

t4_eqrel_1
(TMSD2bKjQ45HGbYzd3vPhcNuds35D9d5XpL)

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Let $v3_relat_2 : \iota \Rightarrow o$ be given. Let $k1_eqrel_1 : \iota \Rightarrow \iota$ be given. Let $v8_relat_2 : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_relat_1 : \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_relat_2 : \iota \Rightarrow o$ be given. Let $r8_relat_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r3_relat_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.(k4_tarski\ X0\ X1 \in k2_zfmisc_1\ X2\ X3) \Leftrightarrow ((X0 \in X2) \wedge (X1 \in X3)) \quad (1)$$

Assume the following.

$$\forall X0.\forall X1.((v1_partfun1\ X1\ X0) \wedge (m1_subset_1\ X1\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X0)))) \Rightarrow (k1_relat_1\ X1 = X0) \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.v1_relat_1\ (k2_zfmisc_1\ X0\ X1) \quad (3)$$

Assume the following.

$$\forall X0.(v1_relat_2\ (k1_eqrel_1\ X0)) \wedge (v1_partfun1\ (k1_eqrel_1\ X0)\ X0) \quad (4)$$

Assume the following.

$$\forall X0.m1_subset_1\ (k1_eqrel_1\ X0)\ (k1_zfmisc_1\ (k2_zfmisc_1\ X0\ X0)) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1_relat_1\ X0) \Rightarrow (\forall X1.(r8_relat_2\ X0\ X1) \Leftrightarrow (\forall X2. \\ & \forall X3.\forall X4.((X2 \in X1) \wedge ((X3 \in X1) \wedge ((X4 \in X1) \wedge (k4_tarski \\ & X2\ X3 \in X0) \wedge (k4_tarski\ X3\ X4 \in X0)))))) \Rightarrow (k4_tarski\ X2\ X4 \in X0)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1_relat_1 X0) \Rightarrow (\forall X1.(r3_relat_2 X0 X1) \Leftrightarrow (\forall X2. \\ \forall X3.((X2 \in X1) \wedge ((X3 \in X1) \wedge (k4_tarski X2 X3 \in X0))) \Rightarrow (k4_tarski \\ X3 X2 \in X0))) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.k1_eqrel_1 X0 = k2_zfmisc_1 X0 X0 \quad (8)$$

Assume the following.

$$\forall X0.(v1_relat_1 X0) \Rightarrow ((v8_relat_2 X0) \Leftrightarrow (r8_relat_2 X0 (k1_relat_1 X0))) \quad (9)$$

Assume the following.

$$\forall X0.(v1_relat_1 X0) \Rightarrow ((v3_relat_2 X0) \Leftrightarrow (r3_relat_2 X0 (k1_relat_1 X0))) \quad (10)$$

Theorem 1

$$\begin{aligned} \forall X0.(v3_relat_2 (k1_eqrel_1 X0) \wedge ((v8_relat_2 (k1_eqrel_1 \\ X0) \wedge (v1_partfun1 (k1_eqrel_1 X0) X0) \wedge (m1_subset_1 (k1_eqrel_1 \\ X0) (k1_zfmisc_1 (k2_zfmisc_1 X0 X0)))))) \end{aligned}$$