

t43_bvfunc11

(TMah9AnJCyDmouksCfx8yQoupaWq22gSgp9)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_margrel1 : \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_bvfunc_2 : \iota \Rightarrow \iota$ be given. Let $m1_eqrel_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_bvfunc_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_bvfunc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k7_bvfunc_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_partit1 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. ((v1_funct_1 X1) \wedge \\
 & (v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (\\
 & k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X2. ((v1_funct_1 X2) \wedge \\
 & ((v1_funct_2 X2 X0 k6_margrel1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\
 & (k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X3. ((v1_funct_1 X3) \wedge \\
 & ((v1_funct_2 X3 X0 k6_margrel1) \wedge (m1_subset_1 X3 (k1_zfmisc_1 \\
 & (k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (((r1_bvfunc_1 X0 X1 X2) \wedge \\
 & r1_bvfunc_1 X0 X2 X1) \Rightarrow (r2_funct_2 X0 k6_margrel1 X1 X2)) \wedge (((r1_bvfunc_1 \\
 & X0 X1 X2) \wedge (r1_bvfunc_1 X0 X2 X3)) \Rightarrow (r1_bvfunc_1 X0 X1 X3)))))) \\
 & \tag{1}
 \end{aligned}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. ((v1_funct_1 X1) \wedge \\
 & (v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (\\
 & k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X2. ((v1_funct_1 X2) \wedge \\
 & ((v1_funct_2 X2 X0 k6_margrel1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\
 & (k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X3. (m1_subset_1 X3 \\
 & (k1_zfmisc_1 (k1_bvfunc_2 X0))) \Rightarrow (\forall X4. (m1_eqrel_1 X4 X0) \Rightarrow \\
 & ((r1_bvfunc_1 X0 X1 X2) \Rightarrow (r1_bvfunc_1 X0 (k7_bvfunc_2 X0 X1 X3 X4) \\
 & (k7_bvfunc_2 X0 X2 X3 X4)))))) \\
 & \tag{2}
 \end{aligned}$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 \\ (k1_partit1 X0))) \Rightarrow (\forall X2.((v1_funct_1 X2) \wedge ((v1_funct_2 \\ X2 X0 k6_margrel1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 \\ X0 k6_margrel1)))) \Rightarrow (\forall X3.(m1_eqrel_1 X3 X0) \Rightarrow (r1_bvfunc_1 \\ X0 X2 (k7_bvfunc_2 X0 X2 X1 X3)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge (\\ (v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (\\ k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X2.((v1_funct_1 X2) \wedge \\ ((v1_funct_2 X2 X0 k6_margrel1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ (k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow ((r1_bvfunc_1 X0 X1 X2) \Rightarrow (r1_bvfunc_1 \\ X0 (k1_bvfunc_1 X0 X2) (k1_bvfunc_1 X0 X1)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.k1_bvfunc_2 X0 = k1_partit1 X0 \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1_xboole_0 X0) \wedge \\ (((v1_funct_1 X1) \wedge ((v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 \\ X1 (k1_zfmisc_1 (k2_zfmisc_1 X0 k6_margrel1)))) \wedge ((m1_subset_1 \\ X2 (k1_zfmisc_1 (k1_bvfunc_2 X0))) \wedge (m1_eqrel_1 X3 X0))) \Rightarrow ((v1_funct_1 \\ (k7_bvfunc_2 X0 X1 X2 X3) \wedge ((v1_funct_2 (k7_bvfunc_2 X0 X1 X2 X3) \\ X0 k6_margrel1) \wedge (m1_subset_1 (k7_bvfunc_2 X0 X1 X2 X3) (k1_zfmisc_1 \\ (k2_zfmisc_1 X0 k6_margrel1)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v1_xboole_0 X0) \wedge ((v1_funct_1 X1) \wedge (\\ (v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (\\ k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow ((v1_funct_1 (k1_bvfunc_1 \\ X0 X1)) \wedge ((v1_funct_2 (k1_bvfunc_1 X0 X1) X0 k6_margrel1) \wedge (m1_subset_1 \\ (k1_bvfunc_1 X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 X0 k6_margrel1)))))) \end{aligned} \quad (7)$$

Theorem 1

$$\begin{aligned} \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge (\\ (v1_funct_2 X1 X0 k6_margrel1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (\\ k2_zfmisc_1 X0 k6_margrel1)))) \Rightarrow (\forall X2.(m1_subset_1 X2 \\ (k1_zfmisc_1 (k1_bvfunc_2 X0))) \Rightarrow (\forall X3.(m1_eqrel_1 X3 X0) \Rightarrow \\ (\forall X4.(m1_eqrel_1 X4 X0) \Rightarrow (r1_bvfunc_1 X0 (k1_bvfunc_1 X0 \\ (k7_bvfunc_2 X0 (k7_bvfunc_2 X0 X1 X2 X3) X2 X4) (k7_bvfunc_2 X0 \\ (k1_bvfunc_1 X0 (k7_bvfunc_2 X0 X1 X2 X4) X2 X3)))))) \end{aligned}$$