

t42_ordinal5

(TMS2maPBmFEyE89F4NKf8kz3R.JvE4eKQdKN)

October 27, 2020

Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $k3_ordinal5 : \iota \Rightarrow \iota$ be given. Let $k1_ordinal1 : \iota \Rightarrow \iota$ be given. Let $k1_ordinal5 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $v5_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_ordinal2 : \iota \Rightarrow o$ be given. Let $k1_ordinal2 : \iota \Rightarrow \iota$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole_0 : \iota$ be given. Let $v4_ordinal1 : \iota \Rightarrow o$ be given. Let $k5_relat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8_ordinal2 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0 : \iota \Rightarrow \iota. \forall X1 : \iota \Rightarrow \iota \Rightarrow \iota. \forall X2 : \iota \Rightarrow \iota \Rightarrow \\
 & \quad \iota. \forall X3. ((v3_ordinal1 X3) \wedge ((\forall X4. \forall X5. v3_ordinal1 (X1 X4 X5)) \wedge (\forall X4. \\
 & \quad (X2 X4 X5)) \wedge ((\forall X4. \forall X5. v3_ordinal1 (X1 X4 X5)) \wedge (\forall X4. \\
 & \quad v3_ordinal1 (X0 X4)))))) \Rightarrow ((\forall X4. (v3_ordinal1 X4) \Rightarrow (\forall X5. \\
 & \quad (v3_ordinal1 X5) \Rightarrow ((X5 = X0 X4) \Leftrightarrow (\exists X6. ((v5_ordinal1 X6) \wedge \\
 & \quad ((v1_relat_1 X6) \wedge (v1_funct_1 X6) \wedge (v1_ordinal2 X6)))))) \wedge ((X5 = \\
 & \quad k1_ordinal2 X6) \wedge (k9_xtuple_0 X6 = k1_ordinal1 X4) \wedge ((k1_funct_1 \\
 & \quad X6 k1_xboole_0 = X3) \wedge ((\forall X7. (v3_ordinal1 X7) \Rightarrow ((k1_ordinal1 \\
 & \quad X7 \in k1_ordinal1 X4) \Rightarrow (k1_funct_1 X6 (k1_ordinal1 X7) = X2 X7 (k1_funct_1 \\
 & \quad X6 X7)))))) \wedge (\forall X7. (v3_ordinal1 X7) \Rightarrow (((X7 \in k1_ordinal1 X4) \wedge \\
 & \quad (v4_ordinal1 X7) \Rightarrow ((X7 = k1_xboole_0) \vee (k1_funct_1 X6 X7 = X1 X7 \\
 & \quad (k5_relat_1 X6 X7)))))))))) \Rightarrow (\forall X4. (v3_ordinal1 X4) \Rightarrow \\
 & \quad (X0 (k1_ordinal1 X4) = X2 X4 (X0 X4)))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v3_ordinal1\ X0) \Rightarrow (\forall X1.(v3_ordinal1\ X1) \Rightarrow ((\\
& \quad X1 = k3_ordinal5\ X0) \Leftrightarrow (\exists X2.((v1_relat_1\ X2) \wedge ((v1_funct_1 \\
& \quad X2) \wedge ((v5_ordinal1\ X2) \wedge (v1_ordinal2\ X2)))))) \wedge ((X1 = k1_ordinal2 \\
& \quad X2) \wedge ((k9_xtuple_0\ X2 = k1_ordinal1\ X0) \wedge ((k1_funct_1\ X2\ k1_xboole_0 = \\
& \quad k1_ordinal5\ k4_ordinal1\ k4_ordinal1) \wedge ((\forall X3.(v3_ordinal1 \\
& \quad X3) \Rightarrow ((k1_ordinal1\ X3 \in k1_ordinal1\ X0) \Rightarrow (k1_funct_1\ X2\ (k1_ordinal1 \\
& \quad X3) = k1_ordinal5\ (k1_funct_1\ X2\ X3)\ k4_ordinal1)))))) \wedge (\forall X3. \\
& \quad (v3_ordinal1\ X3) \Rightarrow (((X3 \in k1_ordinal1\ X0) \wedge (v4_ordinal1\ X3)) \Rightarrow (\\
& \quad (X3 = k1_xboole_0) \vee (k1_funct_1\ X2\ X3 = k8_ordinal2\ (k5_relat_1 \\
& \quad X2\ X3)))))))))
\end{aligned} \tag{2}$$

Theorem 1

$$\forall X0.(v3_ordinal1\ X0) \Rightarrow (k3_ordinal5\ (k1_ordinal1\ X0) = k1_ordinal5\ (k3_ordinal5\ X0)\ k4_ordinal1)$$