

t57\_cohsp\_1 (TM-  
PaEwh9SeRpMffXLDwveVSRH8GM3ub5JSj)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_classes1 : \iota \Rightarrow o$  be given. Let  $v1\_coh\_sp : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v10\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k11\_cohsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v7\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v6\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_cohsp\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_tarski : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $v9\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $v8\_cohsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cohsp\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. \neg (X0 \in X1) \wedge (v1\_xboole\_0 X1) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v1\_xboole\_0 X0) \wedge ((v1\_classes1 X0) \wedge (v1\_coh\_sp \\ & X0))) \Rightarrow (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge ((v1\_classes1 X1) \wedge (v1\_coh\_sp \\ & X1))) \Rightarrow (\forall X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (( \\ & v10\_cohsp\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\ & X1)))))) \Rightarrow (\forall X3. ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge \\ & ((v10\_cohsp\_1 X3) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))) \Rightarrow ((k11\_cohsp\_1 X0 X1 X2 = k11\_cohsp\_1 X0 X1 X3) \Rightarrow (r2\_funct\_2 \\ & X0 X1 X2 X3)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_classes1 X0) \wedge (v1\_coh\_sp \\
& X0))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_classes1 X1) \wedge (v1\_coh\_sp \\
& X1)))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (( \\
& v7\_cohsp\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow \\
& (\forall X3. \forall X4. (k2\_tarski X3 X4 \in X0) \Rightarrow (\forall X5. ((k4\_tarski \\
& X3 X5 \in k11\_cohsp\_1 X0 X1 X2) \wedge (k4\_tarski X4 X5 \in k11\_cohsp\_1 X0 X1 X2)) \Rightarrow \\
& (X3 = X4))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_classes1 X0) \wedge (v1\_coh\_sp \\
& X0))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_classes1 X1) \wedge (v1\_coh\_sp \\
& X1)))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (( \\
& v6\_cohsp\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow \\
& (\forall X3. \forall X4. (k2\_tarski X3 X4 \in X0) \Rightarrow (\forall X5. \forall X6. \\
& ((k4\_tarski X3 X5 \in k11\_cohsp\_1 X0 X1 X2) \wedge (k4\_tarski X4 X6 \in k11\_cohsp\_1 \\
& X0 X1 X2)) \Rightarrow (k2\_tarski X5 X6 \in X1))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. (((v1\_funct\_1 X2) \wedge \\
& ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0 X1)))))) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge (m1\_subset\_1 \\
& X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow ((r2\_funct\_2 X0 X1 X2 \\
& X3) \Leftrightarrow (X2 = X3))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\
& (((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 X0 X1)))))) \wedge (m1\_subset\_1 X3 X0)) \Rightarrow (k3\_funct\_2 X0 \\
& X1 X2 X3 = k1\_funct\_1 X2 X3)
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 \\
& X1) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 ( \\
& k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow (k11\_cohsp\_1 X0 X1 X2 = k10\_cohsp\_1 \\
& X2)
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_classes1 X0) \wedge (v1\_coh\_sp \\
& X0))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_classes1 X1) \wedge (v1\_coh\_sp \\
& X1))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (k3\_tarski X0) (k3\_tarski X1)))) \Rightarrow (\neg(\forall X3.\forall X4.(k2\_tarski \\
& X3 X4 \in X0) \Rightarrow (\forall X5.\forall X6.((k4\_tarski X3 X5 \in X2) \wedge (k4\_tarski \\
& X4 X6 \in X2)) \Rightarrow (k2\_tarski X5 X6 \in X1))) \wedge ((\forall X3.\forall X4.(k2\_tarski \\
& X3 X4 \in X0) \Rightarrow (\forall X5.((k4\_tarski X3 X5 \in X2) \wedge (k4\_tarski X4 X5 \in \\
& X2)) \Rightarrow (X3 = X4))) \wedge (\forall X3.((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 \\
& X0 X1) \wedge ((v10\_cohsp\_1 X3) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X0 X1)))))) \Rightarrow (\neg(X2 = k11\_cohsp\_1 X0 X1 X3) \wedge (\forall X4.(m1\_subset\_1 \\
& X4 X0) \Rightarrow (k3\_funct\_2 X0 X1 X3 X4 = k7\_relat\_1 X2 X4)))))))))
\end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 \\
& X1) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 ( \\
& k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow (m1\_subset\_1 (k11\_cohsp\_1 \\
& X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k3\_tarski X0) (k3\_tarski X1))))))
\end{aligned} \tag{9}$$

Assume the following.

$$\forall X0.\forall X1.k2\_tarski X0 X1 = k2\_tarski X1 X0 \tag{10}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v10\_cohsp\_1 X0))) \Rightarrow \\
& ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v4\_cohsp\_1 X0) \wedge (v9\_cohsp\_1 \\
& X0))))
\end{aligned} \tag{11}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v9\_cohsp\_1 X0))) \Rightarrow \\
& ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge ((v7\_cohsp\_1 X0) \wedge (v8\_cohsp\_1 \\
& X0))))
\end{aligned} \tag{12}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v4\_cohsp\_1 X0))) \Rightarrow \\
& ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v5\_cohsp\_1 X0)))
\end{aligned} \tag{13}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v5\_cohsp\_1 X0))) \Rightarrow \\
& ((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v6\_cohsp\_1 X0)))
\end{aligned} \tag{14}$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 X0 X1))) \Rightarrow (v1\_relat\_1 X2)
\end{aligned} \tag{15}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v1\_classes1 X0) \wedge (v1\_coh\_sp \\ & X0))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_classes1 X1) \wedge (v1\_coh\_sp \\ & X1))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (( \\ & v10\_cohsp\_1 X2) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 \\ & X1)))))) \Rightarrow (\forall X3.(m1\_subset\_1 X3 X0) \Rightarrow (k3\_funct\_2 X0 X1 X2 \\ & X3 = k7\_relat\_1 (k11\_cohsp\_1 X0 X1 X2) X3)))) \end{aligned}$$