

t6\_c0sp1

(TMM15TyowNHxY7Dko9aH2ZWG9fmrbLm38Mk)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v5\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v6\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v7\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v2\_funcsdom : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v5\_group\_1 : \iota \Rightarrow o$  be given. Let  $v1\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v3\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l1\_funcsdom : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v4\_c0sp1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_c0sp1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m2\_c0sp1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $g1\_funcsdom : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_c0sp1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_c0sp1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_c0sp1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_c0sp1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_c0sp1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k5\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_realset1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $u2\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_rlvect\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_c0sp1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l1\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v1\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let

$k1\_rlvect\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 X0) \Rightarrow \\
& \quad (\forall X2. (m1\_subset\_1 X2 X0) \Rightarrow (\forall X3. ((v1\_funct\_1 X3) \wedge \\
& \quad ((v1\_funct\_2 X3 (k2\_zfmisc\_1 X0 X0) X0) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0) X0)))))) \Rightarrow (\forall X4. ((v1\_funct\_1 \\
& \quad X4) \wedge ((v1\_funct\_2 X4 (k2\_zfmisc\_1 X0 X0) X0) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 (k2\_zfmisc\_1 X0 X0) X0)))))) \Rightarrow (\forall X5. ((\neg v2\_struct\_0 \\
& \quad X5) \wedge ((v13\_algstr\_0 X5) \wedge ((v2\_rlvect\_1 X5) \wedge ((v3\_rlvect\_1 X5) \wedge \\
& \quad ((v4\_rlvect\_1 X5) \wedge ((v5\_rlvect\_1 X5) \wedge ((v6\_rlvect\_1 X5) \wedge ((v7\_rlvect\_1 \\
& \quad X5) \wedge ((v2\_funcsdom X5) \wedge ((v3\_group\_1 X5) \wedge ((v5\_group\_1 X5) \wedge (( \\
& \quad v1\_vectsp\_1 X5) \wedge ((v3\_vectsp\_1 X5) \wedge (l1\_funcsdom X5)))))))))) \Rightarrow \\
& \quad (\forall X6. (m1\_subset\_1 X6 (k1\_zfmisc\_1 (u1\_struct\_0 X5))) \Rightarrow \\
& \quad (\forall X7. ((v1\_funct\_1 X7) \wedge ((v1\_funct\_2 X7 (k2\_zfmisc\_1 k1\_numbers \\
& \quad X0) X0) \wedge (m1\_subset\_1 X7 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
& \quad k1\_numbers X0) X0)))))) \Rightarrow (((X6 = X0) \wedge ((X1 = k4\_struct\_0 X5) \wedge ((X2 = \\
& \quad k5\_struct\_0 X5) \wedge ((X3 = k1\_realset1 (u1\_algstr\_0 X5) X6) \wedge ((X4 = \\
& \quad k1\_realset1 (u2\_algstr\_0 X5) X6) \wedge ((X7 = k2\_partfun1 (k2\_zfmisc\_1 \\
& \quad k1\_numbers (u1\_struct\_0 X5)) (u1\_struct\_0 X5) (u1\_rlvect\_1 X5) \\
& \quad (k2\_zfmisc\_1 k1\_numbers X6)) \wedge (v1\_c0sp1 X6 X5)))))) \Rightarrow (m2\_c0sp1 \\
& \quad (g1\_funcsdom X0 X4 X3 X7 X2 X1) X5))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. (l6\_algstr\_0 X0) \Rightarrow ((l2\_algstr\_0 X0) \wedge (l5\_algstr\_0 X0)) \tag{2}$$

Assume the following.

$$\forall X0. (l1\_funcsdom X0) \Rightarrow ((l6\_algstr\_0 X0) \wedge (l1\_rlvect\_1 X0)) \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge \\
& \quad ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 \\
& \quad X0) \wedge ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v2\_funcsdom X0) \wedge \\
& \quad ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ((v1\_vectsp\_1 X0) \wedge ((v3\_vectsp\_1 \\
& \quad X0) \wedge (l1\_funcsdom X0)))))))))) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
& \quad (u1\_struct\_0 X0)))) \Rightarrow ((v1\_funct\_1 (k5\_c0sp1 X0 X1)) \wedge ((v1\_funct\_2 \\
& \quad (k5\_c0sp1 X0 X1) (k2\_zfmisc\_1 k1\_numbers X1) X1) \wedge (m1\_subset\_1 \\
& \quad (k5\_c0sp1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 k1\_numbers \\
& \quad X1) X1))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge \\
& \quad (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow (m1\_subset\_1 \\
& \quad (k4\_c0sp1 X0 X1) X1)
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge \\ & ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))) \wedge ( \\ & m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (m1\_subset\_1 \\ & (k3\_c0sp1 X0 X1) X1) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow ((v1\_funct\_1 \\ & (k2\_c0sp1 X0 X1)) \wedge ((v1\_funct\_2 (k2\_c0sp1 X0 X1) (k2\_zfmisc\_1 X1 \\ & X1) X1) \wedge (m1\_subset\_1 (k2\_c0sp1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X1 X1) X1)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (l2\_algstr\_0 X0)) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow ((v1\_funct\_1 \\ & (k1\_c0sp1 X0 X1)) \wedge ((v1\_funct\_2 (k1\_c0sp1 X0 X1) (k2\_zfmisc\_1 X1 \\ & X1) X1) \wedge (m1\_subset\_1 (k1\_c0sp1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X1 X1) X1)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((v3\_c0sp1 X1 \\ & X0) \Rightarrow ((v1\_xboole\_0 X1) \vee (k4\_c0sp1 X0 X1 = k5\_struct\_0 X0)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v3\_rlvect\_1 \\ & X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))) \Rightarrow (\forall X1. (m1\_subset\_1 \\ & X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (((v1\_ideal\_1 X1 X0) \wedge (v1\_c0sp1 \\ & X1 X0)) \Rightarrow ((v1\_xboole\_0 X1) \vee (k3\_c0sp1 X0 X1 = k4\_struct\_0 X0)))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((v3\_c0sp1 X1 \\ & X0) \Rightarrow ((v1\_xboole\_0 X1) \vee (k2\_c0sp1 X0 X1 = k1\_realset1 (u2\_algstr\_0 \\ & X0) X1)))) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v2\_struct\_0 X0) \wedge (l2\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((v1\_ideal\_1 \\ & X1 X0) \Rightarrow ((v1\_xboole\_0 X1) \vee (k1\_c0sp1 X0 X1 = k1\_realset1 (u1\_algstr\_0 \\ & X0) X1)))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge \\
& ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v2\_funcsdom X0) \wedge ((v3\_group\_1 \\
& X0) \wedge ((v5\_group\_1 X0) \wedge ((v1\_vectsp\_1 X0) \wedge ((v3\_vectsp\_1 X0) \wedge ( \\
& l1\_funcsdom X0)))))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0))) \Rightarrow ((v4\_c0sp1 X1 X0) \Rightarrow ((v1\_xboole\_0 X1) \vee (k5\_c0sp1 \\
& X0 X1 = k2\_partfun1 (k2\_zfmisc\_1 k1\_numbers (u1\_struct\_0 X0)) ( \\
& u1\_struct\_0 X0) (u1\_rlvect\_1 X0) (k2\_zfmisc\_1 k1\_numbers X1))))))
\end{aligned} \tag{13}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge \\
& ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v2\_funcsdom X0) \wedge ((v3\_group\_1 \\
& X0) \wedge ((v5\_group\_1 X0) \wedge ((v1\_vectsp\_1 X0) \wedge ((v3\_vectsp\_1 X0) \wedge ( \\
& l1\_funcsdom X0)))))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0))) \Rightarrow ((v4\_c0sp1 X1 X0) \Leftrightarrow ((v1\_ideal\_1 X1 X0) \wedge ((v1\_c0sp1 \\
& X1 X0) \wedge (\forall X2.(m1\_subset\_1 X2 k1\_numbers) \Rightarrow (\forall X3.( \\
& m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow ((X3 \in X1) \Rightarrow (k1\_rlvect\_1 X0 X3 \\
& X2 \in X1))))))))))
\end{aligned} \tag{14}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v5\_rlvect\_1 X0) \wedge \\
& ((v6\_rlvect\_1 X0) \wedge ((v7\_rlvect\_1 X0) \wedge ((v2\_funcsdom X0) \wedge ((v3\_group\_1 \\
& X0) \wedge ((v5\_group\_1 X0) \wedge ((v1\_vectsp\_1 X0) \wedge ((v3\_vectsp\_1 X0) \wedge ( \\
& l1\_funcsdom X0)))))))))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\
& (u1\_struct\_0 X0))) \Rightarrow (((v4\_c0sp1 X1 X0) \wedge (v3\_c0sp1 X1 X0)) \Rightarrow ((v1\_xboole\_0 \\
& X1) \vee (m2\_c0sp1 (g1\_funcsdom X1 (k2\_c0sp1 X0 X1) (k1\_c0sp1 X0 X1) \\
& (k5\_c0sp1 X0 X1) (k4\_c0sp1 X0 X1) (k3\_c0sp1 X0 X1) X0))))))
\end{aligned}$$