

t7_funct_6

(TMaceYFnYco8DxoLnUJeHK8PNXX2m3iY9gT)

October 27, 2020

Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k10_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k2_funct_5 : \iota \Rightarrow \iota$ be given. Let $k4_funct_5 : \iota \Rightarrow \iota$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_binop_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((v1_relat_1 X2) \wedge (v1_funct_1 \\ & X2)) \Rightarrow (\forall X3. ((v1_relat_1 X3) \wedge (v1_funct_1 X3)) \Rightarrow (((X0 \in k9_xtuple_0 \\ & X2) \wedge ((X3 = k1_funct_1 X2 X0) \wedge (X1 \in k9_xtuple_0 X3))) \Rightarrow ((k4_tarski \\ & X1 X0 \in k9_xtuple_0 (k4_funct_5 X2)) \wedge ((k1_binop_1 (k4_funct_5 \\ & X2) X1 X0 = k1_funct_1 X3 X1) \wedge (k1_funct_1 X3 X1 \in k10_xtuple_0 (k4_funct_5 \\ & X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((v1_relat_1 X2) \wedge (v1_funct_1 \\ & X2)) \Rightarrow (\forall X3. ((v1_relat_1 X3) \wedge (v1_funct_1 X3)) \Rightarrow (((X0 \in k9_xtuple_0 \\ & X2) \wedge ((X3 = k1_funct_1 X2 X0) \wedge (X1 \in k9_xtuple_0 X3))) \Rightarrow ((k4_tarski \\ & X0 X1 \in k9_xtuple_0 (k2_funct_5 X2)) \wedge ((k1_binop_1 (k2_funct_5 \\ & X2) X0 X1 = k1_funct_1 X3 X1) \wedge (k1_funct_1 X3 X1 \in k10_xtuple_0 (k2_funct_5 \\ & X2)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. (r1_tarski X0 X1) \Leftrightarrow (\forall X2. (X2 \in X0) \Rightarrow (X2 \in X1)) \tag{3}$$

Assume the following.

$$\forall X0. ((v1_relat_1 X0) \wedge (v1_funct_1 X0)) \Rightarrow (\forall X1. (X1 = k10_xtuple_0 X0) \Leftrightarrow (\forall X2. (X2 \in X1) \Leftrightarrow (\exists X3. (X3 \in k9_xtuple_0 X0) \wedge (X2 = k1_funct_1 X0 X3)))) \tag{4}$$

Theorem 1

$$\begin{aligned} & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge (v1_funct_1 X1)) \Rightarrow (\forall X2. \\ & ((v1_relat_1 X2) \wedge (v1_funct_1 X2)) \Rightarrow (((X0 \in k9_xtuple_0 X1) \wedge (X2 = \\ & k1_funct_1 X1 X0)) \Rightarrow ((r1_tarski (k10_xtuple_0 X2) (k10_xtuple_0 \\ & (k2_funct_5 X1))) \wedge (r1_tarski (k10_xtuple_0 X2) (k10_xtuple_0 \\ & (k4_funct_5 X1))))) \end{aligned}$$