

t5_nat_3

(TMYCr4ZqF4MESw1955CWkyhpUDpYpatjwfa)

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Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_int_2 : \iota \Rightarrow o$ be given. Let $r1_nat_d : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_newton : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_int_1 : \iota \Rightarrow o$ be given. Let $r1_int_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $np_1 : \iota$ be given. Let $r1_int_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_int_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0.(v7_ordinal1 X0) \Rightarrow (\forall X1.(v7_ordinal1 X1) \Rightarrow (\forall X2. \\ & (v7_ordinal1 X2) \Rightarrow (((r1_nat_d X0 X1) \wedge (r1_nat_d X1 X2)) \Rightarrow (r1_nat_d \\ & \quad X0 X2)))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v7_ordinal1 X0) \Rightarrow (\forall X1.(v1_int_1 X1) \Rightarrow (\forall X2. \\ & (v1_int_1 X2) \Rightarrow ((r1_int_2 X1 X2) \Rightarrow (r1_int_2 (k1_newton X1 X0) X2)))) \end{aligned} \tag{2}$$

Assume the following.

$$r1_xxreal_0 np_1 np_1 \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.((v7_ordinal1 X0) \wedge (v7_ordinal1 X1)) \Rightarrow (r1_nat_d X0 X0) \tag{4}$$

Assume the following.

$$\forall X0.\forall X1.((v1_int_1 X0) \wedge (v1_int_1 X1)) \Rightarrow (r1_int_1 X0 X0) \tag{5}$$

Assume the following.

$$\forall X0.\forall X1.((v7_ordinal1 X0) \wedge (v7_ordinal1 X1)) \Rightarrow (r1_nat_d X0 X1) \Leftrightarrow (r1_int_1 X0 X1) \tag{6}$$

Assume the following.

$$\forall X0.\forall X1.((v7_ordinal1 X0) \wedge (v7_ordinal1 X1)) \Rightarrow (v7_ordinal1 (k1_newton X0 X1)) \tag{7}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v7_ordinal1\ X0) \Rightarrow (\forall X1.(v7_ordinal1\ X1) \Rightarrow (\forall X2. \\ & (v7_ordinal1\ X2) \Rightarrow ((X2 = k3_int_2\ X0\ X1) \Leftrightarrow ((r1_nat_d\ X2\ X0) \wedge ((r1_nat_d \\ & X2\ X1) \wedge (\forall X3.(v7_ordinal1\ X3) \Rightarrow (((r1_nat_d\ X3\ X0) \wedge (r1_nat_d \\ & X3\ X1)) \Rightarrow (r1_nat_d\ X3\ X2)))))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v7_ordinal1\ X0) \Rightarrow ((v1_int_2\ X0) \Leftrightarrow ((\neg r1_xxreal_0\ X0 \\ & np_1) \wedge (\forall X1.(v7_ordinal1\ X1) \Rightarrow (\neg(r1_int_1\ X1\ X0) \wedge ((X1 \neq \\ & np_1) \wedge (X1 \neq X0)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v7_ordinal1\ X0) \Rightarrow (\forall X1.(v7_ordinal1\ X1) \Rightarrow ((\\ & r1_int_2\ X0\ X1) \Leftrightarrow (\forall X2.((v7_ordinal1\ X2) \wedge (v1_int_2\ X2)) \Rightarrow \\ & (\neg(r1_nat_d\ X2\ X0) \wedge (r1_nat_d\ X2\ X1)))))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.(v7_ordinal1\ X0) \Rightarrow (v1_int_1\ X0) \quad (11)$$

Theorem 1

$$\begin{aligned} & \forall X0.(v7_ordinal1\ X0) \Rightarrow (\forall X1.(v7_ordinal1\ X1) \Rightarrow (\forall X2. \\ & ((v7_ordinal1\ X2) \wedge (v1_int_2\ X2)) \Rightarrow ((r1_nat_d\ X2\ (k1_newton\ X0 \\ & X1)) \Rightarrow (r1_nat_d\ X2\ X0)))) \end{aligned}$$