

# t42\_modelc.3 (TMEstJekQUTUr- PRCv9vMbuSPAxsFPCqcQJ6)

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Let  $v1\_modelc.2 : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_modelc.3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_modelc.3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_modelc.3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r6\_modelc.3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_modelc.3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_modelc.2 : \iota \Rightarrow o$  be given. Let  $k12\_modelc.2 : \iota \Rightarrow \iota$  be given. Let  $k11\_modelc.2 : \iota \Rightarrow \iota$  be given. Let  $v4\_modelc.2 : \iota \Rightarrow o$  be given. Let  $v5\_modelc.2 : \iota \Rightarrow o$  be given. Let  $v6\_modelc.2 : \iota \Rightarrow o$  be given. Let  $k10\_modelc.2 : \iota \Rightarrow \iota$  be given. Let  $u3\_modelc.3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v8\_modelc.2 : \iota \Rightarrow o$  be given. Let  $k7\_modelc.2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_modelc.2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_modelc.2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_modelc.2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_modelc.2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& \quad \forall X1.((v1\_modelc.2 X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow ( \\
& \quad \quad \forall X2.((v1\_modelc.3 X2 X1) \wedge ((v3\_modelc.3 X2 X1) \wedge (l1\_modelc.3 \\
& \quad \quad X2 X1))) \Rightarrow (\forall X3.((v1\_modelc.3 X3 X1) \wedge ((v3\_modelc.3 X3 X1) \wedge \\
& \quad \quad (l1\_modelc.3 X3 X1))) \Rightarrow (((r6\_modelc.3 X1 X3 X2) \wedge (X0 \in u1\_modelc.3 \\
& \quad \quad X1 X2)) \Rightarrow (((v4\_modelc.2 X0) \Rightarrow ((k11\_modelc.2 X0 \in u1\_modelc.3 X1 \\
& \quad \quad X2) \wedge (k12\_modelc.2 X0 \in u1\_modelc.3 X1 X2))) \wedge (\neg((v5\_modelc.2 \\
& \quad \quad X0) \vee (v7\_modelc.2 X0)) \wedge (\neg k11\_modelc.2 X0 \in u1\_modelc.3 X1 X2) \wedge \\
& \quad \quad (\neg k12\_modelc.2 X0 \in u1\_modelc.3 X1 X2))) \wedge (((v6\_modelc.2 X0) \Rightarrow ( \\
& \quad \quad k10\_modelc.2 X0 \in u3\_modelc.3 X1 X2)) \wedge ((v8\_modelc.2 X0) \Rightarrow (k12\_modelc.2 \\
& \quad \quad X0 \in u1\_modelc.3 X1 X2))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_modelc\_2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& \quad \forall X1.((v1\_modelc\_2 X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow ( \\
& \quad \quad \forall X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \Rightarrow ( \\
& \quad \quad \quad \forall X3.((v1\_modelc\_3 X3 X2) \wedge ((v3\_modelc\_3 X3 X2) \wedge (l1\_modelc\_3 \\
& \quad \quad \quad \quad X3 X2))) \Rightarrow (\forall X4.((v1\_modelc\_3 X4 X2) \wedge ((v3\_modelc\_3 X4 X2) \wedge \\
& \quad \quad \quad \quad (l1\_modelc\_3 X4 X2))) \Rightarrow (\forall X5.((v1\_modelc\_3 X5 X2) \wedge ((v3\_modelc\_3 \\
& \quad \quad \quad \quad X5 X2) \wedge (l1\_modelc\_3 X5 X2))) \Rightarrow (\neg(r6\_modelc\_3 X2 X4 X3) \wedge ((r6\_modelc\_3 \\
& \quad \quad \quad \quad X2 X3 X5) \wedge ((k7\_modelc\_2 X0 X1 \in u1\_modelc\_3 X2 X3) \wedge ((\neg X1 \in u1\_modelc\_3 \\
& \quad \quad \quad \quad X2 X3) \wedge (\neg(X0 \in u1\_modelc\_3 X2 X3) \wedge (k7\_modelc\_2 X0 X1 \in u1\_modelc\_3 \\
& \quad \quad \quad \quad X2 X5))))))))))))) \\
& \tag{2}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_modelc\_2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& \quad (\neg(\neg v4\_modelc\_2 X0) \wedge (\neg v5\_modelc\_2 X0) \wedge (\neg v7\_modelc\_2 X0) \wedge \\
& \quad \quad (\neg v8\_modelc\_2 X0))) \Rightarrow (\forall X1.((v1\_modelc\_2 X1) \wedge (m2\_finseq\_1 \\
& \quad X1 k5\_numbers)) \Rightarrow (((v4\_modelc\_2 X0) \Rightarrow ((X1 = k12\_modelc\_2 X0) \Leftrightarrow ( \\
& \quad \quad \exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge ( \\
& \quad \quad k4\_modelc\_2 X2 X1 = X0)))) \wedge (((v5\_modelc\_2 X0) \Rightarrow ((X1 = k12\_modelc\_2 \\
& \quad \quad X0) \Leftrightarrow (\exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\
& \quad \quad (k5\_modelc\_2 X2 X1 = X0)))) \wedge (((v7\_modelc\_2 X0) \Rightarrow ((X1 = k12\_modelc\_2 \\
& \quad \quad X0) \Leftrightarrow (\exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\
& \quad \quad (k7\_modelc\_2 X2 X1 = X0)))) \wedge (\neg(\neg v4\_modelc\_2 X0) \wedge (\neg v5\_modelc\_2 \\
& \quad \quad X0) \wedge (\neg v7\_modelc\_2 X0) \wedge (\neg(X1 = k12\_modelc\_2 X0) \Leftrightarrow (\exists X2. \\
& \quad \quad ((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge (k8\_modelc\_2 \\
& \quad \quad X2 X1 = X0))))))))))))) \\
& \tag{3}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_modelc\_2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& \quad (\neg(\neg v4\_modelc\_2 X0) \wedge (\neg v5\_modelc\_2 X0) \wedge (\neg v7\_modelc\_2 X0) \wedge \\
& \quad \quad (\neg v8\_modelc\_2 X0))) \Rightarrow (\forall X1.((v1\_modelc\_2 X1) \wedge (m2\_finseq\_1 \\
& \quad X1 k5\_numbers)) \Rightarrow (((v4\_modelc\_2 X0) \Rightarrow ((X1 = k11\_modelc\_2 X0) \Leftrightarrow ( \\
& \quad \quad \exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge ( \\
& \quad \quad k4\_modelc\_2 X1 X2 = X0)))) \wedge (((v5\_modelc\_2 X0) \Rightarrow ((X1 = k11\_modelc\_2 \\
& \quad \quad X0) \Leftrightarrow (\exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\
& \quad \quad (k5\_modelc\_2 X1 X2 = X0)))) \wedge (((v7\_modelc\_2 X0) \Rightarrow ((X1 = k11\_modelc\_2 \\
& \quad \quad X0) \Leftrightarrow (\exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\
& \quad \quad (k7\_modelc\_2 X1 X2 = X0)))) \wedge (\neg(\neg v4\_modelc\_2 X0) \wedge (\neg v5\_modelc\_2 \\
& \quad \quad X0) \wedge (\neg v7\_modelc\_2 X0) \wedge (\neg(X1 = k11\_modelc\_2 X0) \Leftrightarrow (\exists X2. \\
& \quad \quad ((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge (k8\_modelc\_2 \\
& \quad \quad X1 X2 = X0))))))))))))) \\
& \tag{4}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_modelc\_2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& (v7\_modelc\_2 X0) \Leftrightarrow (\exists X1.((v1\_modelc\_2 X1) \wedge (m2\_finseq\_1 \\
& X1 k5\_numbers)) \wedge (\exists X2.((v1\_modelc\_2 X2) \wedge (m2\_finseq\_1 \\
& X2 k5\_numbers))) \wedge (X0 = k7\_modelc\_2 X1 X2)))
\end{aligned} \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((v1\_modelc\_2 X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ( \\
& \forall X1.((v1\_modelc\_2 X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow ( \\
& \forall X2.((v1\_modelc\_3 X2 X1) \wedge ((v3\_modelc\_3 X2 X1) \wedge (l1\_modelc\_3 \\
& X2 X1))) \Rightarrow (\forall X3.((v1\_modelc\_3 X3 X1) \wedge ((v3\_modelc\_3 X3 X1) \wedge \\
& (l1\_modelc\_3 X3 X1))) \Rightarrow (\forall X4.((v1\_modelc\_3 X4 X1) \wedge ((v3\_modelc\_3 \\
& X4 X1) \wedge (l1\_modelc\_3 X4 X1))) \Rightarrow (\neg(r6\_modelc\_3 X1 X3 X2) \wedge ((r6\_modelc\_3 \\
& X1 X2 X4) \wedge ((X0 \in u1\_modelc\_3 X1 X2) \wedge ((v7\_modelc\_2 X0) \wedge ((\neg k12\_modelc\_2 \\
& X0 \in u1\_modelc\_3 X1 X2) \wedge (\neg(k11\_modelc\_2 X0 \in u1\_modelc\_3 X1 X2) \wedge \\
& (X0 \in u1\_modelc\_3 X1 X4))))))))))
\end{aligned}$$