# t58_member_1 <br> (TMbYGJc1HS7aHNsUU6df6tGvzq2xxmLv2sD) 

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Let v2_membered : $\iota \Rightarrow 0$ be given. Let r1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let $k 10 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 3 \_$xboole $\_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 8 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 4 \_\right. \text {member_1 }\right. \\
\left(k 3 \_x b o o l e \_0 X 0 X 1\right)=k 3 \_x b o o l e \_0\left(k 4 \_m e m b e r \_1 X 0\right)\left(k 4 \_m e m b e r \_1\right. \\
X 1))) \tag{1}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v2_membered $X 2) \Rightarrow\left(r 1 \_t a r s k i ~\left(k 8 \_m e m b e r \_1 ~ X 0\left(k 3 \_x b o o l e \_0 ~ X 1 ~ X 2\right)\right) ~\right.$
( $k 3$ _xboole_0 ( $k 8$ _member_1 X0 X1) (k8_member_1 X0 X2)) )) )
Assume the following.

$$
\begin{array}{r}
\forall X 0 . \forall X 1 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_ m e m b e r e d ~ \left(k 3 \_x b o o l e \_0\right.\right.  \tag{3}\\
X 1 X 0))
\end{array}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 4 \_m e m b e r \_1 X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 10 \_m e m b e r \_1\right.\right.  \tag{5}\\
\left.\left.X 0 X 1=k 8 \_m e m b e r \_1 X 0\left(k 4 \_m e m b e r \_1 X 1\right)\right)\right)
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v2_membered $X 2) \Rightarrow\left(r 1 \_t a r s k i\left(k 10 \_m e m b e r \_1 ~ X 0 ~\left(k 3 \_x b o o l e \_0 ~ X 1 ~\right.\right.\right.$
X2) $\left.\left.\left.)\left(k 3 \_x b o o l e \_0\left(k 10 \_m e m b e r \_1 X 0 X 1\right)\left(k 10 \_m e m b e r \_1 X 0 X 2\right)\right)\right)\right)\right)$

