

## t4\_seqm\_3

(TMFG8oLyvigoyiKm1pRRBGjBApcLiUBvpJG)

October 27, 2020

Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v6\_valued\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. ((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v6\_valued\_0 X0) \Leftrightarrow (\forall X1. (m2\_subset\_1 X1 k1\_numbers k5\_numbers) \Rightarrow \\ & (\forall X2. (m2\_subset\_1 X2 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xxreal\_0 \\ & (k8\_nat\_1 k1\_numbers X0 X1) (k8\_nat\_1 k1\_numbers X0 (k2\_nat\_1 ( \\ & k2\_nat\_1 X1 np\_1) X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\
& (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\
& (((\forall X1.(m2\_subset\_1 X1 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xxreal\_0 \\
& (k8\_nat\_1 k1\_numbers X0 X1) (k8\_nat\_1 k1\_numbers X0 (k2\_nat\_1 X1 \\
& np\_1)))))) \Rightarrow (\forall X1.(m2\_subset\_1 X1 k1\_numbers k5\_numbers) \Rightarrow \\
& (\forall X2.(m2\_subset\_1 X2 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xxreal\_0 \\
& (k8\_nat\_1 k1\_numbers X0 X1) (k8\_nat\_1 k1\_numbers X0 (k2\_nat\_1 ( \\
& k2\_nat\_1 X1 np\_1) X2)))))) \wedge (((\forall X1.(m2\_subset\_1 X1 k1\_numbers \\
& k5\_numbers) \Rightarrow (\forall X2.(m2\_subset\_1 X2 k1\_numbers k5\_numbers) \Rightarrow \\
& (\neg r1\_xxreal\_0 (k8\_nat\_1 k1\_numbers X0 X1) (k8\_nat\_1 k1\_numbers \\
& X0 (k2\_nat\_1 (k2\_nat\_1 X1 np\_1) X2)))))) \Rightarrow (\forall X1.(m2\_subset\_1 \\
& X1 k1\_numbers k5\_numbers) \Rightarrow (\forall X2.(m2\_subset\_1 X2 k1\_numbers \\
& k5\_numbers) \Rightarrow (\neg (\neg r1\_xxreal\_0 X2 X1) \wedge (r1\_xxreal\_0 (k8\_nat\_1 k1\_numbers \\
& X0 X1) (k8\_nat\_1 k1\_numbers X0 X2)))))) \wedge ((\forall X1.(m2\_subset\_1 \\
& X1 k1\_numbers k5\_numbers) \Rightarrow (\forall X2.(m2\_subset\_1 X2 k1\_numbers \\
& k5\_numbers) \Rightarrow (\neg (\neg r1\_xxreal\_0 X2 X1) \wedge (r1\_xxreal\_0 (k8\_nat\_1 k1\_numbers \\
& X0 X1) (k8\_nat\_1 k1\_numbers X0 X2)))))) \Rightarrow (\forall X1.(m2\_subset\_1 \\
& X1 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xxreal\_0 (k8\_nat\_1 k1\_numbers \\
& X0 X1) (k8\_nat\_1 k1\_numbers X0 (k2\_nat\_1 X1 np\_1))))))
\end{aligned} \tag{2}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\
& (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\
& ((v6\_valued\_0 X0) \Leftrightarrow (\forall X1.(m2\_subset\_1 X1 k1\_numbers k5\_numbers) \Rightarrow \\
& (\forall X2.(m2\_subset\_1 X2 k1\_numbers k5\_numbers) \Rightarrow (\neg (\neg r1\_xxreal\_0 \\
& X2 X1) \wedge (r1\_xxreal\_0 (k8\_nat\_1 k1\_numbers X0 X1) (k8\_nat\_1 k1\_numbers \\
& X0 X2))))))
\end{aligned}$$