

t45\_qc\_lang2  
 (TMM6KqKKQAMWiY1L48uM37VZxmSJ3YdoyD6)

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Let  $m1\_qc\_lang1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $r1\_qc\_lang2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k14\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k11\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $v2\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $k8\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $np\_2 : \iota$  be given. Let  $v5\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $np\_3 : \iota$  be given. Let  $k13\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $k3\_qc\_lang1 : \iota \Rightarrow \iota$  be given. Let  $k15\_qc\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1 X0) \Rightarrow & (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k9\_qc\_lang1 X0)) \Rightarrow (\forall X3. \\ (m1\_subset\_1 X3 (k9\_qc\_lang1 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\ (k9\_qc\_lang1 X0)) \Rightarrow ((k14\_qc\_lang1 X0 X1 X2 = k14\_qc\_lang1 X0 X3 X4) \Rightarrow \\ ((X1 = X3) \wedge (X2 = X4))))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_qc\_lang1 X0) \Rightarrow & (\forall X1.(m1\_subset\_1 X1 (k9\_qc\_lang1 \\ X0)) \Rightarrow ((k1\_xtuple\_0 (k1\_funct\_1 (k11\_qc\_lang1 X0 (k12\_qc\_lang1 \\ X0)) np\_1) = k6\_numbers) \wedge ((\neg(v2\_qc\_lang1 X1 X0) \wedge (\forall X2. \\ (m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\neg m2\_subset\_1 (k1\_funct\_1 (k11\_qc\_lang1 \\ X0 X1) np\_1) (k6\_qc\_lang1 X0) (k8\_qc\_lang1 X0 X2)))) \wedge (((v3\_qc\_lang1 \\ X1 X0) \Rightarrow (k1\_xtuple\_0 (k1\_funct\_1 (k11\_qc\_lang1 X0 X1) np\_1) = np\_1) \wedge \\ ((v4\_qc\_lang1 X1 X0) \Rightarrow (k1\_xtuple\_0 (k1\_funct\_1 (k11\_qc\_lang1 X0 X1) np\_1) = np\_2) \wedge ((v5\_qc\_lang1 X1 X0) \Rightarrow (k1\_xtuple\_0 (k1\_funct\_1 \\ (k11\_qc\_lang1 X0 X1) np\_1) = np\_3))))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X_0. \forall X_1. \forall X_2. ((m1\_qc\_lang1 X_0) \wedge ((m1\_subset\_1 \\ & X_1 (k9\_qc\_lang1 X_0)) \wedge (m1\_subset\_1 X_2 (k9\_qc\_lang1 X_0)))) \Rightarrow (m1\_subset\_1 \\ & (k14\_qc\_lang1 X_0 X_1 X_2) (k9\_qc\_lang1 X_0)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X_0. \forall X_1. ((m1\_qc\_lang1 X_0) \wedge (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0))) \Rightarrow (m1\_subset\_1 (k13\_qc\_lang1 X_0 X_1) (k9\_qc\_lang1 X_0)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow ((v5\_qc\_lang1 X_1 X_0) \Leftrightarrow (\exists X_2. (m2\_subset\_1 X_2 (k2\_qc\_lang1 \\ & X_0) (k3\_qc\_lang1 X_0)) \wedge (\exists X_3. (m1\_subset\_1 X_3 (k9\_qc\_lang1 \\ & X_0)) \wedge (X_1 = k15\_qc\_lang1 X_0 X_2 X_3))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow ((v4\_qc\_lang1 X_1 X_0) \Leftrightarrow (\exists X_2. (m1\_subset\_1 X_2 (k9\_qc\_lang1 \\ & X_0)) \wedge (\exists X_3. (m1\_subset\_1 X_3 (k9\_qc\_lang1 X_0)) \wedge (X_1 = k14\_qc\_lang1 \\ & X_0 X_2 X_3))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow (\forall X_2. (m1\_subset\_1 X_2 (k9\_qc\_lang1 X_0)) \Rightarrow ((r1\_qc\_lang2 \\ & X_0 X_1 X_2) \Leftrightarrow (\neg(X_2 \neq k13\_qc\_lang1 X_0 X_1) \wedge ((\forall X_3. (m1\_subset\_1 \\ & X_3 (k9\_qc\_lang1 X_0)) \Rightarrow ((X_2 \neq k14\_qc\_lang1 X_0 X_1 X_3) \wedge (X_2 \neq k14\_qc\_lang1 \\ & X_0 X_3 X_1)) \wedge (\forall X_3. (m2\_subset\_1 X_3 (k2\_qc\_lang1 X_0) (k3\_qc\_lang1 \\ & X_0) \Rightarrow (X_2 \neq k15\_qc\_lang1 X_0 X_3 X_1))))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow ((v3\_qc\_lang1 X_1 X_0) \Leftrightarrow (\exists X_2. (m1\_subset\_1 X_2 (k9\_qc\_lang1 \\ & X_0)) \wedge (X_1 = k13\_qc\_lang1 X_0 X_2)))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow (k11\_qc\_lang1 X_0 X_1 = X_1)) \end{aligned} \quad (9)$$

### Theorem 1

$$\begin{aligned} & \forall X_0. (m1\_qc\_lang1 X_0) \Rightarrow (\forall X_1. (m1\_subset\_1 X_1 (k9\_qc\_lang1 \\ & X_0)) \Rightarrow (\forall X_2. (m1\_subset\_1 X_2 (k9\_qc\_lang1 X_0)) \Rightarrow (\forall X_3. \\ & (m1\_subset\_1 X_3 (k9\_qc\_lang1 X_0)) \Rightarrow ((r1\_qc\_lang2 X_0 X_1 (k14\_qc\_lang1 \\ & X_0 X_2 X_3) \Leftrightarrow ((X_1 = X_2) \vee (X_1 = X_3))))))) \end{aligned}$$