

## t75\_card\_2

(TMP9FpogcYn2azdjDBhMwrU31jksv7HGGuH)

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Let  $v1\_card\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k1\_card\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v4\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k11\_ordinal2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_ordinal1 : \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k10\_ordinal2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_card\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $np\_2 : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_wellord2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow ((v4\_ordinal1 X0) \Rightarrow (k11\_ordinal2 X0 (k1\_ordinal1 np\_1) = X0)) \quad (1)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow ((k11\_ordinal2 np\_1 X0 = X0) \wedge (k11\_ordinal2 X0 np\_1 = X0)) \quad (2)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (k11\_ordinal2 (k1\_ordinal1 X0) X1 = k10\_ordinal2 (k11\_ordinal2 X0 X1) X1)) \quad (3)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (k1\_card\_1 (k11\_ordinal2 X0 X1) = k2\_card\_2 (k1\_card\_1 X0) (k1\_card\_1 X1))) \quad (4)$$

Assume the following.

$$((v2\_xxreal\_0 np\_2) \wedge (m2\_subset\_1 np\_2 k1\_numbers k5\_numbers)) \wedge ((m1\_subset\_1 np\_2 k5\_numbers) \wedge (m1\_subset\_1 np\_2 k1\_numbers)) \quad (5)$$

Assume the following.

$$((v2\_xxreal\_0 np\_1) \wedge (m2\_subset\_1 np\_1 k1\_numbers k5\_numbers)) \wedge ((m1\_subset\_1 np\_1 k5\_numbers) \wedge (m1\_subset\_1 np\_1 k1\_numbers)) \quad (6)$$

Assume the following.

$$k1\_ordinal1 \ np_{-1} = np_{-2} \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.r2\_wellord2 \ X0 \ X0 \quad (8)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (9)$$

Assume the following.

$$(\neg v1\_xboole\_0 \ k4\_ordinal1) \wedge (v3\_ordinal1 \ k4\_ordinal1) \quad (10)$$

Assume the following.

$$\forall X0.v1\_card\_1 \ (k1\_card\_1 \ X0) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.(v1\_card\_1 \ X1) \Rightarrow ((X1 = k1\_card\_1 \ X0) \Leftrightarrow (r2\_wellord2 \ X0 \ X1)) \quad (12)$$

Assume the following.

$$\forall X0.k1\_ordinal1 \ X0 = k2\_xboole\_0 \ X0 \ (k1\_tarski \ X0) \quad (13)$$

Assume the following.

$$\forall X0.(v1\_card\_1 \ X0) \Rightarrow (\forall X1.(v1\_card\_1 \ X1) \Rightarrow (k1\_card\_2 \ X0 \ X1 = k1\_card\_1 \ (k10\_ordinal2 \ X0 \ X1))) \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_card\_1 \ X0) \wedge (v1\_card\_1 \ X1)) \Rightarrow (k2\_card\_2 \ X0 \ X1 = k2\_card\_2 \ X1 \ X0) \quad (15)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 \ X0) \Rightarrow (\forall X1.(m1\_subset\_1 \ X1 \ X0) \Rightarrow (v3\_ordinal1 \ X1)) \quad (16)$$

Assume the following.

$$\forall X0.((\neg v1\_finset\_1 \ X0) \wedge (v1\_card\_1 \ X0)) \Rightarrow ((v4\_ordinal1 \ X0) \wedge (v1\_card\_1 \ X0)) \quad (17)$$

Assume the following.

$$\forall X0.(v1\_card\_1 \ X0) \Rightarrow (v3\_ordinal1 \ X0) \quad (18)$$

**Theorem 1**  $\forall X0.(v1\_card\_1 \ X0) \Rightarrow ((\neg v1\_finset\_1 \ X0) \Rightarrow (k1\_card\_2 \ X0 \ X0 = X0)).$