

t48_topgen_5
(TMaBbKoK3A99hkytM8d1CqsD1qpeKcVCdj8)

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Let $v2_pre_topc : \iota \Rightarrow o$ be given. Let $v7_pre_topc : \iota \Rightarrow o$ be given. Let $l1_pre_topc : \iota \Rightarrow o$ be given. Let $v1_topgen_5 : \iota \Rightarrow o$ be given. Let $v1_tops_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v2_cantor_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_topmetr : \iota$ be given. Let $v5_pre_topc : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_numbers : \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_numbers : \iota$ be given. Let $np_1 : \iota$ be given. Let $v3_pre_topc : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_pre_topc : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1_subset_1 X1 (k1_zfmisc_1 X2))) \Rightarrow (m1_subset_1 X0 X2) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (m1_subset_1 X1 (k1_zfmisc_1 X0)) \Rightarrow (k3_subset_1 X0 (k3_subset_1 X0 X1) = X1) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. (((v2_pre_topc X0) \wedge (l1_pre_topc X0)) \wedge ((v3_pre_topc X1 X0) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (u1_struct_0 X0)))))) \Rightarrow (v4_pre_topc (k3_subset_1 (u1_struct_0 X0) X1) X0) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. (m1_subset_1 X1 (k1_zfmisc_1 X0)) \Rightarrow (m1_subset_1 (k3_subset_1 X0 X1) (k1_zfmisc_1 X0)) \quad (4)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v2_pre_topc\ X0) \wedge (l1_pre_topc\ X0)) \Rightarrow ((v1_topgen_5 \\
& X0) \Leftrightarrow (\forall X1.((v4_pre_topc\ X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1 \\
& (u1_struct_0\ X0)))) \Rightarrow (\forall X2.(m1_subset_1\ X2\ (u1_struct_0 \\
& X0)) \Rightarrow (\neg(X2 \in k3_subset_1\ (u1_struct_0\ X0)\ X1) \wedge (\forall X3.((v1_funct_1 \\
& X3) \wedge ((v1_funct_2\ X3\ (u1_struct_0\ X0)\ (u1_struct_0\ k5_topmetr)) \wedge \\
& ((v5_pre_topc\ X3\ X0\ k5_topmetr) \wedge (m1_subset_1\ X3\ (k1_zfmisc_1 \\
& (k2_zfmisc_1\ (u1_struct_0\ X0)\ (u1_struct_0\ k5_topmetr)))))) \Rightarrow \\
& (\neg(k1_funct_1\ X3\ X2 = k6_numbers) \wedge (r1_tarSKI\ (k7_relset_1\ (u1_struct_0 \\
& X0)\ (u1_struct_0\ k5_topmetr)\ X3\ X1)\ (k6_domain_1\ k1_numbers\ np_1))))))))) \Rightarrow \\
& \hspace{15em} (5)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(l1_pre_topc\ X0) \Rightarrow (\forall X1.(m1_subset_1\ X1\ (k1_zfmisc_1 \\
& (k1_zfmisc_1\ (u1_struct_0\ X0)))) \Rightarrow ((v1_tops_2\ X1\ X0) \Leftrightarrow (\forall X2. \\
& (m1_subset_1\ X2\ (k1_zfmisc_1\ (u1_struct_0\ X0))) \Rightarrow ((X2 \in X1) \Rightarrow (v3_pre_topc \\
& X2\ X0)))))) \Rightarrow \\
& \hspace{15em} (6)
\end{aligned}$$

Theorem 1

$$\begin{aligned}
& \forall X0.((v2_pre_topc\ X0) \wedge ((v7_pre_topc\ X0) \wedge (l1_pre_topc \\
& X0))) \Rightarrow ((v1_topgen_5\ X0) \Rightarrow (\forall X1.((v1_tops_2\ X1\ X0) \wedge ((v2_cantor_1 \\
& X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k1_zfmisc_1\ (u1_struct_0 \\
& X0)))))) \Rightarrow (\forall X2.(m1_subset_1\ X2\ (u1_struct_0\ X0)) \Rightarrow (\forall X3. \\
& (m1_subset_1\ X3\ (k1_zfmisc_1\ (u1_struct_0\ X0))) \Rightarrow (\neg(X2 \in X3) \wedge (\\
& (X3 \in X1) \wedge (\forall X4.((v1_funct_1\ X4) \wedge ((v1_funct_2\ X4\ (u1_struct_0 \\
& X0)\ (u1_struct_0\ k5_topmetr)) \wedge ((v5_pre_topc\ X4\ X0\ k5_topmetr) \wedge \\
& (m1_subset_1\ X4\ (k1_zfmisc_1\ (k2_zfmisc_1\ (u1_struct_0\ X0)\ (u1_struct_0 \\
& k5_topmetr)))))) \Rightarrow (\neg(k1_funct_1\ X4\ X2 = k6_numbers) \wedge (r1_tarSKI \\
& (k7_relset_1\ (u1_struct_0\ X0)\ (u1_struct_0\ k5_topmetr)\ X4\ (k3_subset_1 \\
& (u1_struct_0\ X0)\ X3))\ (k6_domain_1\ k1_numbers\ np_1))))))))) \Rightarrow \\
& \hspace{15em} (6)
\end{aligned}$$