

t7\_scmpds\_3  
(TMLBfW4Qs3ER4Jz3qoXUxyfuyqLQ5eSEDEK)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_scmpds\_2 : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v5\_funct\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_ami\_2 : \iota$  be given. Let  $v2\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_numbers : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $l1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_compos\_1 : \iota \Rightarrow o$  be given. Let  $v1\_setfam\_1 : \iota \Rightarrow o$  be given. Let  $v1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & ((v2\_xxreal\_0 \ np\_2) \wedge (m2\_subset\_1 \ np\_2 \ k1\_numbers \ k5\_numbers)) \wedge \\ & ((m1\_subset\_1 \ np\_2 \ k5\_numbers) \wedge (m1\_subset\_1 \ np\_2 \ k1\_numbers)) \end{aligned} \quad (1)$$

Assume the following.

$$\neg v1\_xboole\_0 \ np\_2 \quad (2)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v1\_relat\_1 \ X1) \wedge ((v4\_relat\_1 \\ & \ X1 \ X0) \wedge ((v1\_funct\_1 \ X1) \wedge (v1\_partfun1 \ X1 \ X0)))) \wedge ((v1\_relat\_1 \\ & \ X2) \wedge ((v4\_relat\_1 \ X2 \ X0) \wedge (v1\_funct\_1 \ X2)))) \Rightarrow ((v1\_relat\_1 \ (k1\_funct\_4 \\ & \ X1 \ X2)) \wedge ((v4\_relat\_1 \ (k1\_funct\_4 \ X1 \ X2) \ X0) \wedge ((v1\_funct\_1 \ (k1\_funct\_4 \\ & \ X1 \ X2)) \wedge (v1\_partfun1 \ (k1\_funct\_4 \ X1 \ X2) \ X0)))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. ((v1\_relat\_1 \ X0) \wedge (v1\_funct\_1 \ X0)) \Rightarrow ((v1\_relat\_1 \ (k5\_relat\_1 \ X0 \ X1)) \wedge (v1\_funct\_1 \ (k5\_relat\_1 \ X0 \ X1))) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge(v4\_relat\_1 X1 X0)\wedge(v1\_funct\_1 X1))\wedge((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge(v1\_funct\_1 X2))))\Rightarrow((v1\_relat\_1 (k1\_funct\_4 X1 X2))\wedge((v4\_relat\_1 (k1\_funct\_4 X1 X2) X0)\wedge(v1\_funct\_1 (k1\_funct\_4 X1 X2)))) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((v1\_relat\_1 X2)\wedge(v4\_relat\_1 X2 X1))\Rightarrow((v1\_relat\_1 (k5\_relat\_1 X2 X0))\wedge((v4\_relat\_1 (k5\_relat\_1 X2 X0) X0)\wedge(v4\_relat\_1 (k5\_relat\_1 X2 X0) X1))) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1))\wedge((v1\_relat\_1 X2)\wedge((v1\_funct\_1 X2)\wedge(v5\_funct\_1 X2 X1))))\Rightarrow((v1\_relat\_1 (k5\_relat\_1 X2 X0))\wedge(v5\_funct\_1 (k5\_relat\_1 X2 X0) X1)) \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(((v1\_relat\_1 X0)\wedge(v1\_funct\_1 X0))\wedge(((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v5\_funct\_1 X1 X0)))\wedge((v1\_relat\_1 X2)\wedge((v1\_funct\_1 X2)\wedge(v5\_funct\_1 X2 X0)))))\Rightarrow((v1\_relat\_1 (k1\_funct\_4 X1 X2))\wedge((v1\_funct\_1 (k1\_funct\_4 X1 X2))\wedge(v5\_funct\_1 (k1\_funct\_4 X1 X2) X0))) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(l1\_extpro\_1 X1 X0)\Rightarrow((l1\_memstr\_0 X1 X0)\wedge(l1\_compos\_1 X1)) \quad (10)$$

Assume the following.

$$\forall X0.\forall X1.(v1\_relat\_1 X0)\Rightarrow(v1\_relat\_1 (k5\_relat\_1 X0 X1)) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_setfam\_1 X0)\wedge(l1\_memstr\_0 X1 X0))\Rightarrow((v1\_relat\_1 (k2\_memstr\_0 X0 X1))\wedge((v4\_relat\_1 (k2\_memstr\_0 X0 X1) (u1\_struct\_0 X1))\wedge((v1\_funct\_1 (k2\_memstr\_0 X0 X1))\wedge(v1\_partfun1 (k2\_memstr\_0 X0 X1) (u1\_struct\_0 X1)))))) \quad (12)$$

Assume the following.

$$(v1\_extpro\_1 k1\_scmpds\_2 np\_2)\wedge(l1\_extpro\_1 k1\_scmpds\_2 np\_2) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge(v1\_funct\_1 X0))\wedge((v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1)))\Rightarrow((v1\_relat\_1 (k1\_funct\_4 X0 X1))\wedge(v1\_funct\_1 (k1\_funct\_4 X0 X1))) \quad (14)$$

Assume the following.

$$\forall X0.(m1\_subset\_1 X0 k4\_ordinal1)\Rightarrow(v7\_ordinal1 X0) \quad (15)$$

Assume the following.

$$\forall X0.((\neg v1\_xboole\_0 X0)\wedge(v7\_ordinal1 X0))\Rightarrow((\neg v1\_xboole\_0 X0)\wedge((v7\_ordinal1 X0)\wedge(\neg v1\_setfam\_1 X0))) \quad (16)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0)\wedge((v4\_relat\_1 X0 (u1\_struct\_0 k1\_scmpds\_2))\wedge \\ & ((v1\_funct\_1 X0)\wedge((v5\_funct\_1 X0 (k2\_memstr\_0 np\_2 k1\_scmpds\_2))\wedge \\ & (v1\_partfun1 X0 (u1\_struct\_0 k1\_scmpds\_2))))))\Rightarrow(\forall X1. \\ & ((v1\_relat\_1 X1)\wedge((v4\_relat\_1 X1 (u1\_struct\_0 k1\_scmpds\_2))\wedge \\ & ((v1\_funct\_1 X1)\wedge((v5\_funct\_1 X1 (k2\_memstr\_0 np\_2 k1\_scmpds\_2))\wedge \\ & (v1\_partfun1 X1 (u1\_struct\_0 k1\_scmpds\_2))))))\Rightarrow((v1\_relat\_1 \\ & (k1\_funct\_4 X0 (k5\_relat\_1 X1 k2\_ami\_2)))\wedge((v4\_relat\_1 (k1\_funct\_4 \\ & X0 (k5\_relat\_1 X1 k2\_ami\_2)) (u1\_struct\_0 k1\_scmpds\_2))\wedge((v1\_funct\_1 \\ & (k1\_funct\_4 X0 (k5\_relat\_1 X1 k2\_ami\_2)))\wedge((v5\_funct\_1 (k1\_funct\_4 \\ & X0 (k5\_relat\_1 X1 k2\_ami\_2)) (k2\_memstr\_0 np\_2 k1\_scmpds\_2))\wedge \\ & (v1\_partfun1 (k1\_funct\_4 X0 (k5\_relat\_1 X1 k2\_ami\_2)) (u1\_struct\_0 \\ & k1\_scmpds\_2))))))))) \end{aligned}$$