

t4\_trees\_a  
(TMKhRj7HvAkTzAWHmCttUEYT7vwDfoJrd2h)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_trees\_1 : \iota \Rightarrow o$  be given. Let  $m4\_trees\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_trees\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $r2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_trees\_1 : \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finseq\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (\neg(\neg r2\_xboole\_0 X0 X1) \wedge ((X0 \neq X1) \wedge (\neg r2\_xboole\_0 X1 X0))) \Leftrightarrow (r3\_xboole\_0 X0 X1) \quad (2)$$

Assume the following.

$$\forall X0. ((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. (m1\_trees\_1 X1 X0) \Leftrightarrow (m1\_subset\_1 X1 X0)) \quad (3)$$

Assume the following.

$$\forall X0. ((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. (m4\_trees\_1 X1 X0) \Rightarrow (v2\_trees\_1 X1)) \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. (r1\_tarski X0 X1) \Leftrightarrow (\forall X2. (X2 \in X0) \Rightarrow (X2 \in X1)) \quad (5)$$

Assume the following.

$$\forall X0. ((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. (v2\_trees\_1 X1) \Rightarrow ((m4\_trees\_1 X1 X0) \Leftrightarrow (r1\_tarski X1 X0))) \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.(v2\_trees\_1 X0) \Leftrightarrow & ((\forall X1.(X1 \in X0) \Rightarrow ((v1\_relat\_1 \\ X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finseq\_1 X1)))) \wedge & (\forall X1.((v1\_relat\_1 \\ X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finseq\_1 X1))) \Rightarrow & (\forall X2.((v1\_relat\_1 \\ X2) \wedge ((v1\_funct\_1 X2) \wedge (v1\_finseq\_1 X2))) \Rightarrow & (\neg(X1 \in X0) \wedge ((X2 \in X0) \wedge \\ & ((X1 \neq X2) \wedge (r3\_xboole\_0 X1 X2))))))) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.(r2\_xboole\_0 X0 X1) \Rightarrow (\neg r2\_xboole\_0 X1 X0) \quad (8)$$

**Theorem 1**

$$\begin{aligned} \forall X0.((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow & (\forall X1. \\ (m4\_trees\_1 X1 X0) \Rightarrow (r1\_tarski X1 (ReplSep (toset & (\lambda X2 : \iota. \\ m1\_trees\_1 X2 X0)) (\lambda X2 : \iota.\forall X3.(m2\_finseq\_1 X3 & k5\_numbers) \Rightarrow \\ (\neg(X3 \in X1) \wedge (r2\_xboole\_0 X3 X2))) (\lambda X2 : \iota.X2)))) \end{aligned}$$