

t56\_pdiff\_9  
(TMG8UJ48yox7y9k2Kwz4iaeC4Dj2BQd6ubM)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_euclid : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $r2\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_pdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_pdiff\_9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_pdiff\_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_finseq\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k7\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_pdiff\_9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pdiff\_9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_pdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k1\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k8\_pdiff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k1\_pdiff\_7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge (m2\_subset\_1 X0 k1\_numbers k5\_numbers)) \Rightarrow \\
& (\forall X1. \forall X2. ((v1\_funct\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k1\_euclid X0) k1\_numbers)))) \Rightarrow (\forall X3. ((v1\_funct\_1 \\
& X3) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) \\
& (k1\_euclid np\_1)))))) \Rightarrow ((r2\_relset\_1 (k1\_euclid X0) (k1\_euclid \\
& np\_1) (k3\_pdiff\_1 X0 X2) X3) \Rightarrow (((r1\_tarski X1 (k1\_relset\_1 (k1\_euclid \\
& X0) X2)) \wedge (r2\_pdiff\_9 X1 X0 X2)) \Leftrightarrow (r1\_pdiff\_6 X1 np\_1 X0 X3))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(m2\_subset\_1 X0 k1\_numbers k5\_numbers) \Rightarrow (\forall X1. \\ & ((v1\_funct\_1 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\ & k1\_euclid X0) k1\_numbers)))) \Rightarrow (k1\_relset\_1 (k1\_euclid X0) (k3\_pdiff\_1 \\ & X0 X1) = k1\_relset\_1 (k1\_euclid X0) X1)) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0 np\_1) \wedge (m2\_subset\_1 np\_1 k1\_numbers k5\_numbers)) \wedge \\ & ((m1\_subset\_1 np\_1 k5\_numbers) \wedge (m1\_subset\_1 np\_1 k1\_numbers)) \end{aligned} \quad (4)$$

Assume the following.

$$\neg v1\_xboole\_0 np\_1 \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((m1\_subset\_1 X2 \\ & (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1)))) \Rightarrow ((r2\_relset\_1 X0 X1 X2 X3) \Leftrightarrow (X2 = X3)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 \\ & X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \end{aligned} \quad (7)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\ & (((v1\_funct\_1 X4) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))) \wedge ((v1\_funct\_1 X5) \wedge (m1\_subset\_1 X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X2 X3)))))) \Rightarrow (k1\_partfun1 X0 X1 X2 X3 X4 X5 = k3\_relat\_1 X4 X5) \end{aligned} \quad (9)$$

Assume the following.

$$(\neg v1\_xboole\_0 k4\_ordinal1) \wedge (v3\_ordinal1 k4\_ordinal1) \quad (10)$$

Assume the following.

$$\neg v1\_xboole\_0 k1\_numbers \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v1\_xboole\_0 \\ & X0)\wedge(m1\_subset\_1 X0 k5\_numbers))\wedge(((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 \\ & X1 k5\_numbers))\wedge(((v1\_funct\_1 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k1\_euclid X0) (k1\_euclid X1)))))\wedge(m1\_subset\_1 \\ & X3 (k1\_euclid X0))))\Rightarrow((v1\_funct\_1 (k8\_pdiff\_1 X0 X1 X2 X3))\wedge( \\ & (v1\_funct\_2 (k8\_pdiff\_1 X0 X1 X2 X3) (k1\_euclid X0) (k1\_euclid X1))\wedge \\ & (m1\_subset\_1 (k8\_pdiff\_1 X0 X1 X2 X3) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k1\_euclid X0) (k1\_euclid X1)))))) \end{aligned} \quad (12)$$

Assume the following.

$$m1\_subset\_1 k5\_numbers (k1\_zfmisc\_1 k1\_numbers) \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v7\_ordinal1 X0)\wedge((v1\_funct\_1 X1)\wedge(m1\_subset\_1 \\ & X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) k1\_numbers))))\Rightarrow \\ & ((v1\_funct\_1 (k3\_pdiff\_1 X0 X1))\wedge(m1\_subset\_1 (k3\_pdiff\_1 X0 \\ & X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) (k1\_euclid np\_1)))))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v1\_xboole\_0 X0)\wedge(m1\_subset\_1 \\ & X0 k5\_numbers))\wedge((v1\_funct\_1 X2)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k1\_euclid X0) k1\_numbers))))\Rightarrow((v1\_funct\_1 (k2\_pdiff\_9 \\ & X0 X1 X2))\wedge(m1\_subset\_1 (k2\_pdiff\_9 X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k1\_euclid X0) (k9\_funct\_2 (k1\_euclid X0) k1\_numbers)))))) \end{aligned} \quad (15)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v1\_xboole\_0 \\ & X0)\wedge(m1\_subset\_1 X0 k5\_numbers))\wedge(((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 \\ & X1 k5\_numbers))\wedge((v1\_funct\_1 X3)\wedge(m1\_subset\_1 X3 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k1\_euclid X0) (k1\_euclid X1))))))\Rightarrow((v1\_funct\_1 \\ & (k1\_pdiff\_9 X0 X1 X2 X3))\wedge(m1\_subset\_1 (k1\_pdiff\_9 X0 X1 X2 X3) ( \\ & k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) (k9\_funct\_2 (k1\_euclid \\ & X0) (k1\_euclid X1)))))) \end{aligned} \quad (16)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v7\_ordinal1 X0)\wedge(v7\_ordinal1 X1))\Rightarrow( \\ & (v1\_funct\_1 (k1\_pdiff\_1 X0 X1))\wedge((v1\_funct\_2 (k1\_pdiff\_1 X0 X1) \\ & (k1\_euclid X1) k1\_numbers)\wedge(m1\_subset\_1 (k1\_pdiff\_1 X0 X1) (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 (k1\_euclid X1) k1\_numbers)))) \end{aligned} \quad (17)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge (m2\_subset\_1 X0 k1\_numbers k5\_numbers)) \Rightarrow \\
& (\forall X1. \forall X2. ((v1\_funct\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k1\_euclid X0) k1\_numbers)))) \Rightarrow ((r1\_tarski X1 (k1\_relset\_1 \\
& (k1\_euclid X0) X2)) \Rightarrow (\forall X3. ((v1\_funct\_1 X3) \wedge (m1\_subset\_1 \\
& X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) (k9\_funct\_2 (k1\_euclid \\
& X0) k1\_numbers)))) \Rightarrow ((X3 = k2\_pdiff\_9 X0 X1 X2) \Leftrightarrow ((k1\_relset\_1 \\
& (k1\_euclid X0) X3 = X1) \wedge (\forall X4. (m2\_finseq\_2 X4 k1\_numbers \\
& (k1\_euclid X0)) \Rightarrow ((X4 \in X1) \Rightarrow (k7\_partfun1 (k9\_funct\_2 (k1\_euclid \\
& X0) k1\_numbers) X3 X4 = k1\_pdiff\_7 X0 X2 X4))))))))) \tag{18}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge (m1\_subset\_1 X0 k5\_numbers)) \Rightarrow \\
& (\forall X1. ((v1\_funct\_1 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k1\_euclid X0) k1\_numbers)))) \Rightarrow (\forall X2. (m2\_finseq\_2 X2 k1\_numbers \\
& (k1\_euclid X0)) \Rightarrow (k1\_pdiff\_7 X0 X1 X2 = k1\_partfun1 (k1\_euclid X0) \\
& (k1\_euclid np\_1) (k1\_euclid np\_1) k1\_numbers (k8\_pdiff\_1 X0 \\
& np\_1 (k3\_pdiff\_1 X0 X1) X2) (k1\_pdiff\_1 np\_1 np\_1)))) \tag{19}
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge (m2\_subset\_1 X0 k1\_numbers k5\_numbers)) \Rightarrow \\
& (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge (m2\_subset\_1 X1 k1\_numbers k5\_numbers)) \Rightarrow \\
& (\forall X2. \forall X3. ((v1\_funct\_1 X3) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k1\_euclid X0) (k1\_euclid X1)))) \Rightarrow ((r1\_tarski X2 \\
& (k1\_relset\_1 (k1\_euclid X0) X3)) \Rightarrow (\forall X4. ((v1\_funct\_1 X4) \wedge \\
& (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) (k9\_funct\_2 \\
& (k1\_euclid X0) (k1\_euclid X1)))))) \Rightarrow ((X4 = k1\_pdiff\_9 X0 X1 X2 X3) \Leftrightarrow \\
& ((k1\_relset\_1 (k1\_euclid X0) X4 = X2) \wedge (\forall X5. (m2\_finseq\_2 \\
& X5 k1\_numbers (k1\_euclid X0)) \Rightarrow ((X5 \in X2) \Rightarrow (k7\_partfun1 (k9\_funct\_2 \\
& (k1\_euclid X0) (k1\_euclid X1)) X4 X5 = k8\_pdiff\_1 X0 X1 X3 X5))))))))) \tag{20}
\end{aligned}$$

Assume the following.

$$\forall X0. (m1\_subset\_1 X0 k4\_ordinal1) \Rightarrow (v7\_ordinal1 X0) \tag{21}$$

**Theorem 1**

$$\begin{aligned} \forall X0.((\neg v1\_xboole\_0 X0) \wedge (m2\_subset\_1 X0 k1\_numbers k5\_numbers)) \Rightarrow \\ (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k1\_euclid X0))) \Rightarrow (\forall X2. \\ ((v1\_funct\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\ k1\_euclid X0) k1\_numbers)))) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge ( \\ m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k1\_euclid X0) (k1\_euclid \\ np\_1)))))) \Rightarrow (((r2\_relset\_1 (k1\_euclid X0) (k1\_euclid np\_1) ( \\ k3\_pdiff\_1 X0 X2) X3) \wedge (r1\_tarski X1 (k1\_relset\_1 (k1\_euclid X0) \\ X2)) \wedge (r2\_pdiff\_9 X1 X0 X2))) \Rightarrow ((r1\_pdiff\_6 X1 np\_1 X0 X3) \wedge (\forall X4. \\ (m2\_finseq\_2 X4 k1\_numbers (k1\_euclid X0)) \Rightarrow ((X4 \in X1) \Rightarrow (k7\_partfun1 \\ (k9\_funct\_2 (k1\_euclid X0) k1\_numbers) (k2\_pdiff\_9 X0 X1 X2) X4 = \\ k3\_relat\_1 (k7\_partfun1 (k9\_funct\_2 (k1\_euclid X0) (k1\_euclid \\ np\_1)) (k1\_pdiff\_9 X0 np\_1 X1 X3) X4) (k1\_pdiff\_1 np\_1 np\_1)))))))))) \end{aligned}$$