

## t54\_card\_2

(TMEw6KtEp7wm62g3tLEQ9zpXLZkiodzurgQ)

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Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_enumset1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_6 : \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_enumset1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_5 : \iota$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xreal\_0 X2) \Rightarrow (\forall X3.(v1\_xreal\_0 X3) \Rightarrow (((r1\_xxreal\_0 \\ & X0 X1) \wedge (r1\_xxreal\_0 X2 X3)) \Rightarrow (r1\_xxreal\_0 (k2\_xcmplx\_0 X0 X2) ( \\ & k2\_xcmplx\_0 X1 X3)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. r1\_xxreal\_0 \\ & (k5\_card\_1 (k3\_enumset1 X0 X1 X2 X3 X4)) np\_5 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_finset\_1 X0) \Rightarrow (\forall X1.(v1\_finset\_1 X1) \Rightarrow (r1\_xxreal\_0 \\ & (k5\_card\_1 (k2\_xboole\_0 X0 X1)) (k2\_nat\_1 (k5\_card\_1 X0) (k5\_card\_1 \\ & X1)))) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0. k1\_card\_1 (k1\_tarski X0) = np\_1 \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow (((r1\_xxreal\_0 X0 X1) \wedge (r1\_xxreal\_0 X1 X2)) \Rightarrow \\ & (r1\_xxreal\_0 X0 X2)))) \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\ & k4\_enumset1\ X0\ X1\ X2\ X3\ X4\ X5 = k2\_xboole\_0\ (k1\_tarski\ X0)\ (k3\_enumset1 \\ & \quad X1\ X2\ X3\ X4\ X5) \end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0\ np\_6) \wedge (m2\_subset\_1\ np\_6\ k1\_numbers\ k5\_numbers)) \wedge \\ & ((m1\_subset\_1\ np\_6\ k5\_numbers) \wedge (m1\_subset\_1\ np\_6\ k1\_numbers)) \end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0\ np\_5) \wedge (m2\_subset\_1\ np\_5\ k1\_numbers\ k5\_numbers)) \wedge \\ & ((m1\_subset\_1\ np\_5\ k5\_numbers) \wedge (m1\_subset\_1\ np\_5\ k1\_numbers)) \end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0\ np\_1) \wedge (m2\_subset\_1\ np\_1\ k1\_numbers\ k5\_numbers)) \wedge \\ & ((m1\_subset\_1\ np\_1\ k5\_numbers) \wedge (m1\_subset\_1\ np\_1\ k1\_numbers)) \end{aligned} \tag{9}$$

Assume the following.

$$k2\_xcmplx\_0\ np\_1\ np\_5 = np\_6 \tag{10}$$

Assume the following.

$$r1\_xxreal\_0\ np\_1\ np\_1 \tag{11}$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \tag{12}$$

Assume the following.

$$\forall X0.(v1\_finset\_1\ X0) \Rightarrow (k5\_card\_1\ X0 = k1\_card\_1\ X0) \tag{13}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1\_subset\_1\ X0\ k5\_numbers) \wedge (v7\_ordinal1 \\ & \quad X1)) \Rightarrow (k2\_nat\_1\ X0\ X1 = k2\_xcmplx\_0\ X0\ X1) \end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\ & v1\_finset\_1\ (k4\_enumset1\ X0\ X1\ X2\ X3\ X4\ X5) \end{aligned} \tag{15}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_xreal\_0\ X0) \wedge (v1\_xreal\_0\ X1)) \Rightarrow (v1\_xreal\_0 \\ & \quad (k2\_xcmplx\_0\ X0\ X1)) \end{aligned} \tag{16}$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.\forall X4.v1\_finset\_1 (k3\_enumset1 X0 X1 X2 X3 X4) \quad (17)$$

Assume the following.

$$\forall X0.v1\_finset\_1 (k1\_tarski X0) \quad (18)$$

Assume the following.

$$\forall X0.(v1\_finset\_1 X0)\Rightarrow(m1\_subset\_1 (k5\_card\_1 X0) k4\_ordinal1) \quad (19)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k4\_ordinal1)\Rightarrow(v7\_ordinal1 X0) \quad (20)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0)\Rightarrow(v1\_xxreal\_0 X0) \quad (21)$$

Assume the following.

$$\forall X0.(v7\_ordinal1 X0)\Rightarrow(v1\_xreal\_0 X0) \quad (22)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k1\_numbers)\Rightarrow(v1\_xreal\_0 X0) \quad (23)$$

**Theorem 1**

$$\forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. r1\_xreal\_0 (k5\_card\_1 (k4\_enumset1 X0 X1 X2 X3 X4 X5)) np\_6$$