

t42_xboole_1

(TMRrgbJjsUdaYctHrosmxVsJXiDqhbFeCoT)

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Let $k4_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k3_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0. \forall X1. r1_tarski X0 (k2_xboole_0 X0 X1) \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. k2_xboole_0 X0 (k2_xboole_0 X0 X1) &= k2_xboole_0 \\ &\quad X0 X1 \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. k2_xboole_0 (k2_xboole_0 X0 \\ X1) X2 &= k2_xboole_0 X0 (k2_xboole_0 X1 X2) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0. k4_xboole_0 k1_xboole_0 X0 = k1_xboole_0 \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. k4_xboole_0 (k4_xboole_0 X0 \\ X1) X2 &= k4_xboole_0 X0 (k2_xboole_0 X1 X2) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. k4_xboole_0 (k2_xboole_0 X0 X1) X1 &= k4_xboole_0 \\ &\quad X0 X1 \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0. k4_xboole_0 X0 k1_xboole_0 = X0 \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. k2_xboole_0 X0 (k4_xboole_0 X1 X0) &= k2_xboole_0 \\ &\quad X0 X1 \end{aligned} \quad (8)$$

Assume the following.

$$\forall X_0 \forall X_1. (r1_tarski\ X_0\ (k4_xboole_0\ X_1\ X_0)) \Rightarrow (X_0 = k1_xboole_0) \quad (9)$$

Assume the following.

$$\forall X_0 \forall X_1. r1_tarski\ (k4_xboole_0\ X_0\ X_1)\ X_0 \quad (10)$$

Assume the following.

$$\forall X_0 \forall X_1 \forall X_2. r1_tarski\ (k2_xboole_0\ (k3_xboole_0\ X_0\ X_1)\ (k3_xboole_0\ X_0\ X_2))\ (k2_xboole_0\ X_1\ X_2) \quad (11)$$

Assume the following.

$$\forall X_0 \forall X_1 \forall X_2. r1_tarski\ (k3_xboole_0\ X_0\ X_1)\ (k2_xboole_0\ X_0\ X_2) \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X_0 \forall X_1 \forall X_2. k2_xboole_0\ (k2_xboole_0\ (k3_xboole_0\ X_0\ X_1)\ (k3_xboole_0\ X_1\ X_2))\ (k3_xboole_0\ X_2\ X_0) \\ & = k3_xboole_0\ (k3_xboole_0\ (k2_xboole_0\ X_0\ X_1)\ (k2_xboole_0\ X_1\ X_2))\ (k2_xboole_0\ X_2\ X_0) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X_0 \forall X_1 \forall X_2. k2_xboole_0\ X_0\ (k3_xboole_0\ X_1\ X_2) \\ & = k3_xboole_0\ (k2_xboole_0\ X_0\ X_1)\ (k2_xboole_0\ X_0\ X_2) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X_0 \forall X_1 \forall X_2. k3_xboole_0\ X_0\ (k2_xboole_0\ X_1\ X_2) \\ & = k2_xboole_0\ (k3_xboole_0\ X_0\ X_1)\ (k3_xboole_0\ X_0\ X_2) \end{aligned} \quad (15)$$

Assume the following.

$$\forall X_0 \forall X_1. k2_xboole_0\ X_0\ (k3_xboole_0\ X_0\ X_1) = X_0 \quad (16)$$

Assume the following.

$$\forall X_0 \forall X_1. (r1_tarski\ X_0\ X_1) \Rightarrow (k2_xboole_0\ X_0\ X_1 = X_1) \quad (17)$$

Assume the following.

$$\begin{aligned} & \forall X_0 \forall X_1 \forall X_2. (r1_tarski\ X_0\ X_1) \Rightarrow (r1_tarski\ X_0\ (k2_xboole_0\ X_2\ X_1)) \\ & \quad (18) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X_0 \forall X_1 \forall X_2. k4_xboole_0\ X_0\ (k3_xboole_0\ X_1\ X_2) \\ & = k2_xboole_0\ (k4_xboole_0\ X_0\ X_1)\ (k4_xboole_0\ X_0\ X_2) \end{aligned} \quad (19)$$

Assume the following.

$$\forall X_0 \forall X_1. (k4_xboole_0 X_0 X_1 = k1_xboole_0) \Leftrightarrow (r1_tarski X_0 X_1) \quad (20)$$

Assume the following.

$$\forall X_0 \forall X_1. k2_xboole_0 X_0 X_0 = X_0 \quad (21)$$

Assume the following.

$$\begin{aligned} \forall X_0 \forall X_1 \forall X_2. (X_2 = k4_xboole_0 X_0 X_1) &\Leftrightarrow (\forall X_3. \\ (X_3 \in X_2) &\Leftrightarrow ((X_3 \in X_0) \wedge (\neg X_3 \in X_1))) \end{aligned} \quad (22)$$

Assume the following.

$$\forall X_0 \forall X_1. (X_0 = X_1) \Leftrightarrow ((r1_tarski X_0 X_1) \wedge (r1_tarski X_1 X_0)) \quad (23)$$

Assume the following.

$$\forall X_0 \forall X_1. k2_xboole_0 X_0 X_1 = k2_xboole_0 X_1 X_0 \quad (24)$$

Theorem 1

$$\begin{aligned} \forall X_0 \forall X_1 \forall X_2. k4_xboole_0 (k2_xboole_0 X_0 X_1) \\ X_2 = k2_xboole_0 (k4_xboole_0 X_0 X_2) (k4_xboole_0 X_1 X_2) \end{aligned}$$