

# t59\_ens\_1 (TMTXWkugHvH- szh7aZRHEDCY4WRTcWe9BheC)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v6\_cat\_1 : \iota \Rightarrow o$  be given. Let  $l1\_cat\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k16\_ens\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k11\_ens\_1 : \iota \Rightarrow \iota$  be given. Let  $k23\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_graph\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_graph\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k17\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_ens\_1 : \iota \Rightarrow \iota$  be given. Let  $l5\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_graph\_1 : \iota \Rightarrow o$  be given. Let  $k19\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\ & (((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1)))))) \wedge (m1\_subset\_1 X3 X0))) \Rightarrow (k3\_funct\_2 X0 \\ & X1 X2 X3 = k1\_funct\_1 X2 X3) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\ & X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))))) \Rightarrow (\forall X2. \\ & ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (u4\_struct\_0 X1) (k2\_ens\_1 ( \\ & k16\_ens\_1 X1))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u4\_struct\_0 \\ & X1) (k2\_ens\_1 (k16\_ens\_1 X1))))))) \Rightarrow ((r1\_tarski (k16\_ens\_1 X1) \\ & X0) \Rightarrow ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (u4\_struct\_0 X1) (u4\_struct\_0 \\ & (k11\_ens\_1 X0))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 ( \\ & u4\_struct\_0 X1) (u4\_struct\_0 (k11\_ens\_1 X0)))))))))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.((\neg v11\_struct\_0 X0) \wedge (l5\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 (u4\_struct\_0 X0)) \quad (3)$$

Assume the following.

$$\forall X0.(l1\_graph\_1 X0) \Rightarrow (l5\_struct\_0 X0) \quad (4)$$

Assume the following.

$$\forall X0.(l1\_cat\_1 X0) \Rightarrow (l1\_graph\_1 X0) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge \\ & ((v2\_cat\_1 X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge \\ & ((v6\_cat\_1 X0) \wedge (l1\_cat\_1 X0)))))))) \wedge (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0))) \Rightarrow ((v1\_funct\_1 (k19\_ens\_1 X0 X1)) \wedge ((v1\_funct\_2 (k19\_ens\_1 \\ & X0 X1) (u4\_struct\_0 X0) (k2\_ens\_1 (k16\_ens\_1 X0))) \wedge (m1\_subset\_1 \\ & (k19\_ens\_1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u4\_struct\_0 X0) ( \\ & k2\_ens\_1 (k16\_ens\_1 X0))))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\ & X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))))) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X1)) \Rightarrow ((r1\_tarski (k16\_ens\_1 X1) \\ & X0) \Rightarrow (k23\_ens\_1 X0 X1 X2 = k19\_ens\_1 X1 X2))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\ & X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\ & X0) \wedge (l1\_cat\_1 X0)))))))) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 \\ & X0)) \Rightarrow (\forall X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (u4\_struct\_0 \\ & X0) (k2\_ens\_1 (k16\_ens\_1 X0))) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 (u4\_struct\_0 X0) (k2\_ens\_1 (k16\_ens\_1 X0))))))) \Rightarrow \\ & ((X2 = k19\_ens\_1 X0 X1) \Leftrightarrow (\forall X3. (m1\_subset\_1 X3 (u4\_struct\_0 \\ & X0)) \Rightarrow (k3\_funct\_2 (u4\_struct\_0 X0) (k2\_ens\_1 (k16\_ens\_1 X0)) X2 \\ & X3 = k1\_domain\_1 (k2\_zfmisc\_1 (k1\_zfmisc\_1 (u4\_struct\_0 X0)) ( \\ & k1\_zfmisc\_1 (u4\_struct\_0 X0))) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_cat\_1 \\ & X0 X1 (k3\_graph\_1 X0 X3)) (k2\_cat\_1 X0 X1 (k4\_graph\_1 X0 X3)))) (k1\_domain\_1 \\ & (k1\_zfmisc\_1 (u4\_struct\_0 X0)) (k1\_zfmisc\_1 (u4\_struct\_0 X0)) \\ & (k2\_cat\_1 X0 X1 (k3\_graph\_1 X0 X3)) (k2\_cat\_1 X0 X1 (k4\_graph\_1 X0 \\ & X3))) (k17\_ens\_1 X0 X1 X3)))))) \end{aligned} \quad (8)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\ & X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))))) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X1)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\ & (u4\_struct\_0 X1)) \Rightarrow ((r1\_tarski (k16\_ens\_1 X1) X0) \Rightarrow (k3\_funct\_2 \\ & (u4\_struct\_0 X1) (u4\_struct\_0 (k11\_ens\_1 X0)) (k23\_ens\_1 X0 X1 \\ & X2) X3 = k1\_domain\_1 (k2\_zfmisc\_1 (k1\_zfmisc\_1 (u4\_struct\_0 X1)) \\ & (k1\_zfmisc\_1 (u4\_struct\_0 X1))) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_cat\_1 \\ X1 X2 (k3\_graph\_1 X1 X3)) (k2\_cat\_1 X1 X2 (k4\_graph\_1 X1 X3)))) (k1\_domain\_1 \\ & (k1\_zfmisc\_1 (u4\_struct\_0 X1)) (k1\_zfmisc\_1 (u4\_struct\_0 X1)) \\ & (k2\_cat\_1 X1 X2 (k3\_graph\_1 X1 X3)) (k2\_cat\_1 X1 X2 (k4\_graph\_1 X1 \\ & X3))) (k17\_ens\_1 X1 X2 X3)))))) \end{aligned}$$