

## t67\_cat\_4

(TMYNKm8xDPnsQ4i7EwhTBAuM1noCBhtjrQZ)

October 27, 2020

Let  $v2\_struct.0 : \iota \Rightarrow o$  be given. Let  $v11\_struct.0 : \iota \Rightarrow o$  be given. Let  $v2\_cat.1 : \iota \Rightarrow o$  be given. Let  $v3\_cat.1 : \iota \Rightarrow o$  be given. Let  $v4\_cat.1 : \iota \Rightarrow o$  be given. Let  $v5\_cat.1 : \iota \Rightarrow o$  be given. Let  $v6\_cat.1 : \iota \Rightarrow o$  be given. Let  $v6\_cat.4 : \iota \Rightarrow o$  be given. Let  $l2\_cat.4 : \iota \Rightarrow o$  be given. Let  $m1\_subset.1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct.0 : \iota \Rightarrow \iota$  be given. Let  $k29\_cat.4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k20\_cat.4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k27\_cat.4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k28\_cat.4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_cat.1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_cat.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole.0 : \iota$  be given. Let  $l1\_cat.1 : \iota \Rightarrow o$  be given. Let  $m1\_cat.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_cat.1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct.0 X0) \wedge ((\neg v11\_struct.0 X0) \wedge ((v2\_cat.1 \\ & X0) \wedge ((v3\_cat.1 X0) \wedge ((v4\_cat.1 X0) \wedge ((v5\_cat.1 X0) \wedge ((v6\_cat.1 \\ & X0) \wedge ((v6\_cat.4 X0) \wedge (l2\_cat.4 X0)))))))))) \Rightarrow (\forall X1.(m1\_subset.1 \\ & X1 (u1\_struct.0 X0)) \Rightarrow (\forall X2.(m1\_subset.1 X2 (u1\_struct.0 \\ & X0)) \Rightarrow ((k2\_cat.1 X0 X1 (k20\_cat.4 X0 X1 X2) \neq k1\_xboole.0) \wedge (k2\_cat.1 \\ & X0 X2 (k20\_cat.4 X0 X1 X2) \neq k1\_xboole.0))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct.0 X0) \wedge ((\neg v11\_struct.0 X0) \wedge ((v2\_cat.1 \\ & X0) \wedge ((v3\_cat.1 X0) \wedge ((v4\_cat.1 X0) \wedge ((v5\_cat.1 X0) \wedge ((v6\_cat.1 \\ & X0) \wedge (l1\_cat.1 X0)))))))))) \Rightarrow (\forall X1.(m1\_subset.1 X1 (u1\_struct.0 \\ & X0)) \Rightarrow (\forall X2.(m1\_subset.1 X2 (u1\_struct.0 X0)) \Rightarrow (\forall X3. \\ & (m1\_cat.1 X3 X0 X1 X2) \Rightarrow ((k2\_cat.1 X0 X1 X2 \neq k1\_xboole.0) \Rightarrow (k5\_cat.1 \\ & X0 X1 X2 X2 X3 (k4\_cat.1 X0 X2) = X3)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0.(l2\_cat.4 X0) \Rightarrow (l1\_cat.1 X0) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct.0 X0) \wedge ((\neg v11\_struct.0 X0) \wedge \\ & ((v5\_cat.1 X0) \wedge ((v6\_cat.1 X0) \wedge (l1\_cat.1 X0)))))) \wedge (m1\_subset.1 \\ & X1 (u1\_struct.0 X0)) \Rightarrow (m1\_cat.1 (k4\_cat.1 X0 X1) X0 X1 X1) \end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 \\ & X0)\wedge((v2\_cat\_1 X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 \\ & X0)\wedge((v6\_cat\_1 X0)\wedge((v6\_cat\_4 X0)\wedge(l2\_cat\_4 X0))))))))))\wedge(( \\ & m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0)))\Rightarrow(m1\_cat\_1 (k28\_cat\_4 X0 X1 X2) X0 X2 (k20\_cat\_4 X0 X1 X2)) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 \\ & X0)\wedge((v2\_cat\_1 X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 \\ & X0)\wedge((v6\_cat\_1 X0)\wedge((v6\_cat\_4 X0)\wedge(l2\_cat\_4 X0))))))))))\wedge(( \\ & m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0)))\Rightarrow(m1\_cat\_1 (k27\_cat\_4 X0 X1 X2) X0 X1 (k20\_cat\_4 X0 X1 X2)) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 \\ & X0)\wedge(l2\_cat\_4 X0)))\wedge((m1\_subset\_1 X1 (u1\_struct\_0 X0))\wedge(m1\_subset\_1 \\ & X2 (u1\_struct\_0 X0))))\Rightarrow(m1\_subset\_1 (k20\_cat\_4 X0 X1 X2) (u1\_struct\_0 \\ & X0)) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge((v6\_cat\_4 X0)\wedge(l2\_cat\_4 X0))))))))))\Rightarrow(\forall X1.(m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0))\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0))\Rightarrow(\forall X4. \\ & (m1\_cat\_1 X4 X0 X1 X3)\Rightarrow(\forall X5.(m1\_cat\_1 X5 X0 X2 X3)\Rightarrow(\neg(k2\_cat\_1 \\ & X0 X1 X3\neq k1\_xboole\_0)\wedge((k2\_cat\_1 X0 X2 X3\neq k1\_xboole\_0)\wedge(\neg\forall X6. \\ & (m1\_cat\_1 X6 X0 (k20\_cat\_4 X0 X1 X2) X3)\Rightarrow((X6 = k29\_cat\_4 X0 X1 X2 X3 \\ & X4 X5)\Leftrightarrow((k5\_cat\_1 X0 X1 (k20\_cat\_4 X0 X1 X2) X3 (k27\_cat\_4 X0 X1 X2) \\ & X6 = X4)\wedge(k5\_cat\_1 X0 X2 (k20\_cat\_4 X0 X1 X2) X3 (k28\_cat\_4 X0 X1 X2) \\ & X6 = X5)))))))))) \end{aligned} \quad (8)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(((\neg v2\_struct\_0 X0)\wedge((\neg v11\_struct\_0 X0)\wedge((v2\_cat\_1 \\ & X0)\wedge((v3\_cat\_1 X0)\wedge((v4\_cat\_1 X0)\wedge((v5\_cat\_1 X0)\wedge((v6\_cat\_1 \\ & X0)\wedge((v6\_cat\_4 X0)\wedge(l2\_cat\_4 X0))))))))))\Rightarrow(\forall X1.(m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0))\Rightarrow(\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0))\Rightarrow(k29\_cat\_4 X0 X1 X2 (k20\_cat\_4 X0 X1 X2) (k27\_cat\_4 X0 X1 X2) \\ & (k28\_cat\_4 X0 X1 X2) = k4\_cat\_1 X0 (k20\_cat\_4 X0 X1 X2)))) \end{aligned}$$