

# t5\_integr15

(TMRvS4cLiJXMvHijkxBh1xLVrTa11LGzjEV)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v2\_measure5 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k1\_integral : \iota \Rightarrow \iota$  be given. Let  $m2\_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_seq\_2 : \iota \Rightarrow o$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_seq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_integra2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_integral : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k7\_integral : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k2\_integra2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_integr15 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v2\_measure5 X0) \wedge (m1\_subset\_1 \\ & X0 (k1\_zfmisc\_1 k1\_numbers)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge \\ & ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 ( \\ & k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow (\forall X2.(m1\_integral X2 X0) \Rightarrow \\ & (\forall X3.(m1\_integr15 X3 X0 X1 X2) \Rightarrow ((v2\_seq\_2 (k2\_partfun1 \\ & X0 k1\_numbers X1 X0)) \Rightarrow (r1\_xxreal\_0 (k7\_integral X0 X1 X2) (k1\_integr15 \\ & X0 X1 X2 X3)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 \\ & X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \end{aligned} \tag{2}$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \tag{3}$$

Assume the following.

$$(\neg v1\_xboole\_0 k4\_ordinal1) \wedge (v3\_ordinal1 k4\_ordinal1) \tag{4}$$

Assume the following.

$$\neg v1\_xboole\_0 \ k1\_numbers \quad (5)$$

Assume the following.

$$m1\_subset\_1 \ k5\_numbers \ (k1\_zfmisc\_1 \ k1\_numbers) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v1\_xboole\_0 \ X0)\wedge((v2\_measure5 \\ & \ X0)\wedge(m1\_subset\_1 \ X0 \ (k1\_zfmisc\_1 \ k1\_numbers))))\wedge(((v1\_funct\_1 \\ & \ X1)\wedge(m1\_subset\_1 \ X1 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ X0 \ k1\_numbers))))\wedge \\ & \ ((v1\_funct\_1 \ X2)\wedge((v1\_funct\_2 \ X2 \ k5\_numbers \ (k1\_integra1 \ X0))\wedge \\ & \ (m1\_subset\_1 \ X2 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ k5\_numbers \ (k1\_integra1 \\ & \ X0))))))\Rightarrow((v1\_funct\_1 \ (k4\_integra2 \ X0 \ X1 \ X2))\wedge((v1\_funct\_2 \\ & \ (k4\_integra2 \ X0 \ X1 \ X2) \ k5\_numbers \ k1\_numbers)\wedge(m1\_subset\_1 \ (k4\_integra2 \\ & \ X0 \ X1 \ X2) \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ k5\_numbers \ k1\_numbers)))))) \quad (7) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v1\_xboole\_0 \\ & \ X0)\wedge((v2\_measure5 \ X0)\wedge(m1\_subset\_1 \ X0 \ (k1\_zfmisc\_1 \ k1\_numbers))))\wedge \\ & \ (((v1\_funct\_1 \ X1)\wedge((v1\_funct\_2 \ X1 \ X0 \ k1\_numbers)\wedge(m1\_subset\_1 \\ & \ X1 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ X0 \ k1\_numbers))))\wedge(((v1\_funct\_1 \\ & \ X2)\wedge((v1\_funct\_2 \ X2 \ k5\_numbers \ (k1\_integra1 \ X0))\wedge(m1\_subset\_1 \\ & \ X2 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ k5\_numbers \ (k1\_integra1 \ X0))))))\wedge \\ & \ (m2\_integr15 \ X3 \ X0 \ X1 \ X2)))\Rightarrow((v1\_funct\_1 \ (k3\_integr15 \ X0 \ X1 \ X2 \\ & \ X3))\wedge((v1\_funct\_2 \ (k3\_integr15 \ X0 \ X1 \ X2 \ X3) \ k5\_numbers \ k1\_numbers)\wedge \\ & \ (m1\_subset\_1 \ (k3\_integr15 \ X0 \ X1 \ X2 \ X3) \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \\ & \ k5\_numbers \ k1\_numbers)))))) \quad (8) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v1\_xboole\_0 \ X0)\wedge((v2\_measure5 \\ & \ X0)\wedge(m1\_subset\_1 \ X0 \ (k1\_zfmisc\_1 \ k1\_numbers))))\wedge(((v1\_funct\_1 \\ & \ X1)\wedge((v1\_funct\_2 \ X1 \ k5\_numbers \ (k1\_integra1 \ X0))\wedge(m1\_subset\_1 \\ & \ X1 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ k5\_numbers \ (k1\_integra1 \ X0))))))\wedge \\ & \ (m1\_subset\_1 \ X2 \ k5\_numbers))\Rightarrow(m1\_integra1 \ (k2\_integra2 \ X0 \ X1 \\ & \ X2) \ X0) \quad (9) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.(((\neg v1\_xboole\_0 \\ & \ X0)\wedge((v2\_measure5 \ X0)\wedge(m1\_subset\_1 \ X0 \ (k1\_zfmisc\_1 \ k1\_numbers))))\wedge \\ & \ (((v1\_funct\_1 \ X1)\wedge((v1\_funct\_2 \ X1 \ X0 \ k1\_numbers)\wedge(m1\_subset\_1 \\ & \ X1 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ X0 \ k1\_numbers))))\wedge(((v1\_funct\_1 \\ & \ X2)\wedge((v1\_funct\_2 \ X2 \ k5\_numbers \ (k1\_integra1 \ X0))\wedge(m1\_subset\_1 \\ & \ X2 \ (k1\_zfmisc\_1 \ (k2\_zfmisc\_1 \ k5\_numbers \ (k1\_integra1 \ X0))))))\wedge \\ & \ ((m2\_integr15 \ X3 \ X0 \ X1 \ X2)\wedge(m1\_subset\_1 \ X4 \ k5\_numbers))))\Rightarrow(m1\_integr15 \\ & \ (k2\_integr15 \ X0 \ X1 \ X2 \ X3 \ X4) \ X0 \ X1 \ (k2\_integra2 \ X0 \ X2 \ X4)) \quad (10) \end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v2\_measure5 X0) \wedge (m1\_subset\_1 \\
& X0 (k1\_zfmisc\_1 k1\_numbers)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge \\
& ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 ( \\
& k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge \\
& ((v1\_funct\_2 X2 k5\_numbers (k1\_integral X0)) \wedge (m1\_subset\_1 X2 \\
& (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_integral X0)))))) \Rightarrow \\
& (\forall X3.(m2\_integr15 X3 X0 X1 X2) \Rightarrow (\forall X4.((v1\_funct\_1 \\
& X4) \wedge ((v1\_funct\_2 X4 k5\_numbers k1\_numbers) \wedge (m1\_subset\_1 X4 ( \\
& k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers k1\_numbers)))))) \Rightarrow ((X4 = k3\_integr15 \\
& X0 X1 X2 X3) \Leftrightarrow (\forall X5.(m2\_subset\_1 X5 k1\_numbers k5\_numbers) \Rightarrow \\
& (k1\_seq\_1 X4 X5 = k1\_integr15 X0 X1 (k2\_integra2 X0 X2 X5) (k2\_integr15 \\
& X0 X1 X2 X3 X5))))))
\end{aligned} \tag{11}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v2\_measure5 X0) \wedge (m1\_subset\_1 \\
& X0 (k1\_zfmisc\_1 k1\_numbers)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge \\
& (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 k1\_numbers)))) \Rightarrow \\
& (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (k1\_integral \\
& X0)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_integral \\
& X0)))))) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers \\
& k1\_numbers) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\
& k1\_numbers)))))) \Rightarrow ((X3 = k4\_integra2 X0 X1 X2) \Leftrightarrow (\forall X4.(m2\_subset\_1 \\
& X4 k1\_numbers k5\_numbers) \Rightarrow (k1\_seq\_1 X3 X4 = k7\_integral X0 X1 (k2\_integra2 \\
& X0 X2 X4))))))
\end{aligned} \tag{12}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v1\_xboole\_0 X0) \wedge ((v2\_measure5 X0) \wedge (m1\_subset\_1 \\
& X0 (k1\_zfmisc\_1 k1\_numbers)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge \\
& ((v1\_funct\_2 X1 X0 k1\_numbers) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 ( \\
& k2\_zfmisc\_1 X0 k1\_numbers)))))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge \\
& ((v1\_funct\_2 X2 k5\_numbers (k1\_integral X0)) \wedge (m1\_subset\_1 X2 \\
& (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (k1\_integral X0)))))) \Rightarrow \\
& (\forall X3.(m2\_integr15 X3 X0 X1 X2) \Rightarrow (\forall X4.(m2\_subset\_1 \\
& X4 k1\_numbers k5\_numbers) \Rightarrow ((v2\_seq\_2 (k2\_partfun1 X0 k1\_numbers \\
& X1 X0)) \Rightarrow (r1\_xreal\_0 (k1\_seq\_1 (k4\_integra2 X0 X1 X2) X4) (k1\_seq\_1 \\
& (k3\_integr15 X0 X1 X2 X3) X4))))))
\end{aligned}$$