

# t6\_homothet (TMTYwn- VjgFmM5n1ecUcsE1FFSrVK25wJPUi)

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Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_diraf : \iota \Rightarrow o$  be given. Let  $v2\_diraf : \iota \Rightarrow o$  be given. Let  $l1\_analoaf : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $r2\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_homothet : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_aff\_2 : \iota \Rightarrow o$  be given. Let  $v8\_transgeo : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_analoaf : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_aff\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1. (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. (m1\_subset\_1 \\
& \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. (m1\_subset\_1 X3 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X4. ((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (u1\_struct\_0 \\
& \quad X0) (u1\_struct\_0 X0)) \wedge ((v3\_funct\_2 X4 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& \quad X0)) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 \\
& \quad X0) (u1\_struct\_0 X0)))))) \Rightarrow ((v8\_transgeo X4 X0) \Rightarrow ((r1\_aff\_1 X0 \\
& \quad X1 X2 X3) \Leftrightarrow (r1\_aff\_1 X0 (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& \quad X0) X4 X1) (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X2) ( \\
& \quad k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X3))))))))) \Rightarrow
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 (u1\_struct\_0 X0) \\
& (u1\_struct\_0 X0)) \wedge ((v3\_funct\_2 X1 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0)) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0)))))) \Rightarrow ((v8\_transgeo X1 X0) \Leftrightarrow (\forall X2. \\
& (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow ((r2\_analoaf X0 \\
& X2 X3 X4 X5) \Leftrightarrow (r2\_analoaf X0 (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X1 X2) (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X1 X3) ( \\
& k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X1 X4) (k3\_funct\_2 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) X1 X5))))))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\
& (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\
& (u1\_struct\_0 X0)) \Rightarrow (((r1\_aff\_1 X0 X1 X2 X4) \wedge ((r1\_aff\_1 X0 X1 X3 X5) \wedge \\
& ((r1\_aff\_1 X0 X1 X3 X6) \wedge ((r2\_analoaf X0 X2 X3 X4 X5) \wedge (r2\_analoaf \\
& X0 X2 X3 X4 X6)))))) \Rightarrow ((r1\_aff\_1 X0 X1 X2 X3) \vee (X5 = X6))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\
& (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\
& (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (((r2\_aff\_1 X0 X1 X2 X6) \wedge ((r1\_aff\_1 \\
& X0 X3 X4 X1) \wedge ((r1\_aff\_1 X0 X3 X5 X2) \wedge ((X3 \in X6) \wedge (X4 = X5)))))) \Rightarrow ((X4 \in \\
& X6) \vee (X1 = X2))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow \\
& (\neg(X1 \in X4) \wedge ((\neg X2 \in X4) \wedge ((r2\_aff\_1 X0 X2 X3 X4) \wedge ((X2 \neq X3) \wedge (r1\_aff\_1 \\
& \quad X0 X1 X2 X3)))))))))
\end{aligned} \tag{6}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge (l1\_analoaf X0))) \Rightarrow \\
& (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& \quad X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\
& \quad ((v1\_aff\_1 X5 X0) \wedge (m1\_subset\_1 X5 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))) \Rightarrow \\
& (((r2\_aff\_1 X0 X1 X2 X5) \wedge (r2\_aff\_1 X0 X3 X4 X5)) \Rightarrow (r2\_analoaf X0 X1 \\
& \quad X2 X3 X4)))))))))
\end{aligned} \tag{7}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& \quad (l1\_analoaf X0)))) \Rightarrow ((v7\_aff\_2 X0) \Leftrightarrow (\forall X1.(m1\_subset\_1 \\
& \quad X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& \quad X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5. \\
& \quad (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\
& \quad (u1\_struct\_0 X0)) \Rightarrow (\forall X7.(m1\_subset\_1 X7 (u1\_struct\_0 X0)) \Rightarrow \\
& (\forall X8.(m1\_subset\_1 X8 (u1\_struct\_0 X0)) \Rightarrow (((X1 \in X2) \wedge ((X3 \in \\
& \quad X2) \wedge ((X4 \in X2) \wedge ((v1\_aff\_1 X2 X0) \wedge ((r1\_aff\_1 X0 X1 X5 X7) \wedge ((r1\_aff\_1 \\
& \quad X0 X1 X6 X8) \wedge ((r2\_aff\_1 X0 X5 X6 X2) \wedge ((r2\_aff\_1 X0 X7 X8 X2) \wedge (r2\_analoaf \\
& \quad X0 X5 X3 X7 X4))))))))) \Rightarrow ((X5 \in X2) \vee (r2\_analoaf X0 X6 X3 X8 X4)))))))))
\end{aligned} \tag{8}$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 (u1\_struct\_0 X0)) \tag{9}$$

Assume the following.

$$\forall X0.(l1\_analoaf X0) \Rightarrow (l1\_struct\_0 X0) \tag{10}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\
& (((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\
& \quad (k2\_zfmisc\_1 X0 X1)))) \wedge (m1\_subset\_1 X3 X0))) \Rightarrow (m1\_subset\_1 ( \\
& \quad k3\_funct\_2 X0 X1 X2 X3) X1)
\end{aligned} \tag{11}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& (l1\_analoaf X0)))) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 \\
& X1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge ((v3\_funct\_2 X1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0)))))) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((r1\_homothet X0 X1 X2) \Leftrightarrow (( \\
& v8\_transgeo X1 X0) \wedge ((v1\_aff\_1 X2 X0) \wedge ((\forall X3.(m1\_subset\_1 \\
& X3 (u1\_struct\_0 X0)) \Rightarrow ((X3 \in X2) \Rightarrow (k3\_funct\_2 (u1\_struct\_0 X0) ( \\
& u1\_struct\_0 X0) X1 X3 = X3))) \wedge (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& X0)) \Rightarrow (r2\_aff\_1 X0 X3 (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X1 X3) X2)))))))))
\end{aligned} \tag{12}$$

Assume the following.

$$\forall X0.(l1\_struct\_0 X0) \Rightarrow ((\neg v7\_struct\_0 X0) \Rightarrow (\neg v2\_struct\_0 X0)) \tag{13}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v7\_struct\_0 X0) \wedge ((v1\_diraf X0) \wedge ((v2\_diraf X0) \wedge \\
& (l1\_analoaf X0)))) \Rightarrow ((\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 \\
& X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\neg (r2\_aff\_1 \\
& X0 X1 X2 X3) \wedge ((\neg X1 \in X3) \wedge (\forall X4.((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 \\
& X4 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \wedge ((v3\_funct\_2 X4 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0)))))) \Rightarrow (\neg (r1\_homothet X0 X4 \\
& X3) \wedge (k3\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X0) X4 X1 = X2)))))) \Rightarrow \\
& (v7\_aff\_2 X0))
\end{aligned}$$