

t7_bhsp_6 (TMXd-
VhD7LMgo8dHcNkLwyCj8SFMMeQPUoCwg)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v13_algstr_0 : \iota \Rightarrow o$ be given. Let $v2_rlvect_1 : \iota \Rightarrow o$ be given. Let $v3_rlvect_1 : \iota \Rightarrow o$ be given. Let $v4_rlvect_1 : \iota \Rightarrow o$ be given. Let $v5_rlvect_1 : \iota \Rightarrow o$ be given. Let $v6_rlvect_1 : \iota \Rightarrow o$ be given. Let $v7_rlvect_1 : \iota \Rightarrow o$ be given. Let $v8_rlvect_1 : \iota \Rightarrow o$ be given. Let $v2_bhsp_1 : \iota \Rightarrow o$ be given. Let $l1_bhsp_1 : \iota \Rightarrow o$ be given. Let $v1_binop_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_algstr_0 : \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v2_binop_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_setwiseo : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $v3_bhsp_6 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $v2_hahnban : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v3_hahnban : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_bhsp_6 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_bhsp_6 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_xxreal_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_numbers : \iota$ be given. Let $v1_finset_1 : \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k18_complex1 : \iota \Rightarrow \iota$ be given. Let $k10_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_bhsp_5 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k33_binop_2 : \iota$ be given. Let $k5_algstr_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_bhsp_6 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k11_binop_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_bhsp_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the

following.

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v5_rlvect_1 X0) \wedge \\
& ((v6_rlvect_1 X0) \wedge ((v7_rlvect_1 X0) \wedge ((v8_rlvect_1 X0) \wedge ((v2_bhsp_1 \\
& X0) \wedge (l1_bhsp_1 X0)))))))))) \Rightarrow (((v1_binop_1 (u1_algstr_0 X0) \\
& (u1_struct_0 X0)) \wedge ((v2_binop_1 (u1_algstr_0 X0) (u1_struct_0 \\
& X0)) \wedge (v1_setwiseo (u1_algstr_0 X0) (u1_struct_0 X0))) \Rightarrow (\forall X1. \\
& (m1_subset_1 X1 (k1_zfmisc_1 (u1_struct_0 X0))) \Rightarrow (\neg (v3_bhsp_6 \\
& X1 X0) \wedge (\forall X2. (m1_subset_1 X2 (u1_struct_0 X0)) \Rightarrow (\exists X3. \\
& ((v1_funct_1 X3) \wedge ((v1_funct_2 X3 (u1_struct_0 X0) k1_numbers) \wedge \\
& ((v2_hahnban X3 X0) \wedge ((v3_hahnban X3 X0) \wedge (m1_subset_1 X3 (k1_zfmisc_1 \\
& (k2_zfmisc_1 (u1_struct_0 X0) k1_numbers)))))) \wedge ((v2_bhsp_6 \\
& X3 X0) \wedge (\exists X4. (m1_subset_1 X4 k1_numbers) \wedge ((\neg r1_xxreal_0 \\
& X4 k6_numbers) \wedge (\forall X5. ((v1_finset_1 X5) \wedge (m1_subset_1 X5 \\
& (k1_zfmisc_1 (u1_struct_0 X0)))) \Rightarrow (\neg (\neg v1_xboole_0 X5) \wedge ((r1_tarski \\
& X5 X1) \wedge (\forall X6. ((v1_finset_1 X6) \wedge (m1_subset_1 X6 (k1_zfmisc_1 \\
& (u1_struct_0 X0)))) \Rightarrow (\neg (r1_tarski X5 X6) \wedge ((r1_tarski X6 X1) \wedge (\\
& r1_xxreal_0 X4 (k18_complex1 (k10_binop_2 (k3_funct_2 (u1_struct_0 \\
& X0) k1_numbers X3 X2) (k5_bhsp_5 k1_numbers (u1_struct_0 X0) k33_binop_2 \\
& X6 X3)))))))))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1_xboole_0 X0) \wedge \\
& (((v1_funct_1 X2) \wedge ((v1_funct_2 X2 X0 X1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\
& (k2_zfmisc_1 X0 X1)))))) \wedge (m1_subset_1 X3 X0)) \Rightarrow (m1_subset_1 (\\
& k3_funct_2 X0 X1 X2 X3) X1)
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v5_rlvect_1 X0) \wedge \\
& ((v6_rlvect_1 X0) \wedge ((v7_rlvect_1 X0) \wedge ((v8_rlvect_1 X0) \wedge ((v2_bhsp_1 \\
& X0) \wedge (l1_bhsp_1 X0)))))))))) \Rightarrow (\forall X1. (m1_subset_1 X1 (k1_zfmisc_1 \\
& (u1_struct_0 X0))) \Rightarrow (\forall X2. ((v1_funct_1 X2) \wedge ((v1_funct_2 \\
& X2 (u1_struct_0 X0) k1_numbers) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\
& (k2_zfmisc_1 (u1_struct_0 X0) k1_numbers)))))) \Rightarrow ((r1_bhsp_6 X0 \\
& X1 X2) \Leftrightarrow (\exists X3. (m1_subset_1 X3 k1_numbers) \wedge (\forall X4. (\\
& m1_subset_1 X4 k1_numbers) \Rightarrow (\neg (\neg r1_xxreal_0 X4 k6_numbers) \wedge (\\
& \forall X5. ((v1_finset_1 X5) \wedge (m1_subset_1 X5 (k1_zfmisc_1 (u1_struct_0 \\
& X0)))) \Rightarrow (\neg (\neg v1_xboole_0 X5) \wedge ((r1_tarski X5 X1) \wedge (\forall X6. (\\
& (v1_finset_1 X6) \wedge (m1_subset_1 X6 (k1_zfmisc_1 (u1_struct_0 X0)))) \Rightarrow \\
& (\neg (r1_tarski X5 X6) \wedge ((r1_tarski X6 X1) \wedge (r1_xxreal_0 X4 (k18_complex1 \\
& (k10_binop_2 X3 (k5_bhsp_5 k1_numbers (u1_struct_0 X0) k33_binop_2 \\
& X6 X2)))))))))))))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v5_rlvect_1 X0) \wedge \\
& ((v6_rlvect_1 X0) \wedge ((v7_rlvect_1 X0) \wedge ((v8_rlvect_1 X0) \wedge ((v2_bhsp_1 \\
& X0) \wedge (l1_bhsp_1 X0)))))))))) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 \\
& (u1_struct_0 X0))) \Rightarrow ((v3_bhsp_6 X1 X0) \Leftrightarrow (\exists X2.(m1_subset_1 \\
& X2 (u1_struct_0 X0)) \wedge (\forall X3.((v1_funct_1 X3) \wedge ((v1_funct_2 \\
& X3 (u1_struct_0 X0) k1_numbers) \wedge ((v2_hahnban X3 X0) \wedge ((v3_hahnban \\
& X3 X0) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 (u1_struct_0 \\
& X0) k1_numbers)))))) \Rightarrow ((v2_bhsp_6 X3 X0) \Rightarrow (\forall X4.(m1_subset_1 \\
& X4 k1_numbers) \Rightarrow (\neg(\neg r1_xxreal_0 X4 k6_numbers) \wedge (\forall X5.(\\
& (v1_finset_1 X5) \wedge (m1_subset_1 X5 (k1_zfmisc_1 (u1_struct_0 X0)))) \Rightarrow \\
& (\neg(\neg v1_xboole_0 X5) \wedge (r1_tarski X5 X1) \wedge (\forall X6.((v1_finset_1 \\
& X6) \wedge (m1_subset_1 X6 (k1_zfmisc_1 (u1_struct_0 X0)))) \Rightarrow (\neg(r1_tarski \\
& X5 X6) \wedge (r1_tarski X6 X1) \wedge (r1_xxreal_0 X4 (k18_complex1 (k3_funct_2 \\
& (u1_struct_0 X0) k1_numbers X3 (k5_algstr_0 X0 X2 (k1_bhsp_6 X0 \\
& X6)))))))))))))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v5_rlvect_1 X0) \wedge \\
& ((v6_rlvect_1 X0) \wedge ((v7_rlvect_1 X0) \wedge ((v8_rlvect_1 X0) \wedge ((v2_bhsp_1 \\
& X0) \wedge (l1_bhsp_1 X0)))))))))) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge \\
& ((v1_funct_2 X1 (u1_struct_0 X0) k1_numbers) \wedge ((v2_hahnban X1 \\
& X0) \wedge ((v3_hahnban X1 X0) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 \\
& (u1_struct_0 X0) k1_numbers)))))) \Rightarrow ((v2_bhsp_6 X1 X0) \Leftrightarrow (\exists X2. \\
& (m1_subset_1 X2 k1_numbers) \wedge (\neg r1_xxreal_0 X2 k6_numbers) \wedge \\
& \forall X3.(m1_subset_1 X3 (u1_struct_0 X0)) \Rightarrow (r1_xxreal_0 (k18_complex1 \\
& (k3_funct_2 (u1_struct_0 X0) k1_numbers X1 X3)) (k11_binop_2 X2 \\
& (k3_bhsp_1 X0 X3)))))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\forall X0.(v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (k1_zfmisc_1 X0)) \Rightarrow (v1_xboole_0 X1)) \tag{6}$$

Theorem 1

$$\begin{aligned} & \forall X0. ((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\ & X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v5_rlvect_1 X0) \wedge \\ & ((v6_rlvect_1 X0) \wedge ((v7_rlvect_1 X0) \wedge ((v8_rlvect_1 X0) \wedge ((v2_bhsp_1 \\ & X0) \wedge (l1_bhsp_1 X0)))))))))) \Rightarrow (((v1_binop_1 (u1_algstr_0 X0) \\ & (u1_struct_0 X0)) \wedge ((v2_binop_1 (u1_algstr_0 X0) (u1_struct_0 \\ & X0)) \wedge (v1_setwiseo (u1_algstr_0 X0) (u1_struct_0 X0)))) \Rightarrow (\forall X1. \\ & (m1_subset_1 X1 (k1_zfmisc_1 (u1_struct_0 X0))) \Rightarrow ((v3_bhsp_6 \\ & X1 X0) \Rightarrow (\forall X2. ((v1_funct_1 X2) \wedge ((v1_funct_2 X2 (u1_struct_0 \\ & X0) k1_numbers) \wedge ((v2_hahnban X2 X0) \wedge ((v3_hahnban X2 X0) \wedge (m1_subset_1 \\ & X2 (k1_zfmisc_1 (k2_zfmisc_1 (u1_struct_0 X0) k1_numbers)))))) \Rightarrow \\ & ((v2_bhsp_6 X2 X0) \Rightarrow (r1_bhsp_6 X0 X1 X2)))))) \end{aligned}$$