

# t45\_prob\_3 (TM- PCP6ENmQVvGbcByDJR7RBMSMhzqJJthsN)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_prob\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_prob\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k9\_setfam\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_prob\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_prob\_2 : \iota \Rightarrow o$  be given. Let  $v2\_comseq\_2 : \iota \Rightarrow o$  be given. Let  $k3\_series\_1 : \iota \Rightarrow \iota$  be given. Let  $k8\_prob\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_seq\_2 : \iota \Rightarrow \iota$  be given. Let  $k1\_rinfsup1 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_kurato\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k2\_prob\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge \\
 & ((v1\_prob\_1 X1 X0) \wedge ((v4\_prob\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
 & (k1\_zfmisc\_1 X0)))))) \Rightarrow (\forall X2. ((v5\_relat\_1 X2 X1) \wedge ((v1\_funct\_1 \\
 & X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (k9\_setfam\_1 X0)) \wedge (m1\_subset\_1 \\
 & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k9\_setfam\_1 X0)))))) \Rightarrow \\
 & (\forall X3. (m2\_prob\_1 X3 X0 X1) \Rightarrow ((v1\_prob\_2 X2) \Rightarrow (r2\_funct\_2 \\
 & k5\_numbers k1\_numbers (k8\_prob\_1 X0 X1 (k2\_prob\_3 X0 X2) X3) (k3\_series\_1 \\
 & (k8\_prob\_1 X0 X1 X2 X3))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge \\
 & ((v1\_prob\_1 X1 X0) \wedge ((v4\_prob\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
 & (k1\_zfmisc\_1 X0)))))) \Rightarrow (\forall X2. ((v5\_relat\_1 X2 X1) \wedge ((v1\_funct\_1 \\
 & X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (k9\_setfam\_1 X0)) \wedge (m1\_subset\_1 \\
 & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k9\_setfam\_1 X0)))))) \Rightarrow \\
 & (\forall X3. (m2\_prob\_1 X3 X0 X1) \Rightarrow ((v2\_comseq\_2 (k8\_prob\_1 X0 X1 \\
 & (k2\_prob\_3 X0 X2) X3) \wedge ((k2\_seq\_2 (k8\_prob\_1 X0 X1 (k2\_prob\_3 X0 \\
 & X2) X3) = k1\_rinfsup1 (k8\_prob\_1 X0 X1 (k2\_prob\_3 X0 X2) X3)) \wedge (k2\_seq\_2 \\
 & (k8\_prob\_1 X0 X1 (k2\_prob\_3 X0 X2) X3) = k1\_funct\_1 X3 (k1\_kurato\_0 \\
 & X0 X2))))))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v1\_funct\_1 X2)\wedge \\ & ((v1\_funct\_2 X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 X3 X0 X1)\wedge(m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))))))\Rightarrow((r2\_funct\_2 X0 X1 X2 \\ & X3)\Leftrightarrow(X2 = X3)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.k9\_setfam\_1 X0 = k1\_zfmisc\_1 X0 \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v1\_xboole\_0 X1)\wedge((v1\_prob\_1 \\ & X1 X0)\wedge((v4\_prob\_1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k1\_zfmisc\_1 \\ & X0))))))\wedge((v5\_relat\_1 X2 X1)\wedge((v1\_funct\_1 X2)\wedge((v1\_funct\_2 \\ & X2 k5\_numbers (k9\_setfam\_1 X0))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 k5\_numbers (k9\_setfam\_1 X0)))))))\Rightarrow((v5\_relat\_1 \\ & (k2\_prob\_3 X0 X2) X1)\wedge((v1\_funct\_1 (k2\_prob\_3 X0 X2))\wedge(v1\_funct\_2 \\ & (k2\_prob\_3 X0 X2) k5\_numbers (k9\_setfam\_1 X0)))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge \\ & ((v1\_prob\_1 X1 X0)\wedge((v4\_prob\_1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k1\_zfmisc\_1 X0))))))\Rightarrow(\forall X2.(m2\_prob\_1 X2 X0 X1)\Rightarrow((v1\_funct\_1 \\ & X2)\wedge((v1\_funct\_2 X2 X1 k1\_numbers)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X1 k1\_numbers)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v1\_xboole\_0 \\ & X1)\wedge((v1\_prob\_1 X1 X0)\wedge((v4\_prob\_1 X1 X0)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k1\_zfmisc\_1 X0))))))\wedge(((v5\_relat\_1 X2 X1)\wedge((v1\_funct\_1 X2)\wedge \\ & ((v1\_funct\_2 X2 k5\_numbers (k9\_setfam\_1 X0))\wedge(m1\_subset\_1 X2 \\ & (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k9\_setfam\_1 X0))))))\wedge \\ & ((v1\_funct\_1 X3)\wedge((v1\_funct\_2 X3 X1 k1\_numbers)\wedge(m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 k1\_numbers))))))\Rightarrow((v1\_funct\_1 \\ & (k8\_prob\_1 X0 X1 X2 X3))\wedge((v1\_funct\_2 (k8\_prob\_1 X0 X1 X2 X3) k5\_numbers \\ & k1\_numbers)\wedge(m1\_subset\_1 (k8\_prob\_1 X0 X1 X2 X3) (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v1\_funct\_1 (k3\_series\_1 X0)) \wedge ((v1\_funct\_2 (k3\_series\_1 X0) \\ & k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 (k3\_series\_1 X0) (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers \\ & (k9\_setfam\_1 X0)) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & k5\_numbers (k9\_setfam\_1 X0)))))) \Rightarrow ((v1\_funct\_1 (k2\_prob\_3 X0 \\ & X1)) \wedge ((v1\_funct\_2 (k2\_prob\_3 X0 X1) k5\_numbers (k9\_setfam\_1 X0)) \wedge \\ & (m1\_subset\_1 (k2\_prob\_3 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\ & (k9\_setfam\_1 X0)))))) \end{aligned} \quad (9)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge \\ & ((v1\_prob\_1 X1 X0) \wedge ((v4\_prob\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & (k1\_zfmisc\_1 X0)))))) \Rightarrow (\forall X2. ((v5\_relat\_1 X2 X1) \wedge ((v1\_funct\_1 \\ & X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (k9\_setfam\_1 X0)) \wedge (m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k9\_setfam\_1 X0)))))) \Rightarrow \\ & (\forall X3. (m2\_prob\_1 X3 X0 X1) \Rightarrow ((v1\_prob\_2 X2) \Rightarrow ((v2\_comseq\_2 \\ & (k3\_series\_1 (k8\_prob\_1 X0 X1 X2 X3)) \wedge ((k2\_seq\_2 (k3\_series\_1 \\ & (k8\_prob\_1 X0 X1 X2 X3)) = k1\_rinfsup1 (k3\_series\_1 (k8\_prob\_1 X0 \\ & X1 X2 X3)) \wedge (k2\_seq\_2 (k3\_series\_1 (k8\_prob\_1 X0 X1 X2 X3)) = k1\_funct\_1 \\ & X3 (k1\_kurato\_0 X0 X2)))))))))) \end{aligned}$$