

# t74\_quatern3 (TMKJbJbuXEzaudwM- RKk7VEP4jVHG1fcLqSU)

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Let  $v1\_quaterni : \iota \Rightarrow o$  be given. Let  $k6\_quatern2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_quaterni : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k17\_quaterni : \iota \Rightarrow \iota$  be given. Let  $k18\_quaterni : \iota \Rightarrow \iota$  be given. Let  $k19\_quaterni : \iota \Rightarrow \iota$  be given. Let  $k20\_quaterni : \iota \Rightarrow \iota$  be given. Let  $k5\_square\_1 : \iota \Rightarrow \iota$  be given. Let  $k3\_quatern2 : \iota \Rightarrow \iota$  be given. Let  $k9\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_quaterni : \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.(v1\_quaterni X0) \Rightarrow (\forall X1.(v1\_quaterni X1) \Rightarrow (( \\
 & k17\_quaterni (k6\_quatern2 X0 X1) = k10\_real\_1 (k7\_real\_1 (k7\_real\_1 \\
 & (k7\_real\_1 (k8\_real\_1 (k17\_quaterni X1) (k17\_quaterni X0)) (k8\_real\_1 \\
 & (k18\_quaterni X0) (k18\_quaterni X1))) (k8\_real\_1 (k19\_quaterni \\
 & X1) (k19\_quaterni X0))) (k8\_real\_1 (k20\_quaterni X1) (k20\_quaterni \\
 & X0))) (k5\_square\_1 (k3\_quatern2 X1))) \wedge ((k18\_quaterni (k6\_quatern2 \\
 & X0 X1) = k10\_real\_1 (k7\_real\_1 (k9\_real\_1 (k9\_real\_1 (k8\_real\_1 \\
 & (k17\_quaterni X1) (k18\_quaterni X0)) (k8\_real\_1 (k18\_quaterni \\
 & X1) (k17\_quaterni X0))) (k8\_real\_1 (k19\_quaterni X1) (k20\_quaterni \\
 & X0))) (k8\_real\_1 (k20\_quaterni X1) (k19\_quaterni X0))) (k5\_square\_1 \\
 & (k3\_quatern2 X1))) \wedge ((k19\_quaterni (k6\_quatern2 X0 X1) = k10\_real\_1 \\
 & (k9\_real\_1 (k9\_real\_1 (k7\_real\_1 (k8\_real\_1 (k17\_quaterni X1) \\
 & (k19\_quaterni X0)) (k8\_real\_1 (k18\_quaterni X1) (k20\_quaterni \\
 & X0))) (k8\_real\_1 (k19\_quaterni X1) (k17\_quaterni X0))) (k8\_real\_1 \\
 & (k20\_quaterni X1) (k18\_quaterni X0))) (k5\_square\_1 (k3\_quatern2 \\
 & X1))) \wedge (k20\_quaterni (k6\_quatern2 X0 X1) = k10\_real\_1 (k9\_real\_1 \\
 & (k7\_real\_1 (k9\_real\_1 (k8\_real\_1 (k17\_quaterni X1) (k20\_quaterni \\
 & X0)) (k8\_real\_1 (k18\_quaterni X1) (k19\_quaterni X0))) (k8\_real\_1 \\
 & (k19\_quaterni X1) (k18\_quaterni X0))) (k8\_real\_1 (k20\_quaterni \\
 & X1) (k17\_quaterni X0))) (k5\_square\_1 (k3\_quatern2 X1))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0.(v1\_quaterni X0) \Rightarrow (X0 = k6\_quaterni (k17\_quaterni X0) \\
 (k18\_quaterni X0) (k19\_quaterni X0) (k20\_quaterni X0)) \tag{2}$$

Assume the following.

$$\forall X0.\forall X1.((v1\_quaterni\ X0)\wedge(v1\_quaterni\ X1))\Rightarrow(m1\_subset\_1\ (k6\_quatern2\ X0\ X1)\ k1\_quaterni) \quad (3)$$

Assume the following.

$$\forall X0.(m1\_subset\_1\ X0\ k1\_quaterni)\Rightarrow(v1\_quaterni\ X0) \quad (4)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(v1\_quaterni\ X0)\Rightarrow(\forall X1.(v1\_quaterni\ X1)\Rightarrow(k6\_quatern2 \\ & X0\ X1 = k6\_quaterni\ (k10\_real\_1\ (k7\_real\_1\ (k7\_real\_1\ (k7\_real\_1 \\ & (k8\_real\_1\ (k17\_quaterni\ X1)\ (k17\_quaterni\ X0))\ (k8\_real\_1\ (k18\_quaterni \\ & X0)\ (k18\_quaterni\ X1)))\ (k8\_real\_1\ (k19\_quaterni\ X1)\ (k19\_quaterni \\ & X0)))\ (k8\_real\_1\ (k20\_quaterni\ X1)\ (k20\_quaterni\ X0)))\ (k5\_square\_1 \\ & (k3\_quatern2\ X1)))\ (k10\_real\_1\ (k7\_real\_1\ (k9\_real\_1\ (k9\_real\_1 \\ & (k8\_real\_1\ (k17\_quaterni\ X1)\ (k18\_quaterni\ X0))\ (k8\_real\_1\ (k18\_quaterni \\ & X1)\ (k17\_quaterni\ X0)))\ (k8\_real\_1\ (k19\_quaterni\ X1)\ (k20\_quaterni \\ & X0)))\ (k8\_real\_1\ (k20\_quaterni\ X1)\ (k19\_quaterni\ X0)))\ (k5\_square\_1 \\ & (k3\_quatern2\ X1)))\ (k10\_real\_1\ (k9\_real\_1\ (k9\_real\_1\ (k7\_real\_1 \\ & (k8\_real\_1\ (k17\_quaterni\ X1)\ (k19\_quaterni\ X0))\ (k8\_real\_1\ (k18\_quaterni \\ & X1)\ (k20\_quaterni\ X0)))\ (k8\_real\_1\ (k19\_quaterni\ X1)\ (k17\_quaterni \\ & X0)))\ (k8\_real\_1\ (k20\_quaterni\ X1)\ (k18\_quaterni\ X0)))\ (k5\_square\_1 \\ & (k3\_quatern2\ X1)))\ (k10\_real\_1\ (k9\_real\_1\ (k7\_real\_1\ (k9\_real\_1 \\ & (k8\_real\_1\ (k17\_quaterni\ X1)\ (k20\_quaterni\ X0))\ (k8\_real\_1\ (k18\_quaterni \\ & X1)\ (k19\_quaterni\ X0)))\ (k8\_real\_1\ (k19\_quaterni\ X1)\ (k18\_quaterni \\ & X0)))\ (k8\_real\_1\ (k20\_quaterni\ X1)\ (k17\_quaterni\ X0)))\ (k5\_square\_1 \\ & (k3\_quatern2\ X1)))))) \end{aligned}$$