

t57\_vfunct\_1 (TMY-  
wDx1UA1ug4HNNJ22498DEDvhtGpMmUt9)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v5\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v6\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v7\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v8\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_normsp\_0 : \iota \Rightarrow o$  be given. Let  $v4\_normsp\_0 : \iota \Rightarrow o$  be given. Let  $v2\_normsp\_1 : \iota \Rightarrow o$  be given. Let  $l1\_normsp\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_vfunct\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_vfunct\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. (\neg v1\_xboole\_0 X1) \Rightarrow (\forall X2. ((\neg v2\_struct\_0 \\
 & \quad X2) \wedge ((v13\_algstr\_0 X2) \wedge ((v2\_rlvect\_1 X2) \wedge ((v3\_rlvect\_1 X2) \wedge \\
 & \quad ((v4\_rlvect\_1 X2) \wedge ((v5\_rlvect\_1 X2) \wedge ((v6\_rlvect\_1 X2) \wedge ((v7\_rlvect\_1 \\
 & \quad X2) \wedge ((v8\_rlvect\_1 X2) \wedge ((v3\_normsp\_0 X2) \wedge ((v4\_normsp\_0 X2) \wedge \\
 & \quad ((v2\_normsp\_1 X2) \wedge (l1\_normsp\_1 X2)))))))))) \Rightarrow (\forall X3. \\
 & \quad ((v1\_funct\_1 X3) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 \\
 & \quad (u1\_struct\_0 X2)))))) \Rightarrow ((v3\_funct\_1 (k2\_partfun1 X1 (u1\_struct\_0 \\
 & \quad X2) X3 X0)) \Rightarrow (r1\_vfunct\_1 X1 X2 X3 X0)))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0. \forall X1. \forall X2. (\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3. \\
 & \quad ((\neg v2\_struct\_0 X3) \wedge ((v13\_algstr\_0 X3) \wedge ((v2\_rlvect\_1 X3) \wedge (( \\
 & \quad v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 X3) \wedge ((v5\_rlvect\_1 X3) \wedge ((v6\_rlvect\_1 \\
 & \quad X3) \wedge ((v7\_rlvect\_1 X3) \wedge ((v8\_rlvect\_1 X3) \wedge ((v3\_normsp\_0 X3) \wedge \\
 & \quad ((v4\_normsp\_0 X3) \wedge ((v2\_normsp\_1 X3) \wedge (l1\_normsp\_1 X3)))))))))) \Rightarrow \\
 & \quad (\forall X4. ((v1\_funct\_1 X4) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
 & \quad X2 (u1\_struct\_0 X3)))))) \Rightarrow (\forall X5. ((v1\_funct\_1 X5) \wedge (m1\_subset\_1 \\
 & \quad X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X2 (u1\_struct\_0 X3)))))) \Rightarrow (((r1\_vfunct\_1 \\
 & \quad X2 X3 X4 X0) \wedge (r1\_vfunct\_1 X2 X3 X5 X1)) \Rightarrow (r1\_vfunct\_1 X2 X3 (k2\_vfunct\_1 \\
 & \quad X2 X3 X4 X5) (k3\_xboole\_0 X0 X1))))))
 \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.\forall X1.k3\_xboole\_0 X0 X1 = k3\_xboole\_0 X1 X0 \quad (3)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3. \\ & ((\neg v2\_struct\_0 X3) \wedge ((v13\_algstr\_0 X3) \wedge ((v2\_rlvect\_1 X3) \wedge (( \\ & v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 X3) \wedge ((v5\_rlvect\_1 X3) \wedge ((v6\_rlvect\_1 \\ & X3) \wedge ((v7\_rlvect\_1 X3) \wedge ((v8\_rlvect\_1 X3) \wedge ((v3\_normsp\_0 X3) \wedge \\ & ((v4\_normsp\_0 X3) \wedge ((v2\_normsp\_1 X3) \wedge (l1\_normsp\_1 X3)))))))))) \Rightarrow \\ & (\forall X4.((v1\_funct\_1 X4) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X2 (u1\_struct\_0 X3)))))) \Rightarrow (\forall X5.((v1\_funct\_1 X5) \wedge (m1\_subset\_1 \\ & X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X2 (u1\_struct\_0 X3)))))) \Rightarrow (((r1\_vfunct\_1 \\ & X2 X3 X4 X0) \wedge (v3\_funct\_1 (k2\_partfun1 X2 (u1\_struct\_0 X3) X5 X1))) \Rightarrow \\ & ((r1\_vfunct\_1 X2 X3 (k2\_vfunct\_1 X2 X3 X4 X5) (k3\_xboole\_0 X0 X1)) \wedge \\ & (r1\_vfunct\_1 X2 X3 (k2\_vfunct\_1 X2 X3 X5 X4) (k3\_xboole\_0 X0 X1)))))) \end{aligned}$$