

t4.altcat\_3  
(TMPD3qr5kDs1N5oGDGPcYXAv2xRaELCABwf)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_altcat\_1 : \iota \Rightarrow o$  be given. Let  $v11\_altcat\_1 : \iota \Rightarrow o$  be given. Let  $v12\_altcat\_1 : \iota \Rightarrow o$  be given. Let  $l2\_altcat\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_altcat\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_altcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_altcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v1\_altcat\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_altcat\_3 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_altcat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_altcat\_1 X0) \wedge ((v11\_altcat\_1 \\ & X0) \wedge ((v12\_altcat\_1 X0) \wedge (l2\_altcat\_1 X0)))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0)) \Rightarrow (\neg(k1\_altcat\_1 X0 X1 X2 \neq k1\_xboole\_0) \wedge ((k1\_altcat\_1 X0 X2 \\ & X1 \neq k1\_xboole\_0) \wedge (\exists X3.(m1\_subset\_1 X3 (k1\_altcat\_1 X0 \\ & X1 X2)) \wedge ((v1\_altcat\_3 X3 X0 X1 X2) \wedge ((v2\_altcat\_3 X3 X0 X1 X2) \wedge (\neg \\ & (k5\_altcat\_1 X0 X1 X2 X1 X3 (k1\_altcat\_3 X0 X1 X2 X3) = k8\_altcat\_1 \\ & X0 X1) \wedge (k5\_altcat\_1 X0 X2 X1 X2 (k1\_altcat\_3 X0 X1 X2 X3) X3 = k8\_altcat\_1 \\ & X0 X2)))))))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v12\_altcat\_1 X0) \wedge (l2\_altcat\_1 \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow ((v1\_altcat\_3 \\ & (k8\_altcat\_1 X0 X1) X0 X1 X1) \wedge (v2\_altcat\_3 (k8\_altcat\_1 X0 X1) X0 \\ & X1 X1))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v12\_altcat\_1 X0) \wedge (l2\_altcat\_1 \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (k1\_altcat\_1 \\ & X0 X1 X1 \neq k1\_xboole\_0)) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge ((v12\_altcat\_1 X0) \wedge \\ & (l2\_altcat\_1 X0))) \wedge (m1\_subset\_1 X1 (u1\_struct\_0 X0))) \Rightarrow (m1\_subset\_1 \\ & (k8\_altcat\_1 X0 X1) (k1\_altcat\_1 X0 X1 X1)) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((\neg v2\_struct\_0 \\ & X0) \wedge ((v2\_altcat\_1 X0) \wedge ((v11\_altcat\_1 X0) \wedge ((v12\_altcat\_1 X0) \wedge \\ & (l2\_altcat\_1 X0)))))) \wedge ((m1\_subset\_1 X1 (u1\_struct\_0 X0)) \wedge ((m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X3 (k1\_altcat\_1 X0 X1 X2)))))) \Rightarrow \\ & (m1\_subset\_1 (k1\_altcat\_3 X0 X1 X2 X3) (k1\_altcat\_1 X0 X2 X1)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. (((\neg v2\_struct\_0 X0) \wedge ((v12\_altcat\_1 X0) \wedge (l2\_altcat\_1 \\ & X0))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (k1\_altcat\_1 X0 X1 X1)) \Rightarrow ((X2 = k8\_altcat\_1 X0 X1) \Leftrightarrow \\ & (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow ((k1\_altcat\_1 \\ & X0 X1 X3 \neq k1\_xboole\_0) \Rightarrow (\forall X4. (m1\_subset\_1 X4 (k1\_altcat\_1 \\ & X0 X1 X3)) \Rightarrow (k5\_altcat\_1 X0 X1 X1 X3 X2 X4 = X4))))))) \end{aligned} \quad (6)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. (((\neg v2\_struct\_0 X0) \wedge ((v2\_altcat\_1 X0) \wedge ((v11\_altcat\_1 \\ & X0) \wedge ((v12\_altcat\_1 X0) \wedge (l2\_altcat\_1 X0)))))) \Rightarrow (\forall X1. (m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0)) \Rightarrow (k1\_altcat\_3 X0 X1 X1 (k8\_altcat\_1 X0 X1) = \\ & k8\_altcat\_1 X0 X1)) \end{aligned}$$