

t4\_numerall (TM-  
VAyuEFTMG4XH4fVErZdhDe6UN71ptQz78)

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Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $np\_1 : \iota$  be given. Let  $k1\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_numeral1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $np\_0 : \iota$  be given. Let  $k5\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v4\_valued\_0 : \iota \Rightarrow o$  be given. Let  $k1\_recdef\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v5\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k1\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_card\_1 : \iota \Rightarrow o$  be given. Let  $v3\_relat\_1 : \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k1\_numeral1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k21\_binop\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0.(v1\_xboole\_0 X0) \Rightarrow (X0 = k1\_xboole\_0) \quad (1)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0) \Rightarrow ((\neg r1\_xxreal\_0 np\_1 X0) \Rightarrow (X0 = k6\_numbers)) \quad (2)$$

Assume the following.

$$v1\_xboole\_0 np\_0 \quad (3)$$

Assume the following.

$$k6\_numbers = k1\_xboole\_0 \quad (4)$$

Assume the following.

$$\forall X0.k5\_afinsq\_1 X0 = k3\_afinsq\_1 X0 \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v4\_valued\_0 X0))) \Rightarrow (k1\_recdef\_1 X0 X1 = k1\_funct\_1 X0 X1) \quad (6)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_afinsq\_1 X0 = k1\_card\_1 X0) \quad (7)$$

Assume the following.

$$\forall X0. \exists X1. (v1\_relat\_1 X1) \wedge ((v5\_relat\_1 X1 X0) \wedge ((v5\_ordinal1 X1) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_xboole\_0 X1) \wedge (v1\_finset\_1 X1))))) \quad (8)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_card\_1 X0 = k9\_xtuple\_0 X0) \quad (9)$$

Assume the following.

$$\forall X0. \neg v1\_xboole\_0 (k3\_afinsq\_1 X0) \quad (10)$$

Assume the following.

$$\forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow ((\neg v1\_xboole\_0 (k1\_card\_1 X0)) \wedge (v1\_card\_1 (k1\_card\_1 X0))) \quad (11)$$

Assume the following.

$$\forall X0. (v1\_xboole\_0 X0) \Rightarrow ((v1\_xboole\_0 (k1\_card\_1 X0)) \wedge (v1\_card\_1 (k1\_card\_1 X0))) \quad (12)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (v7\_ordinal1 (k9\_xtuple\_0 X0)) \quad (13)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X0) \wedge ((v3\_relat\_1 X0) \wedge (v1\_funct\_1 X0))) \Rightarrow (v1\_xboole\_0 (k1\_funct\_1 X0 X1)) \quad (14)$$

Assume the following.

$$\forall X0. \forall X1. ((v7\_ordinal1 X0) \wedge (v7\_ordinal1 X1)) \Rightarrow ((v1\_relat\_1 (k2\_numeral1 X0 X1)) \wedge ((v5\_relat\_1 (k2\_numeral1 X0 X1) k5\_numbers) \wedge ((v1\_funct\_1 (k2\_numeral1 X0 X1)) \wedge ((v5\_ordinal1 (k2\_numeral1 X0 X1)) \wedge (v1\_finset\_1 (k2\_numeral1 X0 X1))))) \quad (15)$$

Assume the following.

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.(v7\_ordinal1\ X1) \Rightarrow (( \\
& \quad \neg r1\_xxreal\_0\ X1\ np\_1) \Rightarrow (\forall X2.((v1\_relat\_1\ X2) \wedge ((v5\_relat\_1 \\
& \quad X2\ k5\_numbers) \wedge ((v1\_funct\_1\ X2) \wedge ((v5\_ordinal1\ X2) \wedge (v1\_finset\_1 \\
& \quad X2)))))) \Rightarrow (((X0 \neq k6\_numbers) \Rightarrow ((X2 = k2\_numeral1\ X0\ X1) \Leftrightarrow ((k1\_numeral1 \\
& \quad X2\ X1 = X0) \wedge ((k1\_recdef\_1\ X2\ (k21\_binop\_2\ (k1\_afinsq\_1\ X2)\ np\_1) \neq \\
& \quad k6\_numbers) \wedge (\forall X3.(v7\_ordinal1\ X3) \Rightarrow ((X3 \in k1\_relset\_1 \\
& \quad k5\_numbers\ X2) \Rightarrow ((r1\_xxreal\_0\ k6\_numbers\ (k1\_recdef\_1\ X2\ X3)) \wedge \\
& \quad (\neg r1\_xxreal\_0\ X1\ (k1\_recdef\_1\ X2\ X3)))))))))) \wedge ((X0 = k6\_numbers) \Rightarrow \\
& \quad ((X2 = k2\_numeral1\ X0\ X1) \Leftrightarrow (X2 = k5\_afinsq\_1\ k6\_numbers))))))
\end{aligned} \tag{16}$$

Assume the following.

$$\forall X0.((v1\_xboole\_0\ X0) \wedge (v1\_relat\_1\ X0)) \Rightarrow ((v1\_relat\_1\ X0) \wedge (v4\_valued\_0\ X0)) \tag{17}$$

Assume the following.

$$\forall X0.((v1\_xboole\_0\ X0) \wedge (v1\_relat\_1\ X0)) \Rightarrow ((v1\_relat\_1\ X0) \wedge (v3\_relat\_1\ X0)) \tag{18}$$

Assume the following.

$$\forall X0.(v1\_xboole\_0\ X0) \Rightarrow (v1\_relat\_1\ X0) \tag{19}$$

Assume the following.

$$\forall X0.(v1\_xboole\_0\ X0) \Rightarrow (v1\_funct\_1\ X0) \tag{20}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(v7\_ordinal1\ X0) \Rightarrow (\forall X1.(v7\_ordinal1\ X1) \Rightarrow (( \\
& \quad \neg r1\_xxreal\_0\ X1\ np\_1) \Rightarrow (r1\_xxreal\_0\ np\_1\ (k1\_afinsq\_1\ (k2\_numeral1 \\
& \quad X0\ X1))))))
\end{aligned}$$