

t50\_pre\_poly (TMJs-  
nuMT6SG9VYcMWYsuQmZvTn6povP4H8z)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_poly : \iota \Rightarrow o$  be given. Let  $r6\_pboole : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k11\_pre\_poly : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r3\_pre\_poly : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xcmplx\_0 : \iota \Rightarrow o$  be given. Let  $k3\_binop\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v3\_valued\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 X0) \wedge \\ & (v1\_funct\_1 X1) \wedge ((v1\_partfun1 X1 X0) \wedge ((v4\_valued\_0 X1) \wedge (v2\_pre\_poly \\ & X1)))))) \Rightarrow (\forall X2. ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 X2 X0) \wedge \\ & (v1\_funct\_1 X2) \wedge ((v1\_partfun1 X2 X0) \wedge ((v4\_valued\_0 X2) \wedge (v2\_pre\_poly \\ & X2)))))) \Rightarrow ((\forall X3. (X3 \in X0) \Rightarrow (r1\_xxreal\_0 (k1\_funct\_1 X1 X3) \\ & (k1\_funct\_1 X2 X3))) \Rightarrow (r3\_pre\_poly X0 X1 X2))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. (v7\_ordinal1 X0) \Rightarrow (\forall X1. (v7\_ordinal1 X1) \Rightarrow (r1\_xxreal\_0 X0 (k2\_xcmplx\_0 X0 X1))) \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 \\ & X1 X0) \wedge ((v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 X0)))) \wedge ((v1\_relat\_1 \\ & X2) \wedge ((v4\_relat\_1 X2 X0) \wedge ((v1\_funct\_1 X2) \wedge (v1\_partfun1 X2 X0)))))) \Rightarrow \\ & ((r6\_pboole X0 X1 X2) \Leftrightarrow (X1 = X2)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_xcmplx\_0 X0) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow (k3\_binop\_2 X0 X1 = k2\_xcmplx\_0 X0 X1) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v4\_valued\_0 X0)))\Rightarrow(v7\_ordinal1 (k1\_funct\_1 X0 X1)) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 X0)))\Rightarrow(v1\_xcmplx\_0 (k1\_funct\_1 X0 X1)) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge((v4\_relat\_1 \\ & X1 X0)\wedge((v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v1\_valued\_0 X1))))\wedge \\ & ((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 X2)\wedge((v1\_partfun1 \\ & X2 X0)\wedge(v1\_valued\_0 X2))))))\Rightarrow((v1\_relat\_1 (k11\_pre\_poly X0 X1 \\ & X2))\wedge((v4\_relat\_1 (k11\_pre\_poly X0 X1 X2) X0)\wedge((v1\_funct\_1 (k11\_pre\_poly \\ & X0 X1 X2))\wedge(v1\_partfun1 (k11\_pre\_poly X0 X1 X2) X0)))) \quad (7) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v4\_relat\_1 X1 X0)\wedge( \\ & (v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v1\_valued\_0 X1))))\Rightarrow( \\ & \forall X2.((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 \\ & X2)\wedge((v1\_partfun1 X2 X0)\wedge(v1\_valued\_0 X2))))\Rightarrow(\forall X3.( \\ & (v1\_relat\_1 X3)\wedge((v4\_relat\_1 X3 X0)\wedge((v1\_funct\_1 X3)\wedge(v1\_partfun1 \\ & X3 X0))))\Rightarrow((X3 = k11\_pre\_poly X0 X1 X2)\Leftrightarrow(\forall X4.k1\_funct\_1 \\ & X3 X4 = k3\_binop\_2 (k1\_funct\_1 X1 X4) (k1\_funct\_1 X2 X4)))) \quad (8) \end{aligned}$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge(v4\_valued\_0 X0))\Rightarrow((v1\_relat\_1 X0)\wedge(v3\_valued\_0 X0)) \quad (9)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0)\wedge(v3\_valued\_0 X0))\Rightarrow((v1\_relat\_1 X0)\wedge(v1\_valued\_0 X0)) \quad (10)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v4\_relat\_1 X1 X0)\wedge( \\ & (v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge((v4\_valued\_0 X1)\wedge(v2\_pre\_poly \\ & X1))))))\Rightarrow(\forall X2.((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge( \\ & (v1\_funct\_1 X2)\wedge((v1\_partfun1 X2 X0)\wedge((v4\_valued\_0 X2)\wedge(v2\_pre\_poly \\ & X2))))))\Rightarrow(\forall X3.((v1\_relat\_1 X3)\wedge((v4\_relat\_1 X3 X0)\wedge( \\ & (v1\_funct\_1 X3)\wedge((v1\_partfun1 X3 X0)\wedge((v4\_valued\_0 X3)\wedge(v2\_pre\_poly \\ & X3))))))\Rightarrow((r6\_pboole X0 X1 (k11\_pre\_poly X0 X2 X3))\Rightarrow(r3\_pre\_poly \\ & X0 X2 X1)))) \end{aligned}$$