

t53\_genealg1 (TMWfKd-  
FCAgFhoxJ1jwzCSnUw4ARNbGaSRGK)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v2\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finseq\_1 : \iota \Rightarrow o$  be given. Let  $m1\_genealg1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_genealg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_genealg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_genealg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_card\_3 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.(m1\_subset\_1 X0 k5\_numbers) \Rightarrow (\forall X1.(m1\_subset\_1 \\
 & \quad X1 k5\_numbers) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
 & (m1\_subset\_1 X3 k5\_numbers) \Rightarrow (\forall X4.(m1\_subset\_1 X4 k5\_numbers) \Rightarrow \\
 & \quad (\forall X5.((\neg v1\_xboole\_0 X5) \wedge ((v1\_relat\_1 X5) \wedge ((v2\_relat\_1 \\
 & \quad X5) \wedge ((v1\_funct\_1 X5) \wedge (v1\_finseq\_1 X5)))))) \Rightarrow (\forall X6.(m1\_genealg1 \\
 & \quad X6 X5) \Rightarrow (\forall X7.(m1\_genealg1 X7 X5) \Rightarrow (m1\_genealg1 (k5\_genealg1 \\
 & \quad X5 X6 X7 X0 X1 X2 X3 X4) X5)))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0.(m1\_subset\_1 X0 k5\_numbers) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 \\
 & X1) \wedge ((v1\_relat\_1 X1) \wedge ((v2\_relat\_1 X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finseq\_1 \\
 & \quad X1)))))) \Rightarrow (\forall X2.(m1\_genealg1 X2 X1) \Rightarrow (\forall X3.(m1\_genealg1 \\
 & \quad X3 X1) \Rightarrow (m1\_genealg1 (k1\_genealg1 X1 X2 X3 X0) X1)))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 \\
 & X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finseq\_1 X0)))))) \Rightarrow (\forall X1.(m1\_genealg1 \\
 & \quad X1 X0) \Rightarrow (m2\_finseq\_1 X1 (k3\_card\_3 X0)))
 \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_relat\_1 X0) \wedge ((v2\_relat\_1 \\
& X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finseq\_1 X0)))))) \Rightarrow (\forall X1.(m2\_finseq\_1 \\
& X1 (k3\_card\_3 X0)) \Rightarrow (\forall X2.(m2\_finseq\_1 X2 (k3\_card\_3 X0)) \Rightarrow \\
& (\forall X3.(m1\_subset\_1 X3 k5\_numbers) \Rightarrow (\forall X4.(m1\_subset\_1 \\
& X4 k5\_numbers) \Rightarrow (\forall X5.(m1\_subset\_1 X5 k5\_numbers) \Rightarrow (\forall X6. \\
& (m1\_subset\_1 X6 k5\_numbers) \Rightarrow (\forall X7.(m1\_subset\_1 X7 k5\_numbers) \Rightarrow \\
& (\forall X8.(m1\_subset\_1 X8 k5\_numbers) \Rightarrow (k6\_genealg1 X0 X1 X2 \\
& X3 X4 X5 X6 X7 X8 = k1\_genealg1 X0 (k5\_genealg1 X0 X1 X2 X3 X4 X5 X6 X7) \\
& (k5\_genealg1 X0 X2 X1 X3 X4 X5 X6 X7) X8)))))))))) \\
& \hspace{15em} (4)
\end{aligned}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.(m1\_subset\_1 X0 k5\_numbers) \Rightarrow (\forall X1.(m1\_subset\_1 \\
& X1 k5\_numbers) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k5\_numbers) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 k5\_numbers) \Rightarrow (\forall X4.(m1\_subset\_1 X4 k5\_numbers) \Rightarrow \\
& (\forall X5.(m1\_subset\_1 X5 k5\_numbers) \Rightarrow (\forall X6.((\neg v1\_xboole\_0 \\
& X6) \wedge ((v1\_relat\_1 X6) \wedge (v2\_relat\_1 X6) \wedge (v1\_funct\_1 X6) \wedge (v1\_finseq\_1 \\
& X6)))))) \Rightarrow (\forall X7.(m1\_genealg1 X7 X6) \Rightarrow (\forall X8.(m1\_genealg1 \\
& X8 X6) \Rightarrow (m1\_genealg1 (k6\_genealg1 X6 X7 X8 X0 X1 X2 X3 X4 X5) X6))))))
\end{aligned}$$