

## t5\_zf\_lang

(TMN4gsMEgJiq3LvYZANw2jYbHo9YHBKmf63)

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Let  $v1\_zf\_lang : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v2\_zf\_lang : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zf\_lang : \iota$  be given. Let  $k4\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_zf\_lang : \iota \Rightarrow o$  be given. Let  $k5\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_zf\_lang : \iota \Rightarrow o$  be given. Let  $k6\_zf\_lang : \iota \Rightarrow \iota$  be given. Let  $v5\_zf\_lang : \iota \Rightarrow o$  be given. Let  $k7\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v6\_zf\_lang : \iota \Rightarrow o$  be given. Let  $k8\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ v6\_zf\_lang X0) \Leftrightarrow (\exists X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \wedge \\ (\exists X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\ X0 = k8\_zf\_lang X1 X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ v5\_zf\_lang X0) \Leftrightarrow (\exists X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 \\ k5\_numbers)) \wedge (\exists X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\ (X0 = k7\_zf\_lang X1 X2)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ v4\_zf\_lang X0) \Leftrightarrow (\exists X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 \\ k5\_numbers)) \wedge (X0 = k6\_zf\_lang X1))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ v3\_zf\_lang X0) \Leftrightarrow (\exists X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \wedge \\ (\exists X2.(m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \wedge (X0 = k5\_zf\_lang \\ X1 X2)))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ & v2\_zf\_lang X0) \Leftrightarrow (\exists X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \wedge \\ & (\exists X2.(m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \wedge (X0 = k4\_zf\_lang \\ & X1 X2)))) \end{aligned} \quad (5)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (( \\ & \neg(v2\_zf\_lang X0) \wedge (\forall X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \Rightarrow \\ & (\forall X2.(m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \Rightarrow (X0 \neq k4\_zf\_lang \\ & X1 X2)))) \wedge (((\exists X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \wedge \\ & (\exists X2.(m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \wedge (X0 = k4\_zf\_lang \\ & X1 X2))) \Rightarrow (v2\_zf\_lang X0)) \wedge ((\neg(v3\_zf\_lang X0) \wedge (\forall X1.(m2\_subset\_1 \\ & X1 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X2.(m2\_subset\_1 X2 k5\_numbers \\ & k1\_zf\_lang) \Rightarrow (X0 \neq k5\_zf\_lang X1 X2)))) \wedge (((\exists X1.(m2\_subset\_1 \\ & X1 k5\_numbers k1\_zf\_lang) \wedge (\exists X2.(m2\_subset\_1 X2 k5\_numbers \\ & k1\_zf\_lang) \wedge (X0 = k5\_zf\_lang X1 X2))) \Rightarrow (v3\_zf\_lang X0)) \wedge ((\neg(v4\_zf\_lang \\ & X0) \wedge (\forall X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow \\ & (X0 \neq k6\_zf\_lang X1))) \wedge (((\exists X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 \\ & X1 k5\_numbers)) \wedge (X0 = k6\_zf\_lang X1)) \Rightarrow (v4\_zf\_lang X0)) \wedge ((\neg(v5\_zf\_lang \\ & X0) \wedge (\forall X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow \\ & (\forall X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \Rightarrow ( \\ & X0 \neq k7\_zf\_lang X1 X2)))) \wedge (((\exists X1.((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 \\ & X1 k5\_numbers)) \wedge (\exists X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 \\ & k5\_numbers)) \wedge (X0 = k7\_zf\_lang X1 X2))) \Rightarrow (v5\_zf\_lang X0)) \wedge ((\neg( \\ & v6\_zf\_lang X0) \wedge (\forall X1.(m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \Rightarrow \\ & (\forall X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \Rightarrow ( \\ & X0 \neq k8\_zf\_lang X1 X2)))) \wedge (((\exists X1.(m2\_subset\_1 X1 k5\_numbers \\ & k1\_zf\_lang) \wedge (\exists X2.((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \wedge \\ & (X0 = k8\_zf\_lang X1 X2))) \Rightarrow (v6\_zf\_lang X0)))))))))) \end{aligned}$$