

t56\_rinfsup1  
(TMHv7LKfdsHD5x1Nj1y5o1Rg6ZbkCn9fvMq)

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Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_comseq\_2 : \iota \Rightarrow o$  be given. Let  $k4\_rinfsup1 : \iota \Rightarrow \iota$  be given. Let  $k3\_rinfsup1 : \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_rinfsup1 : \iota \Rightarrow \iota$  be given. Let  $k1\_seq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_rinfsup1 : \iota \Rightarrow \iota$  be given. Let  $v1\_seq\_2 : \iota \Rightarrow o$  be given. Let  $v8\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_seq\_2 : \iota \Rightarrow o$  be given. Let  $v7\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $np\_1 : \iota$  be given. Let  $np\_0 : \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_valued\_0 : \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $k2\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_membered : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0.(v1\_xboole\_0 X0) \Rightarrow (X0 = k1\_xboole\_0) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m2\_subset\_1 X0 k1\_numbers k5\_numbers) \Rightarrow (\forall X1. \\ & ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 \\ & X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow ((v1\_comseq\_2 \\ & X1) \Rightarrow (r1\_xxreal\_0 (k1\_rinfsup1 (k3\_rinfsup1 X1)) (k1\_seq\_1 (k4\_rinfsup1 \\ & X1) X0)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m2\_subset\_1 X0 k1\_numbers k5\_numbers) \Rightarrow (\forall X1. \\ & ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 \\ & X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow ((v1\_comseq\_2 \\ & X1) \Rightarrow (r1\_xxreal\_0 (k1\_seq\_1 (k3\_rinfsup1 X1) X0) (k2\_rinfsup1 \\ & (k4\_rinfsup1 X1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v1\_seq\_2 X0) \Rightarrow (v8\_valued\_0 (k4\_rinf sup1 X0))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v2\_seq\_2 X0) \Rightarrow (v7\_valued\_0 (k3\_rinf sup1 X0))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & (((v7\_valued\_0 X0) \Rightarrow (v2\_seq\_2 X0)) \wedge ((v8\_valued\_0 X0) \Rightarrow (v1\_seq\_2 \\ & X0))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0 np\_1) \wedge (m2\_subset\_1 np\_1 k1\_numbers k5\_numbers)) \wedge \\ & ((m1\_subset\_1 np\_1 k5\_numbers) \wedge (m1\_subset\_1 np\_1 k1\_numbers)) \end{aligned} \quad (7)$$

Assume the following.

$$v1\_xboole\_0 np\_0 \quad (8)$$

Assume the following.

$$\neg r1\_xxreal\_0 np\_1 np\_0 \quad (9)$$

Assume the following.

$$k6\_numbers = k1\_xboole\_0 \quad (10)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (11)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_valued\_0 X0))) \Rightarrow (k1\_seq\_1 X0 X1 = k1\_funct\_1 X0 X1) \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0. (v1\_xreal\_0 X0) \Rightarrow (\forall X1. (v1\_xreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xreal\_0 X2) \Rightarrow ((r1\_xxreal\_0 X0 X1) \Rightarrow ((r1\_xxreal\_0 X2 k6\_numbers) \vee \\ & ((\neg r1\_xxreal\_0 (k2\_xcmplx\_0 X1 X2) X0) \wedge (\neg r1\_xxreal\_0 X1 (k6\_xcmplx\_0 \\ & X0 X2))))))) \end{aligned} \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xreal\_0 X0)\wedge(v1\_xreal\_0 X1))\Rightarrow(v1\_xreal\_0 (k6\_xcmplx\_0 X0 X1)) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v3\_valued\_0 X0)))\Rightarrow(v1\_xreal\_0 (k1\_funct\_1 X0 X1)) \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xreal\_0 X0)\wedge(v1\_xreal\_0 X1))\Rightarrow(v1\_xreal\_0 (k2\_xcmplx\_0 X0 X1)) \quad (16)$$

Assume the following.

$$v3\_membered\ k1\_numbers \quad (17)$$

Assume the following.

$$\begin{aligned} &\forall X0.((v1\_funct\_1 X0)\wedge((v1\_funct\_2 X0\ k5\_numbers\ k1\_numbers)\wedge \\ &(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers))))))\Rightarrow \\ &((v1\_funct\_1 (k4\_rinfsup1 X0))\wedge((v1\_funct\_2 (k4\_rinfsup1 X0) \\ &k5\_numbers\ k1\_numbers)\wedge(m1\_subset\_1 (k4\_rinfsup1 X0) (k1\_zfmisc\_1 \\ &(k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers)))))) \end{aligned} \quad (18)$$

Assume the following.

$$\begin{aligned} &\forall X0.((v1\_funct\_1 X0)\wedge((v1\_funct\_2 X0\ k5\_numbers\ k1\_numbers)\wedge \\ &(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers))))))\Rightarrow \\ &((v1\_funct\_1 (k3\_rinfsup1 X0))\wedge((v1\_funct\_2 (k3\_rinfsup1 X0) \\ &k5\_numbers\ k1\_numbers)\wedge(m1\_subset\_1 (k3\_rinfsup1 X0) (k1\_zfmisc\_1 \\ &(k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers)))))) \end{aligned} \quad (19)$$

Assume the following.

$$\begin{aligned} &\forall X0.((v1\_funct\_1 X0)\wedge((v1\_funct\_2 X0\ k5\_numbers\ k1\_numbers)\wedge \\ &(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers))))))\Rightarrow \\ &(m1\_subset\_1 (k2\_rinfsup1 X0) k1\_numbers) \end{aligned} \quad (20)$$

Assume the following.

$$\begin{aligned} &\forall X0.((v1\_funct\_1 X0)\wedge((v1\_funct\_2 X0\ k5\_numbers\ k1\_numbers)\wedge \\ &(m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1\ k5\_numbers\ k1\_numbers))))))\Rightarrow \\ &(m1\_subset\_1 (k1\_rinfsup1 X0) k1\_numbers) \end{aligned} \quad (21)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v2\_seq\_2 X0) \Leftrightarrow (\exists X1.(v1\_xreal\_0 X1) \wedge (\forall X2.(m2\_subset\_1 \\ & X2 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xreal\_0 (k1\_seq\_1 X0 X2) X1)))) \end{aligned} \quad (22)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v1\_seq\_2 X0) \Leftrightarrow (\exists X1.(v1\_xreal\_0 X1) \wedge (\forall X2.(m2\_subset\_1 \\ & X2 k1\_numbers k5\_numbers) \Rightarrow (\neg r1\_xreal\_0 X1 (k1\_seq\_1 X0 X2)))))) \end{aligned} \quad (23)$$

Assume the following.

$$k1\_xboole\_0 = the (\lambda X0 : \iota.v1\_xboole\_0 X0) \quad (24)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v3\_valued\_0 \\ & X0) \wedge ((v1\_seq\_2 X0) \wedge (v2\_seq\_2 X0)))))) \Rightarrow ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 \\ & X0) \wedge ((v3\_valued\_0 X0) \wedge (v1\_comseq\_2 X0)))) \end{aligned} \quad (25)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k1\_numbers) \Rightarrow (v1\_xreal\_0 X0) \quad (26)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v3\_valued\_0 \\ & X0) \wedge (v1\_comseq\_2 X0)))) \Rightarrow ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge \\ & ((v3\_valued\_0 X0) \wedge ((v1\_seq\_2 X0) \wedge (v2\_seq\_2 X0)))))) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1))) \Rightarrow (v1\_relat\_1 X2) \end{aligned} \quad (28)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v3\_membered X1) \Rightarrow (\forall X2.(m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))) \Rightarrow (v3\_valued\_0 X2)) \end{aligned} \quad (29)$$

### Theorem 1

$$\begin{aligned} & \forall X0.((v1\_funct\_1 X0) \wedge ((v1\_funct\_2 X0 k5\_numbers k1\_numbers) \wedge \\ & (m1\_subset\_1 X0 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow \\ & ((v1\_comseq\_2 X0) \Rightarrow ((v1\_comseq\_2 (k4\_rinfsup1 X0) \wedge (v1\_comseq\_2 \\ & (k3\_rinfsup1 X0)))))) \end{aligned}$$