

t45_monoid_0 (TMXVnt-
tNiZ3TMhS1zEBcCxZTpjjfLKAaXMT)

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Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $k5_numbers : \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $k5_monoid_0 : \iota$ be given. Let $k6_algstr_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k23_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $m2_monoid_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_monoid_0 : \iota$ be given. Let $k9_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $l3_algstr_0 : \iota \Rightarrow o$ be given. Let $m1_monoid_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u2_algstr_0 : \iota \Rightarrow \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $v1_xreal_0 : \iota \Rightarrow o$ be given. Let $k2_xcmplx_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v3_membered : \iota \Rightarrow o$ be given. Let $m5_monoid_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v22_algstr_0 : \iota \Rightarrow o$ be given. Let $v4_vectsp_1 : \iota \Rightarrow o$ be given. Let $k4_monoid_0 : \iota$ be given. Let $v15_algstr_0 : \iota \Rightarrow o$ be given. Let $v1_group_1 : \iota \Rightarrow o$ be given. Let $v17_monoid_0 : \iota \Rightarrow o$ be given. Let $k3_monoid_0 : \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0. ((\neg v2_struct_0 X0) \wedge (m2_monoid_0 X0 k2_monoid_0)) \Rightarrow \\
 & (\forall X1. (m1_subset_1 X1 (u1_struct_0 X0)) \Rightarrow (\forall X2. (m1_subset_1 \\
 & X2 (u1_struct_0 X0)) \Rightarrow (\forall X3. (m1_subset_1 X3 k1_numbers) \Rightarrow \\
 & (\forall X4. (m1_subset_1 X4 k1_numbers) \Rightarrow (((X1 = X3) \wedge (X2 = X4)) \Rightarrow \\
 & (k6_algstr_0 X0 X1 X2 = k9_binop_2 X3 X4)))))) \Rightarrow \quad (1)
 \end{aligned}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. ((\neg v2_struct_0 X0) \wedge (l3_algstr_0 X0)) \Rightarrow (\forall X1. \\
 & (m1_monoid_0 X1 X0) \Rightarrow ((u1_struct_0 X1 = u1_struct_0 X0) \wedge ((r1_funct_2 \\
 & (k2_zfmisc_1 (u1_struct_0 X1) (u1_struct_0 X1)) (u1_struct_0 \\
 & X1) (k2_zfmisc_1 (u1_struct_0 X0) (u1_struct_0 X0)) (u1_struct_0 \\
 & X0) (u2_algstr_0 X1) (u2_algstr_0 X0)) \wedge (\forall X2. (m1_subset_1 \\
 & X2 (u1_struct_0 X1)) \Rightarrow (\forall X3. (m1_subset_1 X3 (u1_struct_0 \\
 & X1)) \Rightarrow (\forall X4. (m1_subset_1 X4 (u1_struct_0 X0)) \Rightarrow (\forall X5. \\
 & (m1_subset_1 X5 (u1_struct_0 X0)) \Rightarrow (((X2 = X4) \wedge (X3 = X5)) \Rightarrow (k6_algstr_0 \\
 & X1 X2 X3 = k6_algstr_0 X0 X4 X5)))))))))) \Rightarrow \quad (2)
 \end{aligned}$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X1 (k1_zfmisc_1 X0))))\Rightarrow(\forall X2.(m2_subset_1 X2 X0 X1)\Leftrightarrow(m1_subset_1 X2 X1)) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.((v1_xreal_0 X0)\wedge(v1_xreal_0 X1))\Rightarrow(k9_binop_2 X0 X1 = k2_xcmplx_0 X0 X1) \quad (4)$$

Assume the following.

$$k5_numbers = k4_ordinal1 \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((v7_ordinal1 X0)\wedge(v7_ordinal1 X1))\Rightarrow(k23_binop_2 X0 X1 = k2_xcmplx_0 X0 X1) \quad (6)$$

Assume the following.

$$(\neg v1_xboole_0 k4_ordinal1)\wedge(v3_ordinal1 k4_ordinal1) \quad (7)$$

Assume the following.

$$v3_membered k1_numbers \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.((l3_algstr_0 X0)\wedge(m2_monoid_0 X1 X0))\Rightarrow(\forall X2.(m5_monoid_0 X2 X0 X1)\Rightarrow(m2_monoid_0 X2 X0)) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((\neg v1_xboole_0 X1)\wedge(m1_subset_1 X1 (k1_zfmisc_1 X0))))\Rightarrow(\forall X2.(m2_subset_1 X2 X0 X1)\Rightarrow(m1_subset_1 X2 X0)) \quad (10)$$

Assume the following.

$$\forall X0.(l3_algstr_0 X0)\Rightarrow(\forall X1.(m2_monoid_0 X1 X0)\Rightarrow(l3_algstr_0 X1)) \quad (11)$$

Assume the following.

$$m1_subset_1 k5_numbers (k1_zfmisc_1 k1_numbers) \quad (12)$$

Assume the following.

$$(\neg v2_struct_0 k5_monoid_0)\wedge((v22_algstr_0 k5_monoid_0)\wedge((v4_vectsp_1 k5_monoid_0)\wedge(m1_monoid_0 k5_monoid_0 k4_monoid_0))) \quad (13)$$

Assume the following.

$$(\neg v2_struct_0 k4_monoid_0) \wedge ((v15_algstr_0 k4_monoid_0) \wedge ((v1_group_1 k4_monoid_0) \wedge ((v17_monoid_0 k4_monoid_0) \wedge (m5_monoid_0 k4_monoid_0 k2_monoid_0 k3_monoid_0)))))) \quad (14)$$

Assume the following.

$$(\neg v2_struct_0 k3_monoid_0) \wedge ((v15_algstr_0 k3_monoid_0) \wedge (m2_monoid_0 k3_monoid_0 k2_monoid_0)) \quad (15)$$

Assume the following.

$$(\neg v2_struct_0 k2_monoid_0) \wedge (l3_algstr_0 k2_monoid_0) \quad (16)$$

Assume the following.

$$\forall X0. (m1_subset_1 X0 k4_ordinal1) \Rightarrow (v7_ordinal1 X0) \quad (17)$$

Assume the following.

$$\forall X0. (v1_xboole_0 X0) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_zfmisc1 X0)) \Rightarrow (v1_xboole_0 X1)) \quad (18)$$

Assume the following.

$$\forall X0. (v3_membered X0) \Rightarrow (\forall X1. (m1_subset_1 X1 X0) \Rightarrow (v1_xreal_0 X1)) \quad (19)$$

Theorem 1

$$\forall X0. (m2_subset_1 X0 k1_numbers k5_numbers) \Rightarrow (\forall X1. (m2_subset_1 X1 k1_numbers k5_numbers) \Rightarrow (\forall X2. (m1_subset_1 X2 (u1_struct_0 k5_monoid_0)) \Rightarrow (\forall X3. (m1_subset_1 X3 (u1_struct_0 k5_monoid_0)) \Rightarrow (((X0 = X2) \wedge (X1 = X3)) \Rightarrow (k6_algstr_0 k5_monoid_0 X2 X3 = k23_binop_2 X0 X1))))))$$