

# t55\_xboolean (TMKjgoyBWKXAhdmHreAEM- BRKSi8QZceBF32)

October 27, 2020

Let  $v1\_xboolean : \iota \Rightarrow o$  be given. Let  $k8\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xboolean : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (\forall X2. \\ & (v1\_xboolean X2) \Rightarrow (k4\_xboolean X0 (k5\_xboolean X1 X2) = k5\_xboolean \\ & (k4\_xboolean X0 X1) (k4\_xboolean X0 X2)))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (k4\_xboolean \\ & X0 (k8\_xboolean X0 X1) = k4\_xboolean X0 (k3\_xboolean X1))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (k3\_xboolean (k3\_xboolean X0) = X0) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_xboolean X0) \wedge (v1\_xboolean X1)) \Rightarrow ( \\ & v1\_xboolean (k8\_xboolean X0 X1)) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_xboolean X0) \wedge (v1\_xboolean X1)) \Rightarrow ( \\ & v1\_xboolean (k5\_xboolean X0 X1)) \end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_xboolean X0) \wedge (v1\_xboolean X1)) \Rightarrow ( \\ & v1\_xboolean (k4\_xboolean X0 X1)) \end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (k8\_xboolean \\ & X0 X1 = k3\_xboolean (k4\_xboolean X0 X1))) \end{aligned} \tag{7}$$

Assume the following.

$$\forall X0.(v1\_xboolean\ X0) \Rightarrow (\forall X1.(v1\_xboolean\ X1) \Rightarrow (k5\_xboolean\ X0\ X1 = k3\_xboolean\ (k4\_xboolean\ (k3\_xboolean\ X0)\ (k3\_xboolean\ X1)))) \quad (8)$$

**Theorem 1**

$$\forall X0.(v1\_xboolean\ X0) \Rightarrow (\forall X1.(v1\_xboolean\ X1) \Rightarrow (\forall X2.(v1\_xboolean\ X2) \Rightarrow (k8\_xboolean\ X0\ (k5\_xboolean\ X1\ X2) = k4\_xboolean\ (k3\_xboolean\ (k4\_xboolean\ X0\ X1)\ (k3\_xboolean\ (k4\_xboolean\ X0\ X2))))))$$