

t58_exchsort (TM-
MYYTp9iBMfpRNpW8YgsV6pbQkjX3hZkTw)

October 27, 2020

Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v3_orders_2 : \iota \Rightarrow o$ be given. Let $v4_orders_2 : \iota \Rightarrow o$ be given. Let $v5_orders_2 : \iota \Rightarrow o$ be given. Let $v16_waybel_0 : \iota \Rightarrow o$ be given. Let $l1_orders_2 : \iota \Rightarrow o$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v5_relat_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_exchsort : \iota \Rightarrow o$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_exchsort : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_funct_7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $r2_orders_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_ordinal6 : \iota \Rightarrow o$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v2_ordinal1 : \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} \forall X0.((v1_relat_1 X0) \wedge (v1_funct_1 X0)) \Rightarrow (\forall X1. \forall X2. \\ k9_xtuple_0 (k10_funct_7 X0 X1 X2) = k9_xtuple_0 X0) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. ((\neg v2_struct_0 X2) \wedge ((v3_orders_2 \\ X2) \wedge ((v4_orders_2 X2) \wedge ((v5_orders_2 X2) \wedge ((v16_waybel_0 X2) \wedge \\ (l1_orders_2 X2)))))) \Rightarrow (\forall X3. ((v1_relat_1 X3) \wedge ((v5_relat_1 \\ X3 (u1_struct_0 X2)) \wedge ((v1_funct_1 X3) \wedge (v1_exchsort X3)))) \Rightarrow (\\ (k4_tarski X0 X1 \in k6_exchsort X2 X3) \Leftrightarrow ((X0 \in k9_xtuple_0 X3) \wedge ((X1 \in \\ k9_xtuple_0 X3) \wedge ((X0 \in X1) \wedge (r2_orders_2 X2 (k7_partfun1 (u1_struct_0 \\ X2) X3 X1) (k7_partfun1 (u1_struct_0 X2) X3 X0)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. ((v1_relat_1 \\ X4) \wedge ((v5_relat_1 X4 X0) \wedge ((v1_funct_1 X4) \wedge (v1_exchsort X4)))) \Rightarrow \\ ((X1 \in k9_xtuple_0 X4) \Rightarrow ((X1 = X2) \vee ((X1 = X3) \vee (k7_partfun1 X0 (k10_funct_7 \\ X4 X2 X3) X1 = k7_partfun1 X0 X4 X1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((v1_relat_1 X3)\wedge \\ & ((v5_relat_1 X3 X0)\wedge((v1_funct_1 X3)\wedge(v1_exhsort X3))))\Rightarrow((\\ & (X1 \in k9_xtuple_0 X3)\wedge(X2 \in k9_xtuple_0 X3))\Rightarrow(k7_partfun1 X0 (k10_funct_7 \\ & X3 X1 X2) X2 = k7_partfun1 X0 X3 X1)) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1)\Rightarrow(m1_subset_1 X0 X1) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(v1_ordinal1 X2)\Rightarrow(((X0 \in X1)\wedge \\ & (X1 \in X2))\Rightarrow(X0 \in X2)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((v1_relat_1 X1)\wedge \\ & ((v5_relat_1 X1 X0)\wedge(v1_funct_1 X1)))\Rightarrow(v5_relat_1 (k10_funct_7 \\ & X1 X2 X3) X0) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge(v1_exhsort X0)))\Rightarrow \\ & (v1_ordinal6 (k9_xtuple_0 X0)) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((v1_relat_1 X0)\wedge(v1_funct_1 \\ & X0))\Rightarrow((v1_relat_1 (k10_funct_7 X0 X1 X2))\wedge(v1_funct_1 (k10_funct_7 \\ & X0 X1 X2))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((v1_relat_1 X0)\wedge((v1_funct_1 \\ & X0)\wedge(v1_exhsort X0)))\Rightarrow(v1_exhsort (k10_funct_7 X0 X1 X2)) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1_ordinal6 X0)\Rightarrow(\forall X1.(m1_subset_1 X1 X0)\Rightarrow \\ & (v3_ordinal1 X1)) \end{aligned} \quad (11)$$

Assume the following.

$$\forall X0.(v3_ordinal1 X0)\Rightarrow((v1_ordinal1 X0)\wedge(v2_ordinal1 X0)) \quad (12)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1)\Rightarrow(\neg X1 \in X0) \quad (13)$$

Theorem 1

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v2_struct_0 X3) \wedge \\ & ((v3_orders_2 X3) \wedge (v4_orders_2 X3) \wedge (v5_orders_2 X3) \wedge (v16_waybel_0 \\ & X3) \wedge (l1_orders_2 X3)))) \Rightarrow (\forall X4. ((v1_relat_1 X4) \wedge (v5_relat_1 \\ & X4 (u1_struct_0 X3)) \wedge (v1_funct_1 X4) \wedge (v1_exhsort X4))) \Rightarrow (\\ & (k4_tarski X0 X1 \in k6_exhsort X3 X4) \Rightarrow (((X1 \in X2) \wedge (k4_tarski X0 X2 \in \\ & k6_exhsort X3 X4)) \Leftrightarrow (k4_tarski X1 X2 \in k6_exhsort X3 (k10_funct_7 \\ & X4 X0 X1)))) \end{aligned}$$