

t61_cat_1 (TMYPT-
DXTH1TARK7sbZg9A6bwS62ghzE5dRC)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v11_struct_0 : \iota \Rightarrow o$ be given. Let $v2_cat_1 : \iota \Rightarrow o$ be given. Let $v3_cat_1 : \iota \Rightarrow o$ be given. Let $v4_cat_1 : \iota \Rightarrow o$ be given. Let $v5_cat_1 : \iota \Rightarrow o$ be given. Let $v6_cat_1 : \iota \Rightarrow o$ be given. Let $l1_cat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u4_struct_0 : \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_cat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_graph_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_graph_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_cat_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m2_cat_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $u1_cat_1 : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_cat_1 \\
 & X0))) \Rightarrow ((v2_cat_1 X0) \Leftrightarrow (\forall X1.(m1_subset_1 X1 (u4_struct_0 \\
 & X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u4_struct_0 X0)) \Rightarrow ((k4_tarski \\
 & X2 X1 \in k9_xtuple_0 (u1_cat_1 X0)) \Leftrightarrow (k3_graph_1 X0 X2 = k4_graph_1 \\
 & X0 X1))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge ((v2_cat_1 \\
& X0) \wedge ((v3_cat_1 X0) \wedge ((v4_cat_1 X0) \wedge ((v5_cat_1 X0) \wedge ((v6_cat_1 \\
& X0) \wedge (l1_cat_1 X0))))))) \Rightarrow (\forall X1.((\neg v2_struct_0 X1) \wedge ((\\
& \neg v11_struct_0 X1) \wedge ((v2_cat_1 X1) \wedge ((v3_cat_1 X1) \wedge ((v4_cat_1 \\
& X1) \wedge ((v5_cat_1 X1) \wedge ((v6_cat_1 X1) \wedge (l1_cat_1 X1))))))) \Rightarrow (\forall X2. \\
& ((v1_funct_1 X2) \wedge ((v1_funct_2 X2 (u4_struct_0 X0) (u4_struct_0 \\
& X1)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 (u4_struct_0 \\
& X0) (u4_struct_0 X1)))))) \Rightarrow ((m2_cat_1 X2 X0 X1) \Leftrightarrow ((\forall X3.(\\
& m1_subset_1 X3 (u1_struct_0 X0)) \Rightarrow (\exists X4.(m1_subset_1 X4 \\
& (u1_struct_0 X1)) \wedge (k3_funct_2 (u4_struct_0 X0) (u4_struct_0 \\
& X1) X2 (k4_cat_1 X0 X3) = k4_cat_1 X1 X4))) \wedge ((\forall X3.(m1_subset_1 \\
& X3 (u4_struct_0 X0)) \Rightarrow ((k3_funct_2 (u4_struct_0 X0) (u4_struct_0 \\
& X1) X2 (k4_cat_1 X0 (k3_graph_1 X0 X3)) = k4_cat_1 X1 (k3_graph_1 \\
& X1 (k3_funct_2 (u4_struct_0 X0) (u4_struct_0 X1) X2 X3))) \wedge (k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 (k4_cat_1 X0 (k4_graph_1 X0 \\
& X3)) = k4_cat_1 X1 (k4_graph_1 X1 (k3_funct_2 (u4_struct_0 X0) (\\
& u4_struct_0 X1) X2 X3)))))) \wedge (\forall X3.(m1_subset_1 X3 (u4_struct_0 \\
& X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 (u4_struct_0 X0)) \Rightarrow ((k4_tarski \\
& X4 X3 \in k9_xtuple_0 (u1_cat_1 X0)) \Rightarrow (k3_funct_2 (u4_struct_0 X0) \\
& (u4_struct_0 X1) X2 (k1_cat_1 X0 X3 X4) = k1_cat_1 X1 (k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 X3) (k3_funct_2 (u4_struct_0 \\
& X0) (u4_struct_0 X1) X2 X4)))))))))
\end{aligned} \tag{2}$$

Theorem 1

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge ((v2_cat_1 \\
& X0) \wedge ((v3_cat_1 X0) \wedge ((v4_cat_1 X0) \wedge ((v5_cat_1 X0) \wedge ((v6_cat_1 \\
& X0) \wedge (l1_cat_1 X0))))))) \Rightarrow (\forall X1.((\neg v2_struct_0 X1) \wedge ((\\
& \neg v11_struct_0 X1) \wedge ((v2_cat_1 X1) \wedge ((v3_cat_1 X1) \wedge ((v4_cat_1 \\
& X1) \wedge ((v5_cat_1 X1) \wedge ((v6_cat_1 X1) \wedge (l1_cat_1 X1))))))) \Rightarrow (\forall X2. \\
& ((v1_funct_1 X2) \wedge ((v1_funct_2 X2 (u4_struct_0 X0) (u4_struct_0 \\
& X1)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 (u4_struct_0 \\
& X0) (u4_struct_0 X1)))))) \Rightarrow (((\forall X3.(m1_subset_1 X3 (u1_struct_0 \\
& X0)) \Rightarrow (\exists X4.(m1_subset_1 X4 (u1_struct_0 X1)) \wedge (k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 (k4_cat_1 X0 X3) = k4_cat_1 \\
& X1 X4))) \wedge ((\forall X3.(m1_subset_1 X3 (u4_struct_0 X0)) \Rightarrow ((k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 (k4_cat_1 X0 (k3_graph_1 X0 \\
& X3)) = k4_cat_1 X1 (k3_graph_1 X1 (k3_funct_2 (u4_struct_0 X0) (\\
& u4_struct_0 X1) X2 X3))) \wedge (k3_funct_2 (u4_struct_0 X0) (u4_struct_0 \\
& X1) X2 (k4_cat_1 X0 (k4_graph_1 X0 X3)) = k4_cat_1 X1 (k4_graph_1 \\
& X1 (k3_funct_2 (u4_struct_0 X0) (u4_struct_0 X1) X2 X3)))))) \wedge (\forall X3. \\
& (m1_subset_1 X3 (u4_struct_0 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 \\
& (u4_struct_0 X0)) \Rightarrow ((k3_graph_1 X0 X4 = k4_graph_1 X0 X3) \Rightarrow (k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 (k1_cat_1 X0 X3 X4) = k1_cat_1 \\
& X1 (k3_funct_2 (u4_struct_0 X0) (u4_struct_0 X1) X2 X3) (k3_funct_2 \\
& (u4_struct_0 X0) (u4_struct_0 X1) X2 X4)))))) \Rightarrow (m2_cat_1 X2 X0 \\
& X1))))
\end{aligned}$$