

t59_uniroots

(TMJebsefEZUsWzdeB5fY3ShP5NujEouB6Scc)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m2_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $k5_numbers : \iota$ be given. Let $r1_nat_d : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $k1_complfld : \iota$ be given. Let $v1_int_1 : \iota \Rightarrow o$ be given. Let $k2_polynom4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_uniroots : \iota \Rightarrow \iota$ be given. Let $r1_int_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_int_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k21_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k13_newton : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $np_1 : \iota$ be given. Let $k4_uniroots : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_newton : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_xxreal_0 : \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $k1_newton : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_xcmplx_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_xreal_0 : \iota \Rightarrow o$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v6_membered : \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v1_xboole_0 X0) \wedge (m2_subset_1 X0 k1_numbers k5_numbers)) \Rightarrow \\
 & (\forall X1.((\neg v1_xboole_0 X1) \wedge (m2_subset_1 X1 k1_numbers k5_numbers)) \Rightarrow \\
 & (\forall X2.(v1_int_1 X2) \Rightarrow ((r1_nat_d X1 X0) \Rightarrow ((r1_xxreal_0 X0 \\
 & X1) \vee (\forall X3.(m1_subset_1 X3 (u1_struct_0 k1_complfld)) \Rightarrow \\
 & ((X3 = X2) \Rightarrow (\forall X4.(v1_int_1 X4) \Rightarrow (\forall X5.(v1_int_1 X5) \Rightarrow \\
 & (\forall X6.(v1_int_1 X6) \Rightarrow (((X4 = k2_polynom4 k1_complfld (k5_uniroots \\
 & X0) X3) \wedge ((X5 = k2_polynom4 k1_complfld (k4_uniroots X0 k1_complfld) \\
 & X3) \wedge (X6 = k2_polynom4 k1_complfld (k4_uniroots X1 k1_complfld \\
 & X3)))) \Rightarrow (r1_int_1 X4 (k5_int_1 X5 X6))))))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v1_xboole_0 X0) \wedge (m2_subset_1 X0 k1_numbers k5_numbers)) \Rightarrow \\
 & (\forall X1.(m1_subset_1 X1 (u1_struct_0 k1_complfld)) \Rightarrow ((v1_int_1 \\
 & X1) \Rightarrow (v1_int_1 (k2_polynom4 k1_complfld (k4_uniroots X0 k1_complfld) \\
 & X1))))
 \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v1_xboole_0 X0) \wedge (m2_subset_1 X0 k1_numbers k5_numbers)) \Rightarrow \\ (\forall X1.(m1_subset_1 X1 k1_numbers) \Rightarrow (\exists X2.(m1_subset_1 \\ X2 (u1_struct_0 k1_complfld) \wedge ((X2 = X1) \wedge (k2_polynom4 k1_complfld \\ (k4_uniroots X0 k1_complfld) X2 = k10_binop_2 (k2_newton X1 X0) \\ np_1)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1) \Rightarrow (m1_subset_1 X0 X1) \quad (4)$$

Assume the following.

$$\begin{aligned} ((v2_xreal_0 np_1) \wedge (m2_subset_1 np_1 k1_numbers k5_numbers)) \wedge \\ ((m1_subset_1 np_1 k5_numbers) \wedge (m1_subset_1 np_1 k1_numbers)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v1_xboole_0 X0) \wedge ((\neg v1_xboole_0 X1) \wedge \\ (m1_subset_1 X1 (k1_zfmisc_1 X0)))) \Rightarrow (\forall X2.(m2_subset_1 \\ X2 X0 X1) \Leftrightarrow (m1_subset_1 X2 X1)) \end{aligned} \quad (6)$$

Assume the following.

$$k5_numbers = k4_ordinal1 \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.((m1_subset_1 X0 k1_numbers) \wedge (v7_ordinal1 X1)) \Rightarrow (k2_newton X0 X1 = k1_newton X0 X1) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.((v1_int_1 X0) \wedge (v1_int_1 X1)) \Rightarrow (k21_binop_2 X0 X1 = k6_xcplx_0 X0 X1) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.((m1_subset_1 X0 k5_numbers) \wedge (m1_subset_1 X1 k5_numbers)) \Rightarrow (k13_newton X0 X1 = k1_newton X0 X1) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.((v1_xreal_0 X0) \wedge (v1_xreal_0 X1)) \Rightarrow (k10_binop_2 X0 X1 = k6_xcplx_0 X0 X1) \quad (11)$$

Assume the following.

$$(\neg v1_xboole_0 k4_ordinal1) \wedge (v3_ordinal1 k4_ordinal1) \quad (12)$$

Assume the following.

$$v6_membered\ k4_ordinal1 \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.((v1_int_1\ X0)\wedge(v7_ordinal1\ X1))\Rightarrow(v1_int_1\ (k1_newton\ X0\ X1)) \quad (14)$$

Assume the following.

$$\neg v1_xboole_0\ k1_numbers \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1_xboole_0\ X0)\wedge((\neg v1_xboole_0\ X1)\wedge(m1_subset_1\ X1\ (k1_zfmisc_1\ X0))))\Rightarrow(\forall X2.(m2_subset_1\ X2\ X0\ X1)\Rightarrow(m1_subset_1\ X2\ X0)) \quad (16)$$

Assume the following.

$$m1_subset_1\ k5_numbers\ (k1_zfmisc_1\ k1_numbers) \quad (17)$$

Assume the following.

$$\forall X0.(v7_ordinal1\ X0)\Leftrightarrow(X0 \in k4_ordinal1) \quad (18)$$

Assume the following.

$$\forall X0.(v1_int_1\ X0)\Rightarrow(v1_xreal_0\ X0) \quad (19)$$

Assume the following.

$$\forall X0.(v7_ordinal1\ X0)\Rightarrow(v1_int_1\ X0) \quad (20)$$

Assume the following.

$$\forall X0.(v6_membered\ X0)\Rightarrow(\forall X1.(m1_subset_1\ X1\ X0)\Rightarrow(v7_ordinal1\ X1)) \quad (21)$$

Theorem 1

$$\begin{aligned} & \forall X0.((\neg v1_xboole_0\ X0)\wedge(m2_subset_1\ X0\ k1_numbers\ k5_numbers))\Rightarrow \\ & (\forall X1.((\neg v1_xboole_0\ X1)\wedge(m2_subset_1\ X1\ k1_numbers\ k5_numbers))\Rightarrow \\ & (\forall X2.((\neg v1_xboole_0\ X2)\wedge(m2_subset_1\ X2\ k1_numbers\ k5_numbers))\Rightarrow \\ & ((r1_nat_d\ X1\ X0)\Rightarrow((r1_xreal_0\ X0\ X1)\vee(\forall X3.(m1_subset_1 \\ & X3\ (u1_struct_0\ k1_complfld))\Rightarrow((X3 = X2)\Rightarrow(\forall X4.(v1_int_1 \\ & X4)\Rightarrow((X4 = k2_polynom4\ k1_complfld\ (k5_uniroots\ X0)\ X3)\Rightarrow(r1_int_1 \\ & X4\ (k5_int_1\ (k21_binop_2\ (k13_newton\ X2\ X0)\ np_1)\ (k21_binop_2 \\ & (k13_newton\ X2\ X1)\ np_1)))))))))) \end{aligned}$$