang X0 X1 X3)))))))))) \end{aligned}$$