# t77_member_1 (TMaUZajHuMKZ3pNXDC74xvmb9y5EPfZa62J) 

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Let $v 1 \_x c m p l x \_0: \iota \Rightarrow o$ be given. Let $k$ 11_member_1: $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k2_tarski : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k1_tarski : $\iota \Rightarrow \iota$ be given. Let k4_binop_2 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v 1 \_$membered $: \iota \Rightarrow o$ be given. Let k9_member_1: $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 2_{\_} x$ boole_0 $: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5$ _member_ $1: \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_ x \text { cmplx_0 X1) } \Rightarrow \left(k 11 \_m e m b e r \_1\right.\right.\right. \\
\left.\left.\left(k 1 \_t a r s k i X 0\right)\left(k 1_{1} \text { tarski } X 1\right)=k 1 \_t a r s k i\left(k 4 \_b i n o p \_2 X 0 X 1\right)\right)\right) \tag{1}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 9 \_m e m b e r \_1 ~ X 0\left(k 2 \_x b o o l e \_0 X 1 X 2\right)=k 2 \_x b o o l e \_0\right.$
(k9_member_1 X0 X1) (k9_member_1 X0 X2))))
Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 . k 2 \_t a r s k i ~ X 0 X 1=k 2 \_x b o o l e \_0\left(k 1 \_t a r s k i\right. \\
X 0)\left(k 1 \_t a r s k i ~ X 1\right) \tag{3}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_x \text { cmplx_0 } X 0\right) \wedge\left(v 1 \_x c m p l x \_0 X 1\right)\right) \Rightarrow(  \tag{5}\\
\left.v 1 \_m e m b e r e d ~\left(k 2 \_t a r s k i ~ X 0 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{6}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_ \text {membered } X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1 X 0\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right) \tag{7}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow(  \tag{8}\\
\left.k 9 \_m e m b e r \_1 X 0 X 1=k 9 \_m e m b e r \_1 X 1 X 0\right)
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 2 \_ \text {tarski } X 0 X 1=k 2 \_ \text {tarski } X 1 X 0 \tag{9}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 11 \_m e m b e r \_1\left(k 2 \_t a r s k i X 0 X 1\right)\left(k 1 \_t a r s k i ~ X 2\right)=\right.$ k2_tarski (k4_binop_2 X0 X2) (k4_binop_2 X1 X2))))

