

t4_arytm_0 (TM-
SLP8RzLXuSLuQfXCTcJrYXDXqGF3fBsZ)

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Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_arytm_2 : \iota$ be given. Let $k2_arytm_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_numbers : \iota$ be given. Let $r1_arytm_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_arytm_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_arytm_3 : \iota$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 X1 k2_arytm_2) \Rightarrow (\neg(\neg r1_arytm_2 X0 X1) \wedge (k1_arytm_1 X0 X1 = k11_arytm_3))) \quad (1)$$

Assume the following.

$$\forall X0.\forall X1.(m1_subset_1 X0 X1) \Rightarrow ((v1_xboole_0 X1) \vee (X0 \in X1)) \quad (2)$$

Assume the following.

$$\forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow ((X0 \neq k11_arytm_3) \Rightarrow (k4_tarski k11_arytm_3 X0 \in k1_numbers)) \quad (3)$$

Assume the following.

$$r1_tarski k2_arytm_2 k1_numbers \quad (4)$$

Assume the following.

$$\neg v1_xboole_0 k2_arytm_2 \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((m1_subset_1 X0 k2_arytm_2) \wedge (m1_subset_1 X1 k2_arytm_2)) \Rightarrow (m1_subset_1 (k1_arytm_1 X0 X1) k2_arytm_2) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.(r1_tarski X0 X1) \Leftrightarrow (\forall X2.(X2 \in X0) \Rightarrow (X2 \in X1)) \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k2_arytm_2) \Rightarrow (((r1_arytm_2 X1 X0) \Rightarrow (k2_arytm_1 X0 X1 = k1_arytm_1 \\ & X0 X1)) \wedge ((\neg r1_arytm_2 X1 X0) \Rightarrow (k2_arytm_1 X0 X1 = k4_tarski k11_arytm_3 \\ & (k1_arytm_1 X1 X0)))))) \end{aligned} \tag{8}$$

Theorem 1

$$\begin{aligned} & \forall X0.(m1_subset_1 X0 k2_arytm_2) \Rightarrow (\forall X1.(m1_subset_1 \\ & X1 k2_arytm_2) \Rightarrow (k2_arytm_1 X0 X1 \in k1_numbers)) \end{aligned}$$