

# t5\_hilbasis (TMN- mwnbM2bmHS41C42TMr7KT6NQnb74QpN1)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_poly : \iota \Rightarrow o$  be given. Let  $k5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_pre\_poly : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k11\_pre\_poly : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_relset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_valued\_0 : \iota \Rightarrow o$  be given. Let  $k7\_nat\_d : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_binop\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_valued\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (v1\_relat\_1 X1) \Rightarrow (k9\_xtuple\_0 (k5\_relat\_1 X1 X0) = k3\_xboole\_0 (k9\_xtuple\_0 X1) X0) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((v1\_relat\_1 X2) \wedge (v1\_funct\_1 X2)) \Rightarrow ((X0 \in k9\_xtuple\_0 (k5\_relat\_1 X2 X1)) \Rightarrow (k1\_funct\_1 (k5\_relat\_1 X2 X1) X0 = k1\_funct\_1 X2 X0)) \quad (2)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1. ((v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \Rightarrow (((k9\_xtuple\_0 X0 = k9\_xtuple\_0 X1) \wedge (\forall X2. (X2 \in k9\_xtuple\_0 X0) \Rightarrow (k1\_funct\_1 X0 X2 = k1\_funct\_1 X1 X2))) \Rightarrow (X0 = X1))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X1) \wedge (v4\_relat\_1 X1 X0)) \Rightarrow (k1\_relset\_1 X0 X1 = k9\_xtuple\_0 X1) \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow ((v1\_relat\_1 (k5\_relat\_1 X0 X1)) \wedge (v1\_funct\_1 (k5\_relat\_1 X0 X1))) \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge((v4\_relat\_1 \\ & X1 X0)\wedge((v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v4\_valued\_0 X1)))))\wedge \\ & ((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 X2)\wedge((v1\_partfun1 \\ & X2 X0)\wedge(v4\_valued\_0 X2))))))\Rightarrow((v1\_relat\_1 (k12\_pre\_poly X0 X1 \\ & X2))\wedge((v4\_relat\_1 (k12\_pre\_poly X0 X1 X2) X0)\wedge((v1\_funct\_1 (k12\_pre\_poly \\ & X0 X1 X2))\wedge((v1\_partfun1 (k12\_pre\_poly X0 X1 X2) X0)\wedge(v4\_valued\_0 \\ & (k12\_pre\_poly X0 X1 X2)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.(v1\_relat\_1 X0)\Rightarrow(v1\_relat\_1 (k5\_relat\_1 X0 X1)) \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge((v4\_relat\_1 \\ & X1 X0)\wedge((v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v1\_valued\_0 X1)))))\wedge \\ & ((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 X2)\wedge((v1\_partfun1 \\ & X2 X0)\wedge(v1\_valued\_0 X2))))))\Rightarrow((v1\_relat\_1 (k11\_pre\_poly X0 X1 \\ & X2))\wedge((v4\_relat\_1 (k11\_pre\_poly X0 X1 X2) X0)\wedge((v1\_funct\_1 (k11\_pre\_poly \\ & X0 X1 X2))\wedge(v1\_partfun1 (k11\_pre\_poly X0 X1 X2) X0)))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v4\_relat\_1 X1 X0)\wedge( \\ & (v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v4\_valued\_0 X1)))))\Rightarrow( \\ & \forall X2.((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 \\ & X2)\wedge((v1\_partfun1 X2 X0)\wedge(v4\_valued\_0 X2)))))\Rightarrow(\forall X3.( \\ & (v1\_relat\_1 X3)\wedge((v4\_relat\_1 X3 X0)\wedge((v1\_funct\_1 X3)\wedge(v1\_partfun1 \\ & X3 X0))))\Rightarrow((X3 = k12\_pre\_poly X0 X1 X2)\Leftrightarrow(\forall X4.k1\_funct\_1 \\ & X3 X4 = k7\_nat.d (k1\_funct\_1 X1 X4) (k1\_funct\_1 X2 X4)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v4\_relat\_1 X1 X0)\wedge( \\ & (v1\_funct\_1 X1)\wedge((v1\_partfun1 X1 X0)\wedge(v1\_valued\_0 X1)))))\Rightarrow( \\ & \forall X2.((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 \\ & X2)\wedge((v1\_partfun1 X2 X0)\wedge(v1\_valued\_0 X2)))))\Rightarrow(\forall X3.( \\ & (v1\_relat\_1 X3)\wedge((v4\_relat\_1 X3 X0)\wedge((v1\_funct\_1 X3)\wedge(v1\_partfun1 \\ & X3 X0))))\Rightarrow((X3 = k11\_pre\_poly X0 X1 X2)\Leftrightarrow(\forall X4.k1\_funct\_1 \\ & X3 X4 = k3\_binop-2 (k1\_funct\_1 X1 X4) (k1\_funct\_1 X2 X4)))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X1)\wedge(v4\_relat\_1 X1 X0))\Rightarrow( \\ (v1\_partfun1 X1 X0)\Leftrightarrow(k1\_relset\_1 X0 X1 = X0)) \quad (11)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge (v4\_valued\_0 X0)) \Rightarrow ((v1\_relat\_1 X0) \wedge (v3\_valued\_0 X0)) \quad (12)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge (v3\_valued\_0 X0)) \Rightarrow ((v1\_relat\_1 X0) \wedge (v1\_valued\_0 X0)) \quad (13)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 \\ & X2 X1) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_partfun1 X2 X1) \wedge ((v4\_valued\_0 X2) \wedge \\ & (v2\_pre\_poly X2)))))) \Rightarrow (\forall X3. ((v1\_relat\_1 X3) \wedge ((v4\_relat\_1 \\ & X3 X1) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_partfun1 X3 X1) \wedge ((v4\_valued\_0 X3) \wedge \\ & (v2\_pre\_poly X3)))))) \Rightarrow (\forall X4. ((v1\_relat\_1 X4) \wedge ((v4\_relat\_1 \\ & X4 X0) \wedge ((v1\_funct\_1 X4) \wedge ((v1\_partfun1 X4 X0) \wedge ((v4\_valued\_0 X4) \wedge \\ & (v2\_pre\_poly X4)))))) \Rightarrow (\forall X5. ((v1\_relat\_1 X5) \wedge ((v4\_relat\_1 \\ & X5 X0) \wedge ((v1\_funct\_1 X5) \wedge ((v1\_partfun1 X5 X0) \wedge ((v4\_valued\_0 X5) \wedge \\ & (v2\_pre\_poly X5)))))) \Rightarrow (((X4 = k5\_relat\_1 X2 X0) \wedge (X5 = k5\_relat\_1 \\ & X3 X0)) \Rightarrow ((k5\_relat\_1 (k12\_pre\_poly X1 X2 X3) X0 = k12\_pre\_poly X0 \\ & X4 X5) \wedge (k5\_relat\_1 (k11\_pre\_poly X1 X2 X3) X0 = k11\_pre\_poly X0 X4 \\ & X5)))))) \end{aligned}$$