

t48_cqc_the3

(TMN43AgXmwf65jxyjvJSNp7JWoW8f7wkDi6)

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Let $m1_qc_lang1 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k9_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k3_cqc_lang : \iota \Rightarrow \iota$ be given. Let $r6_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_cqc_lang : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v6_qc_lang1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r5_cqc_the3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_numbers : \iota$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $np_1 : \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_finseq_1 : \iota \Rightarrow o$ be given. Let $k3_finseq_1 : \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k3_qc_lang1 : \iota \Rightarrow \iota$ be given. Let $k2_nat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_cqc_lang : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) &\Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (\forall X3.(m2_subset_1 X3 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (((r1_cqc_the3 X0 X1 X2) \wedge (r1_cqc_the3 X0 \\ X2 X3)) \Rightarrow (r1_cqc_the3 X0 X1 X3)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) &\Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (((v6_qc_lang1 X1 X0) \wedge (r1_cqc_the3 X0 (\\ k6_cqc_lang X0 X1) (k6_cqc_lang X0 X2))) \Rightarrow (r1_cqc_the3 X0 X2 X1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) &\Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (((v6_qc_lang1 X1 X0) \wedge (r1_cqc_the3 X0 X1 \\ X2)) \Rightarrow (r1_cqc_the3 X0 (k6_cqc_lang X0 X2) (k6_cqc_lang X0 X1)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1_qc_lang1 X0) &\Rightarrow (\forall X1.(m2_subset_1 X1 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow (\forall X2.(m2_subset_1 X2 (k9_qc_lang1 \\ X0) (k3_cqc_lang X0)) \Rightarrow ((r6_cqc_the3 X0 X1 X2) \Rightarrow (r5_cqc_the3 X0 \\ X1 X2)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned}
& \forall X_0. (m1_qc_lang1 X_0) \Rightarrow (\forall X_1. (m2_subset_1 X_1 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (\forall X_2. (m2_subset_1 X_2 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow ((r6_cqc_the3 X_0 X_1 X_2) \Leftrightarrow ((v6_qc_lang1 X_1 \\
& X_0) \wedge (\exists X_3. (m1_subset_1 X_3 k5_numbers) \wedge ((r1_xxreal_0 np_1 \\
& X_3) \wedge (\exists X_4. ((v1_relat_1 X_4) \wedge ((v1_funct_1 X_4) \wedge (v1_finseq_1 \\
& X_4))) \wedge ((k3_finseq_1 X_4 = X_3) \wedge ((k1_funct_1 X_4 np_1 = X_2) \wedge ((k1_funct_1 \\
& X_4 X_3 = X_1) \wedge (\forall X_5. (m1_subset_1 X_5 k5_numbers) \Rightarrow (\neg(r1_xxreal_0 \\
& np_1 X_5) \wedge ((\neg r1_xxreal_0 X_3 X_5) \wedge (\forall X_6. (m2_subset_1 X_6 \\
& k2_qc_lang1 X_0) (k3_qc_lang1 X_0)) \Rightarrow (\forall X_7. (m2_subset_1 X_7 \\
& (k9_qc_lang1 X_0) (k3_cqc_lang X_0)) \Rightarrow (\neg(X_7 = k1_funct_1 X_4 X_5) \wedge \\
& k1_funct_1 X_4 (k2_nat_1 X_5 np_1) = k11_cqc_lang X_0 X_6 X_7))))))))))) \\
& (5)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X_0. (m1_qc_lang1 X_0) \Rightarrow (\forall X_1. (m2_subset_1 X_1 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (\forall X_2. (m2_subset_1 X_2 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow ((r5_cqc_the3 X_0 X_1 X_2) \Leftrightarrow ((r1_cqc_the3 X_0 \\
& X_1 X_2) \wedge (r1_cqc_the3 X_0 X_2 X_1)))) \\
& (6)
\end{aligned}$$

Theorem 1

$$\begin{aligned}
& \forall X_0. (m1_qc_lang1 X_0) \Rightarrow (\forall X_1. (m2_subset_1 X_1 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (\forall X_2. (m2_subset_1 X_2 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (\forall X_3. (m2_subset_1 X_3 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (\forall X_4. (m2_subset_1 X_4 (k9_qc_lang1 \\
& X_0) (k3_cqc_lang X_0)) \Rightarrow (((r6_cqc_the3 X_0 X_1 X_2) \wedge (r6_cqc_the3 X_0 \\
& X_3 X_4)) \Rightarrow ((r1_cqc_the3 X_0 X_2 X_4) \Leftrightarrow (r1_cqc_the3 X_0 (k6_cqc_lang X_0 \\
& X_3) (k6_cqc_lang X_0 X_1)))))))
\end{aligned}$$